

STUDENT SUPPORT MATERIAL SESSION: 2022-23







केन्द्रीय विद्यालय संगठन क्षेत्रीय कार्यालय एर्नाकुलम KENDRIYA VIDYALAYA SANGATHAN ERNAKULAM REGION

Based on the latest CBSE Exam Pattern for the Session 2022 - 23

STUDENT SUPPORT MATERIAL



INSPIRATION



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Preface

This Study Material is an in-house academic exercise undertaken by the Maths teachers of KVS Ernakulam Region under the supervision of a subject expert, Smt.Bindu Lekshmy P L, Principal, KV Chenneerkara, to provide the students a comprehensive, yet concise, support tool for consolidation of learning.

It consists of curriculum, deleted topics and questions from all chapters. This material is developed keeping in mind the latest CBSE curriculum and pattern of the question paper. It will definitely provide the students a valuable window on precise information and it covers all essential components that are required for effective revision of the subject.

Hoping this material will prove to be a helpful tool for quick revision and will serve the purpose of enhancing students' confidence level to help them perform better.

Best of Luck.



आर सेन्दिल कुमार उपायुक्त R. Senthíl Kumar Deputy Commissioner



F.31/Acad/KVS(EKM)



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Date : 03/10/2022

MESSAGE FROM DEPUTY COMMISSIONER

I am extremely elated to bring out the study material for Class X Mathematics. The material is prepared with the aim of equipping students with the necessary inputs incorporating all the latest changes in curriculum and assessment patterns framed by CBSE. It is designed to be of help to class X students, guiding them for effective Board Examination Preparation.

The Support Study Material covers all the important aspects like design and blueprint of question paper, Split Up Syllabus, Concept Map of Summary of chapters, important formulas, Sample question papers and models of Problem Solving and Case Study questions. Tips for preparation of Portfolio, Art Integrated Project etc., will be of immense help to the students. All efforts have been taken to provide a comprehensive set of sample questions from every topic and I hope that this will be used extensively by students and their teachers.

Let me express my gratitude and appreciation to the team of dedicated members whose consistent research and hard work produced this excellent study material. Their efforts are worthy of praise.

Persistent hard work and meticulous revision of such study materials taken up by the students will certainly result in glorious achievements in the forthcoming Board examinations.

I hope this study material is harnessed as a tool for producing excellence.

With Best Wishes

(R SENTHIL KUMAR) DEPUTY COMMISSIONER



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MATHEMATICS (CODE NO. 041)

COURSE STRUCTURE CLASS –X

UNITS	UNIT NAME	MARKS
Ι	NUMBER SYSTEM	6
II	ALGEBRA	20
III	CO-ORDINATE GEOMETRY	6
IV	GEOMETRY	15
V	TRIGONOMETRY	12
VI	MENSURATION	10
VII	STATISTICS & PROBABILITY	11
	TOTAL	80
	INTERNAL ASSESSMENT	20
	TOTAL	100

INTERNAL ASSESSMENT

INTERNAL ASSESSMENT	marks	TOTAL MARKS
Pen Paper Test and Multiple Assessment (5+5)	10marks	
Portfolio	05 marks	20 marks
Lab Practical (Lab activities to be done from the prescribed books)	05 marks	

UNIT I: NUMBER SYSTEMS

1. REAL NUMBER

(15) periods

Fundamental Theorem of Arithmetic - statements after reviewing work done earlier and after illustrating and motivating through examples, Proofs of irrationality of $\sqrt{2}$, $\sqrt{3}$, $\sqrt{5}$

UNIT II: ALGEBRA

1. POLYNOMIALS (8) periods Zeros of a polynomial. Relationship between zeros and coefficients of quadratic polynomials.

2. PAIR OF LINEAR EQUATIONS IN TWO VARIABLES

(15) Periods Pair of linear equations in two variables and graphical method of their solution, consistency/inconsistency. Algebraic conditions for number of solutions. Solution of a pair of linear equations in two variables algebraically - by substitution, by elimination. Simple situational problems.

3. QUADRATIC EQUATIONS Standard form of a quadratic equation $ax^2 + bx + c = 0$, $(a \neq 0)$. Solutions of quadratic equations (only real roots) by factorization, and by using quadratic formula. Relationship between discriminant and nature of roots. Situational problems based on quadratic equations related to day to day activities to be incorporated.

4. ARITHMETIC PROGRESSIONS (10) Periods Motivation for studying Arithmetic Progression. Derivation of the nth term and sum of the first n terms of A.P. and their application in solving daily life problems.

UNIT III: CO-ORDINATE GEOMETRY

Co-ordinate Geometry

Review: Concepts of co-ordinate geometry, graphs of linear equations. Distance formula. Section formula (internal division).

UNIT IV: GEOMETRY

1. TRIANGLES

Definitions, examples, counter examples of similar triangles.

- 1. (Prove) If a line is drawn parallel to one side of a triangle to intersect the other two sides in distinct points, the other two sides are divided in the same ratio.
- 2. (Motivate) If a line divides two sides of a triangle in the same ratio, the line is parallel to the third side.
- 3. (Motivate) If in two triangles, the corresponding angles are equal, their corresponding sides are proportional and the triangles are similar.
- 4. (Motivate) If the corresponding sides of two triangles are proportional, their corresponding angles are equal and the two triangles are similar.
- 5. (Motivate) If one angle of a triangle is equal to one angle of another triangle and the sides including these angles are proportional, the two triangles are similar.

2. CIRCLES

Tangent to a circle at, point of contact

(10) Periods



2

(15) Periods

(15) Periods

(15) Periods



- 1. (Prove) The tangent at any point of a circle is perpendicular to the radius through the point of contact.
- 2. (Prove) The lengths of tangents drawn from an external point to a circle are equal.

UNIT V: TRIGONOMETRY

- INTRODUCTION TO TRIGONOMETRY (10) Periods Trigonometric ratios of an acute angle of a right-angled triangle. Proof of their existence (well defined); motivate the ratios whichever are defined at 0° and 90°. Values of the trigonometric ratios of 30°, 45° and 60°. Relationships between the ratios.
- 2. TRIGONOMETRIC IDENTITIES (15) Periods Proof and applications of the identity $\sin^2 A + \cos^2 A = 1$. Only simple identities to be given.
- HEIGHTS AND DISTANCES: Angle of elevation, Angle of Depression. (10) Periods Simple problems on heights and distances. Problems should not involve more than two right triangles. Angles of elevation / depression should be only 30°, 45°, and 60°.

UNIT VI: MENSURATION

- AREAS RELATED TO CIRCLES (12) Periods Area of sectors and segments of a circle. Problems based on areas and perimeter / circumference of the above said plane figures. (In calculating area of segment of a circle, problems should be restricted to central angle of 60°, 90° and 120° only.
- 2. SURFACE AREAS AND VOLUMES (12) Periods Surface areas and volumes of combinations of any two of the following: cubes, cuboids, spheres, hemispheres and right circular cylinders/cones.

UNIT VII: STATISTICS AND PROBABILITY

- 1. STATISTICS (18) Periods Mean, median and mode of grouped data (bimodal situation to be avoided).
- 2. PROBABILITY (10) Periods Classical definition of probability. Simple problems on finding the probability of an event.



DELETED TOPICS

CHAPTER NAME	PAGE NUMBERS	DROPPED TOPICS
REAL NUMBERS	2-7 , 15-18	1.2 EUCLID'S DIVISION LEMMA 1.5 REVISITING RATIONAL NUMBERS AND THEIR DECIMAL EXPANSION
POLYNOMIALS	33-37	DIVISION OF ALGORITHM FOR POLYNOMIALS
PAIR OF LINEAR EQUATIONS IN TWO VARIABLES	PAGE 67 EXERCISE 3.6 COMPLETELY DELETED	 3.4 CROSS MULTIPLICATION METHOD (ONLY METOD, NOT QUESTIONS) 3-5 EQUATIONS REDUCIBLE TO A PAIR OF LINEAR EQUATIONS IN 2 VARIABLES.
QUADRATIC EQUATIONS	77 - 82	4.4SOLUTION OF A QUADRATIC EQUATION BY COMPLETING THE SQUARE (ONLY METHOD IS DELETED)
ARITHMETIC PROGRESSION		NO DELETION
TRIANGLES		Theorem 6.2 converse of BPT Theorem 6.3 Theorem 6.4 Theorem 6.5 Exercise 6.4 completely DELETED Theorem 6.7, Pythagoras theorem 6.8, .6.9 CONVERSE Exercise 6.5 completely deleted
COORDINATE GEOMETRY	168 - 170	AREA OF A TRIANGLE EXERCISE 7.3 DELETED
INTRODUCTION TO TRIGONOMETRY	187 - 190	TRIGONOMETRIC RATIOS OF COMPLEMENTARY ANGLES 8.2 DELETED 8.3 DELETED 8.4 (QN NO 3)
APPLICATIONS OF TRIGONOMETRY		NO DELETION
CIRCLES		NO DELETION
AREA RELATED TO CIRCLES	231 - 238	PLANE FIGURES INVOLVING TRIANGLES, SIMPLE QUADRILATERALS AND CIRCLE(COMBINATION OF PLANE FIGURES)



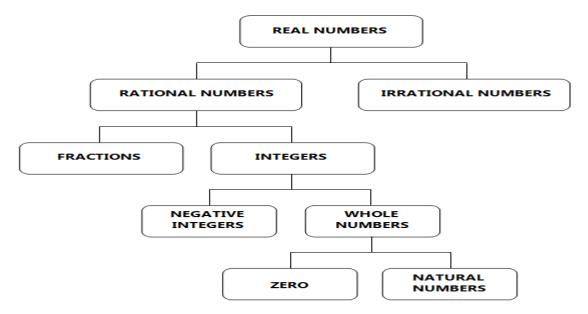
	1	
		IN CALCULATING AREA OF A
		SEGMENTOF A CIRCLE
		PROBLEMS SHOULD BE
		RESTRICTED TO THE CENTRAL
		ANGLES OF 60° 90° AND 120°
		ONLY.
		EXAMPLE 2 IN PAGE 228 IS
		DELETED
		EXERCISE 12.2(QNS 11& 12)
		DELETED
		EXERCISE12.3 DELETED,
SURFACE AREAS AND	247, 249 - 258	Example 7 in page no 247 deleted
VOLUMES		In 13.2 QUESTIONS 5 and 7 deleted
		CONVERSION OF SOLID FROM
		ONE SHAPE TO ANOTHER
		EXERCISE 13.3 COMPLETELY
		DELETED
		FRUSTUM OF A CONE DELETED
		AND RELATED EXERCISE 13.4
		DELETED
STATISTICS	289-291	GRAPHICAL REPRESENTATION
		OF CUMULATIVE FREQUENCY
		DISTRIBUTION
		EXERCISE 14.4 DELETED
PROBABILITY		NO DELETION



<u>UNIT - 1</u>

REAL NUMBERS

IMPORTANT FORMULAS & CONCEPTS



The Fundamental Theorem of Arithmetic

Every composite number can be expressed (factorised) as a product of primes, and this factorisation is unique, apart from the order in which the prime factors occur.

Prime and Composite numbers

A prime number is a number which has only two factors i.e. one and itself whereas the composite number is a number which has more than two factors.

HCF and LCM of numbers

HCF is the highest common factor also known as GCD i.e. greatest common divisor.

LCM of two numbers is their least common multiple.

Property of HCF and LCM of two positive integers 'a' and 'b':

HCF (a, b)×LCM (a, b) = a ×b

HCF and LCM by Prime factorization method

 \blacktriangleright HCF (a, b) = Product of the smallest power of each common prime factor in the numbers.

 \blacktriangleright LCM (a, b) = Product of the greatest power of each prime factor, involved in the numbers.



MULTIPLE CHOICE QUESTIONS AND OBJECTIVE QUESTIONS (1 MARK): SECTION A

		<u>BECHON M</u>				
HCF	of 8, 9, 25 is					
a)	8		c)	25		
b)	9		d)	1		
press	98 as a product of its p	rimes				
a)	$2^2 \times 7$		c)	2×7^2		
b)	$2^2 \times 7^2$		d)	$2^3 \times 7$		
If the	e LCM of a and 18 is 3	6 and the HCF of a and 18	is 2	, then a =?		
a)	2	b) 3	c)	4	d)	1
If H	CF(26, 169) = 13, the	n LCM (26, 169) is				
a)	26		c)	338		
b)	52		d)	13		
The	product of a rational ar	nd irrational number is				
a) [Rational		c)	both of above		
b) [Irrational		d) 1	none of above		
If H	CF(16, y) = 8 and LCN	M(16, y) = 48, then the val	lue c	of y is		
a) 1	24		c) (8		
b)	16		d) 4	48		
The	number 'π' is					
a)	natural number		c)	irrational number		
b)	rational number		d)	rational or irrational		
The	ratio between the LCM	I and HCF of 5, 15, 20 is:				
a) (9:1					
b) -	4:3					
c)	11:1					
d)	12:1					
	 a) b) press 4 a) b) If the a) If H a) b) The p a) c) 	b) 9 press 98 as a product of its p a) $2^2 \times 7$ b) $2^2 \times 7^2$ If the LCM of a and 18 is 3 a) 2 If HCF (26, 169) = 13, then a) 26 b) 52 The product of a rational ar a) Rational b) Irrational If HCF (16, y) = 8 and LCM a) 24 b) 16 The number ' π ' is a) natural number b) rational number	HCF of 8, 9, 25 is a) 8 b) 9 press 98 as a product of its primes a) $2^2 \times 7$ b) $2^2 \times 7^2$ If the LCM of a and 18 is 36 and the HCF of a and 18 a) 2 b) 3 If HCF (26, 169) = 13, then LCM (26, 169) is a) 26 b) 52 The product of a rational and irrational number is a) Rational b) Irrational If HCF (16, y) = 8 and LCM (16, y) = 48, then the val a) 24 b) 16 The number ' π ' is a) natural number b) rational number The ratio between the LCM and HCF of 5, 15, 20 is: a) 9 : 1 b) 4 : 3 c) 11 : 1	HCF of 8, 9, 25 is a) 8 c) b) 9 d) press 98 as a product of its primes a) $2^2 \times 7$ c) b) $2^2 \times 7^2$ d) If the LCM of a and 18 is 36 and the HCF of a and 18 is 2 a) 2 b) 3 c) If HCF (26, 169) = 13, then LCM (26, 169) is a) 26 c) b) 52 d) If he product of a rational and irrational number is a) Rational c) 1 b) Irrational d) 1 If HCF (16, y) = 8 and LCM (16, y) = 48, then the value of a) 24 c) 15 b) 16 d) The number ' π ' is a) natural number c) b) rational number d) The ratio between the LCM and HCF of 5, 15, 20 is: a) 9 : 1 b) 4 : 3 c) 11 : 1	HCF of 8, 9, 25 is a) 8 c) 25 b) 9 d) 1 press 98 as a product of its primes a) $2^2 \times 7$ c) 2×7^2 b) $2^2 \times 7^2$ d) $2^3 \times 7$ If the LCM of a and 18 is 36 and the HCF of a and 18 is 2, then a =? a) 2 b) 3 c) 4 If HCF (26, 169) = 13, then LCM (26, 169) is a) 26 c) 338 b) 52 d) 13 The product of a rational and irrational number is a) Rational c) both of above b) Irrational d) none of above If HCF (16, y) = 8 and LCM (16, y) = 48, then the v= of y is a) 24 c) 8 b) 16 d) 48 The number ' π ' is a) natural number b) rational number c) irrational number b) rational number c) irrational number b) rational number c) irrational number b) rational number c) irrational number c) irrational number b) rational number c) irrational number c) irrational number c) irrational number b) rational number c) irrational number	HCF of 8, 9, 25 is a) 8 c) 25 b) 9 d) 1 press 98 as a product of its primes a) $2^2 \times 7$ c) 2×7^2 b) $2^2 \times 7^2$ d) $2^3 \times 7$ If the LCM of a and 18 is 36 and the HCF of a and 18 is 2, then a =? a) 2 b) 3 c) 4 d) If HCF (26, 169) = 13, then LCM (26, 169) is a) 26 c) 338 b) 52 d) 13 The product of a rational and irrational number is a) Rational c) both of above b) Irrational d) inone of above b) Irrational CLM (16, y) = 48, then the value of y is a) 24 c) 8 b) 16 d) 48 The number ' π ' is a) natural number c irrational number b) rational number c) irrational number b) rational number c) irrational number c) irrational number b) rational number c) irrational number b) rational number c) irrational number c) irrational number b) rational number c) irrational number c) irrational number b) rational number c) irrational irrationa



Q9. The product of a non-zero number and an irrational number is:

a) always
irrational
b) always
rational
d) one

Q10. L.C.M. of 23×32 and 22×33 is :

- a) 23 b) 33 c) 23 × 33
- Q11. Find the LCM of smallest prime and the smallest odd composite natural number

d) 22 × 32

- Q12. If p and q are two coprime numbers, then find the HCF and LCM of p and q.
- Q13. What is the greatest possible speed at which a man can walk 52 km and 91 km in an exact number of minutes?
- Q14. Prime factorization of 120 is ...
- Q15. State fundamental theorem of arithmetic
- Q16. Given that LCM (91, 26) = 182, then HCF (91, 26) is:



- Q17. The values of x and y in the given figure are:
- Q18. If the HCF of 65 and 117 is expressible in the form 65m 117, then the value of m is
 - a) 4 c) 1
 - b) 2 d) 3
- Q19. If two positive integers a and b are written as $a = p^3q^2$ and $b = pq^3$; p, q are prime numbers, then HCF (a, b) is:
- Q20. If two positive integers a, b are written as $a = xy^2$ and $b = x^3y$, where x, y are prime numbers, then find LCM (a, b).

Short Answer Type Questions (2 marks):

SECTION B

Q1. Find the prime factorization of 1152



- Q2. Show that the product of two numbers 60 and 84 is equal to the product of their HCF and LCM
- Q3. P and Q are two positive integers such that $P = p^3 q$ and $Q = (pq)^2$, where p and q are prime numbers. What is LCM (P, Q)?
- Q4. The product of two numbers is 228096 and their LCM is 66. Find their HCF.
- Q5. Prove that $\sqrt{5}$ is irrational
- Q6. What is the LCM of smallest prime number and smallest composite number?
- Q7. Prove that $\sqrt{3}$ is irrational
- Q8. Find the sum of exponents of prime factors in the prime factorization of 216?
- Q9. Prove that $\sqrt{2}$ is irrational
- Q10. The difference of the irrational numbers $5 + \sqrt{2}$ and $5 \sqrt{2}$?
- Q11. If p and q are two coprime numbers, then p^3 and q^3 are?
- Q12. Determine the prime factorisation of 2057?
- Q13. Show that $5-\sqrt{3}$ is irrational
- Q14. If $a=2^3\times3$, $b=2\times3\times5$, $c=3^n\times5$ and LCM $[a,b,c]=2^3\times3^2\times5$ then, n=?
- Q15. Explain why $3 \times 5 \times 7 + 7$ is a composite number.
- Q16. If n is an even prime number then, $2(7^n + 8^n)$ ends with?
- Q17. Can the number 4n, n being a natural number, end with the digit 0? Give reasons.
- Q18. If the HCF of 408 and 1032 is expressible in the form 1032 m -408x5 ,find m.
- Q19. 144 cartons of coke cans and 90 cartons of Pepsi cans are to be stacked in a canteen. If each stack is of the same height and is to contain cartons of the same drink, what would be the greatest number of cartons each stack would have?
- Q20. The length, breadth and height of a room are 825 cm, 675 cm and 450 cm respectively. Find the longest tape which can measure the three dimensions of the room exactly.

SHORT ANSWER QUESTIONS (3 MARKS): SECTION C

- Q1. Find the LCM and HCF of the following pairs of positive integers by applying the prime factorization method.
 - a) 225, 240 b) 52,63,162
- Q2. Prove that $3\sqrt{2}$ is irrational



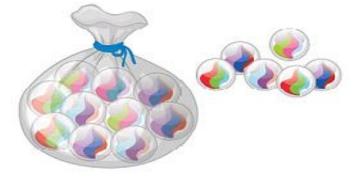
- Q3. The LCM of two numbers is 64699, their HCF is 97 and one of the numbers is 2231.Find the other.
- Q4. Two brands of chocolates are available in packs of 24 and 15 respectively. If I need to buy an equal number of chocolates of both kinds, what is the least number of boxes of each kind I would need to buy?
- Q5. If the sum of LCM and HCF of two numbers is 1260 and their LCM is 900 more than their HCF then, find the product of two numbers.
- Q6. Find HCF and LCM of 135 and 225 and verify the that HCF x LCM = Product of the two givennumbers.
- Q7. Find HCF and LCM of 867 and 255 and verify the that HCF x LCM = Product of the two given numbers
- Q8. Prove that $7 + 3\sqrt{2}$ is not a rational number.
- Q9. Prove that 2 $3\sqrt{5}$ is irrational number.
- Q10. Is $(\sqrt{2} + \sqrt{3})^2$ and $(2 \sqrt{2})(2 + \sqrt{2})$ irrational? Justify your answer.
- Q11. Prove that the difference and quotient of $(3 + 2\sqrt{3})$ and $(3 2\sqrt{3})$ are irrational.
- Q12. Prove that \sqrt{n} is not a rational number if n is not a perfect square.
- Q13. Two bells toll at intervals of 24 minutes and 36 minutes respectively. If they toll together at 9am, after how many minutes do they toll together again, at the earliest?
- Q14. There are 44 boys and 32 girls in a class. These students arranged in rows for a prayer in such a way that each row consists of only either boys or girls, and every row contains an equal number of students. Find the minimum number of rows in which all students can be arranged.
- Q15. The LCM of two number is 14 times their HCF. The sum of LCM and HCF is 600.If one numberis 280, then find the other number.
- Q16. 144 Cartons of coke can and 90 cartons of Pepsi can are to be stacked in a canteen. If eachstack is of the same height and is to contain cartons of the same drink. What would be the greater number of cartons each stack would have?
- Q17. Find the largest number that will divide 398, 436 and 542 leaving reminders7,11 and 15respectively.
- Q18. Find the largest number which divides 70 and 125 leaving reminder 5 and 8 respectively.



- Q19. Explain why 17 x 5 x 11 x 3 x 2 + 2 x11 is a composite number.
- Q20. Can two numbers have 15 as their HCF and 175 as their LCM? Give reasons.

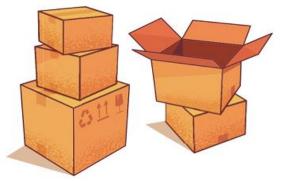
Long Answer Type Questions (4 marks): SECTION D

- Q1. Prove that $\sqrt{5}$ is an irrational number
- Q2. Find HCF and LCM of 378, 180 and 420 by prime factorization method. Is HCF X LCM of these numbers equal to the product of given three numbers?
- Q3. The sum of LCM and HCF of two numbers is 7380. If the LCM of these numbers is 7340 more than their HCF. Find the product of the two numbers
- Q4. A charitable trust donates 28 different books of Maths,16 different books of science and 12 different books of Social Science to the poor students. Each student is given maximum number of books of only one subject of his interest and each student got equal number of books
 - i. Find the number of books each student got.
 - ii. Find the total number of students who got books.
- Q5. When the marbles in a bag are divided evenly between two friends, there is one marble left over When the same marbles are divided evenly among three friends, there is one marble left over .When the marbles are divided evenly among five friends, there is one marble left over.



- i. What is the least possible number of marbles in the bag?
- ii. What is another possible number of marbles in the bag?
- Q6. Flipkart is an Indian e-commerce company, headquartered in Bangalore, Karnataka and incorporated in Singapore as a private limited company. The company initially focussed on online book sales before expanding into other product categories such as consumer electronics fashion, home essentials groceries and lifestyle products.





Flipkart sells 10 types of items which are packed into various sizes of cartons which are packed into various size of cartons which are given below

Carton type	Inner Dimension (1 X b)
	cm ²
Small	6 x 8
Medium	12 x 24
Large	24 x 36
Extra Large	36 x 48
XXL	48 x 96

Flipkart places supporting thermocol sheets inside every package along the edges. The company thought of buying same sized sheets for all type of cartons

- i. What should be the maximum size of the sheet that fits into all type of cartons?
- ii. What should have been size of semi large (which is larger than medium carton but smaller than large carton) so that the maximum sized sheet remains same?
- Q7. Kerosene, paraffin, or lamp oil is a combustible hydrocarbon liquid which is derivative from petroleum. Kerosen's uses vary from fuel for oil lamps to cleaning agents , jet fuel , heating oil or fuel for cooking



Two oil tankers contain 825 litres and 675 litres of kerosene oil respectively.

- i. Find the maximum capacity of a container which can measure the Kerosene oil of both the tankers when used an exact number of times.
- ii. How many times we have to use container for both the tanker to fill?
- Q8. Amar, Akbar and Anthony are playing a game. Amar climbs 5 stairs and gets down



2 stairs in one turn .Akbar goes up by 7 stairs and comes down by 2 stairs every time. Anthony goes 10 stairs up and 3 stairs down each time.



During this they have to reach to the nearest point of 100th stairs and they will stop once they find it impossible to go forward. They can not cross 100th stair any way

- i. Who reaches the nearest point?
- ii. Who takes least number of steps to reach nearest hundred?
- Q9. A woman wants to organise her birthday party. She was happy on her birthday but there was a problem that she does not want to serve fast food to her guests because she is very health conscious. She as 15 apples and 40 bananas at home and decided to serve them. She want to distribute fruits among guests. She does not want to discriminate among guests so she decided to distribute equally among all. So
 - i. How many guests she can invite?
 - ii. How many apples and banana will each guest get?
- Q10. A hall has a certain number of chairs. Guests want to sit in different groups like in pairs, triplets, quadruplets, fives and sixes etc. When organiser arranges chairs in such pattern like 2's, 3's ,4's.5's and 6's then 1,2,3,4 and 5 chairs are left respectively. But when he arranges in 11's no chair will be left
 - i. In the hall how many chairs are available?
 - a) 407
 - b) 143
 - c) 539
 - d) 209
 - ii. If one chair is added to the total number of chairs, how many chairs will be left when arranged in 11's

ANSWER KEY



1d) 12c) 2×7^2 3c) 44c) 3385b) irrational6a) 247c) Irrational number8d) 12 : 19(a) Always irrational10c) $2^3 \times 3^3$ 11LCM of 2 and 4 is 412HCF = 1 and LCM = pq1313m / min14 $2^3 \times 3 \times 5$ 15Fundamental Theorem of Arithmetic states that every integer greater than 1either a prime number or can be expressed in the form of the product of its prime factors.ORRefer textbook (Theorem 1.2 pg no. 8)16HCF = 1317 $x = 21$ and $y = 84$ 18b) 219HCF = pq ² 20 x^3y^2	Q.No.	Answer
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10	0511217
12	$2 \times 5 \times 11^2 \times 17$
13	Refer textbook (Example – 10 pg no. 14)
14	2
15	112 is an even number and is therefore a composite number
16	6
17	No
18	2
19	18
20	75 cm
Q.III Lo	ong Answer Type Questions (3 marks):
1	a)HCF (225, 240) = 15 LCM (225, 240) = 600
	b)HCF (52, 6, 162) = 1 LCM (52, 63, 162) = 29484
2	Refer textbook
3	2813
4	5 of 1 st kind, 8 of 2 nd kind
5	194400
6	LCM (135, 225) = 675, HCF (135, 225) = 45. Verification by showing
	LHS = RHS i.e., 135 x 225 = 675 x 45
7	LCM $(867, 255) = 4335$, HCF $(867, 255) = 51$. Verification by showing
	LHS = RHS i.e., 867 x 255 = 4335 x 51
8	Refer textbook
9	Refer textbook
10	$(\sqrt{2} + \sqrt{3})^2$ is irrational as the result is $5 + \sqrt{6}$, which is irrational. (2- $\sqrt{2}$)(2+ $\sqrt{2}$) is rational as the result is 2, which is rational.
11	The difference of $(3 + 2\sqrt{3})$ and $(3 - 2\sqrt{3})$ is $4\sqrt{3}$ which is irrational.
1 11	
	Dividing $(3 + 2\sqrt{3})$ by $(3 - 2\sqrt{3})$ we get $-7 - 4\sqrt{3}$ which is irrational.
11	Dividing $(3 + 2\sqrt{3})$ by $(3 - 2\sqrt{3})$ we get $-7 - 4\sqrt{3}$ which is irrational. Let on the contrary say it is rational.
	Let on the contrary say it is rational.
	Let on the contrary say it is rational. Then
	Let on the contrary say it is rational . Then $\sqrt{n=p/q}, q\neq 0$ where p and q are coprime integers.
	Let on the contrary say it is rational . Then $\sqrt{n=p/q}, q\neq 0$ where p and q are coprime integers. so $n=p2q2$ p2=nq2 This shows p divides q
	Let on the contrary say it is rational . Then $\sqrt{n=p/q}, q \neq 0$ where p and q are coprime integers. so $n=p2q2$ p2=nq2 This shows p divides q which is a contradiction.
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	Let on the contrary say it is rational . Then $\sqrt{n=p/q}, q \neq 0$ where p and q are coprime integers. so $n=p2q2$ p2=nq2 This shows p divides q which is a contradiction.
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12	Let on the contrary say it is rational . Then $\sqrt{n=p/q}, q \neq 0$ where p and q are coprime integers. so $n=p2q2$ p2=nq2 This shows p divides q which is a contradiction. Hence \sqrt{n} is irrational if n is not a perfect square. $24 = 2^3 \times 3$ $36 = 2^2 \times 3^2$ LCM = $2^3 \times 3^2 = 8 \times 9 = 72$ After 72 minutes = 1 hr 12 minutes they toll together.
12	Let on the contrary say it is rational . Then $\sqrt{n=p/q}, q \neq 0$ where p and q are coprime integers. so $n=p2q2$ p2=nq2 This shows p divides q which is a contradiction. Hence \sqrt{n} is irrational if n is not a perfect square. $24 = 2^3 \times 3$ $36 = 2^2 \times 3^2$ LCM = $2^3 \times 3^2 = 8 \times 9 = 72$
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12	Let on the contrary say it is rational . Then $\sqrt{n=p/q}, q \neq 0$ where p and q are coprime integers. so $n=p2q2$ p2=nq2 This shows p divides q which is a contradiction. Hence \sqrt{n} is irrational if n is not a perfect square. $24 = 2^3 \times 3$ $36 = 2^2 \times 3^2$ LCM = $2^3 \times 3^2 = 8 \times 9 = 72$ After 72 minutes = 1 hr 12 minutes they toll together. $44 = 2^2 \times 11$



	Therefore, minimum number of rows in which all srudents can be
	arranged = $\frac{44}{4} + \frac{32}{4} = 11 + 8 = 19$ rows
15	HCF = x
15	LCM = 14 x HCF = 14 x
	$LCM = 14 \times HCF = 14 \times LCM + HCF = 600$
	14x + x = 500
	14x + x = 500 15x = 600
	$\begin{array}{l} 15x = 000\\ x = 40 \end{array}$
	$HCF = 40$ and $LCM = 14 \times 40 = 560$
	Since, LCM x HCF = product of the numbers
	$560 \times 40 = 280 \times \text{second number}$
	Second number $= 80$
16	$144 = 2^4 \times 3^2$
	$90 = 2 \times 3^2 \times 5$
	$HCF = 2 \times 3^2 = 18 \text{ cartons}$
17	398 - 7 = 391
	436 - 11 = 425
	542 - 15 = 527
	$391 = 17 \ge 23$
	$425 = 5^2 \times 17$
	$527 = 17 \times 31$
	HCF = 17
	i.e., 17 is the largest number that will divide 398, 436 and 542
	leaving remainders 7, 11 and 15 respectively.
18	70 - 5 = 65
	125 - 8 = 117
	$65 = 5 \times 13$
	$117 = 3^2 \times 13$
	HCF = 13
10	i.e., 13 is the largest number that will divide 65 and 117.
19	$17 \times 5 \times 11 \times 3 \times 2 + 2 \times 11 = 2 \times 11 (17 \times 5 \times 3 + 1)$
	$= 2 \times 11 (255 + 1)$
	$= 2 \times 11 \times 256$
	$= 2 \times 11 \times 2^8$
	This number has more than 2 prime factors. Therefore $17 \times 5 \times 11 \times 2 \times 2 + 2 \times 11$ is a composite number
20	Therefore, $17 \times 5 \times 11 \times 3 \times 2 + 2 \times 11$ is a composite number.
20	No, two numbers cannot have 15 as their HCF and 175 as LCM because, HCF of the numbers must be a factor of the LCM.
	Therefore, $LCM = k \times HCF$ (k $\in N$)
	$175 = k \times 15$
	$k = \frac{175}{15} = \frac{35}{3} \notin N$



Q.IV V	Very Long Answer Type Questions (4 marks):	
1	Assume that $\sqrt{5}$ is a rational number	
	Therefore $\sqrt{5} = \frac{p}{q}$ p and q are co primes and $q \neq 0$	(1)
	<i>q</i>	(-)
	$p = \sqrt{5} q$ Squaring both the sides	
	$p^2 = 5q^2$	
	Thus 5 is a factor of p^2	
	Therefore 5 is a factor of p	(1)
	Let p=5c where c is some integer, then we have $p^2=25c^2$	
	Substituting $p^2=5q^2$	
	$5q^2 = 25c^2$	
	$q^2 = 5c^2$	(1) c
	Thus 5 is a factor of q^2 and also 5 is also a factor of Thus 5 is a factor of both r and q . But this is a cont	-
	Thus 5 is a factor of both p and q .But this is a contrained q are co primes	(1)
	Thus our assumption is wrong that $\sqrt{5}$ is a rational	
	Hence $\sqrt{5}$ is an irrational number	number
2	$378 = 3^3 \times 2 \times 7$	
Ζ.	$ \begin{array}{c} 378-3 \times 2 \times 7 \\ 180=3^2 \times 2^2 \times 5 \end{array} $	(1)
	$420=3 \times 2^2 \times 5 \times 7$	(1)
	HCF = 3 X 2 =6	(1)
	$LCM = 3^3 x 2^2 x 5 x 7 = 3780$	(1)
	HCF x LCM = 3780 x 6 = 22,680	
	Product of numbers = 378 x 180 x 420 = 28576800	
	No HCF x LCM is not equal to product of three num	mbers (1)
3	LCM + HCF = 7380	
	LCM - HCF = 7340	
	2LCM = 14720 LCM = 14720/2	
	LCM = 7360 (2)	
	LCM + HCF = 7380 (2)	
	7360 + HCF = 7380	
	HCF = 7380 - 7360	
	$HCF = 20 \tag{1}$	
	HCF x LCM = product of numbers	
	$20 \times 7360 =$ product of numbers	
	$147200 = \text{product of numbers} \tag{1}$	
4	(i) HCF of 28,16 and 12 is 4	$\sim 1 \sim 1 \sim 10^{-10}$
	Therefore maximum number of books each student (ii) Number of mathe books $28/4 - 7$	get is 4 (2)
	(ii) Number of maths books $28/4 = 7$ Number of science books $16/4 = 4$	
	Number of social science $= 12/4 = 3$	
	Total books = $7 + 4 + 3 = 14$ (2)	
5	(i) LCM of 2,3 and 5 = 30	



	Thus 31 marbles are there in the bag (2)
	(ii) If we add 1 in multiple of 30 we will get another possible number of
	marble. These are $61,91,121,$ (2)
6	(i) HCF of all length
	HCF(6,12,24,36,48) = 6
	(ii) HCF of all width
	HCF(8,24,36,48,96) = 4
	Thus maximum size of sheet is 6 by 4
7	(i) HCF of 825 and 625
	$825 = 3 \times 5 \times 5 \times 11$
	$675 = 3 \times 3 \times 3 \times 5 \times 5$
	$HCF = 3 \times 5 \times 5 = 75$ (2)
	Maximum capacity reqired is 75 litres
	(ii) The first tanker will require $875/75 = 11$ times to fill
0	The second tanker will require $675/75 = 9$ times to fill (2)
8	(i)Amar reaches 96 stairs
	Akbar reaches 95 stairs
	Anthony reaches 91 stairs
	Thus Amar will reach nearest point (2)
	(ii)Amar will take $100/3 = 33.3$
	Akbar will take $100/5 = 20$
	Anthony will take $100/7 = 14.22$
	Anthony will take least step (2)
9	(i)HCF of(15,40) =5
	Fruits will be distributed equally among 5 guests (2)
	(ii)Out of 15 apples each guest will get $15/5 = 3$ apples
	Out of 40 banana each guest will get $40/5 = 8$ bananas (2)
10	(i) 539 chairs (2)
	(ii) if 1 chair is added as 539 is already divisible by 11,1 chair will be left (2)



UNIT 2- ALGEBRA

POLYNOMIALS

IMPORTANT CONCEPTS

A polynomial is an algebraic expression in which the exponent on any variable is a wholenumber. / A polynomial is an algebraic expression with variables having positive integralpowers only.

General Form:

$a_n x^n + a_{n-1} x^{n-1} + ... + a_2 x^2 + a_1 x + a_0$

L Degree of a polynomial

• The highest power of x in p(x) is called the degree of the polynomial p(x).

Name of the polynomial	Degree of the polynomial	Example
Zero polynomial	Not defined	0,5,-3
Linear polynomial	1	x-3
Quadratic polynomial	2	6x²-3y
Cubic polynomial	3	4x ³ +5y ² -1

♦ Value of a polynomial:

If p(x) is a polynomial in x, and if k is any real number, then the value obtained by replacing x by k in p(x), is called the value of p(x) at x = k, and is denoted by p(k).

Q. Find the value of the polynomial $p(x) = x^2 + 4x + 4$ where x = 2. Given polynomial: $p(x) = x^2 + 4x + 4$. Value of given polynomial when x = 2 and we get: $p(2) = (2)^2 + 4(2) + 4$ = 4 + 8 + 4 = 16Hence the value of $p(x) = x^2 + 4x + 4$, where x = 2, is 16



Zero of a polynomial

A real number k is said to be a zero of a polynomial p(x), if p(k) = 0

What is the value of $p(x) = x^2 - 3x - 4$ at x = -1? We have : $p(-1) = (-1) 2 - \{3 \times (-1)\} - 4 = 0$ Also, note that $p(4) = 4^2 - (3 \times 4) - 4 = 0$. As p(-1) = 0 and p(4) = 0, -1 and 4 are called the zeroes of the quadratic polynomial $x^2 - 3x - 4$.

RELATIONSHIP BETWEEN ZEROES & COEFFICIENTS OF POLYNOMIALS

Type of Polynomial	General form	No. of zeroes	Relationship between zeroes and coefficients
Linear	$ax + b, a \neq 0$	1	$k = -\frac{b}{a}$, <i>i.e.</i> $k = -\frac{\text{Constant term}}{\text{Coefficient of x}}$
Quadratic	$ax^2 + bx + c, a \neq 0$	2	Sum of zeroes $(\alpha + \beta) = -\frac{\text{Coefficient of } x}{\text{Coefficient of } x^2} = -\frac{b}{a}$ Product of zeroes $(\alpha\beta) = \frac{\text{Constant term}}{\text{Coefficient of } x^2} = \frac{c}{a}$
Cubic	$ax^3 + bx^2 + cx + d,$ a \ne 0	3	Sum of zeroes $(\alpha + \beta + \gamma) = -\frac{\text{Coefficient of } x^2}{\text{Coefficient of } x^3} = -\frac{b}{a}$ Product of sum of zeroes taken two at a time $(\alpha\beta + \beta\gamma + \gamma\alpha) = \frac{\text{Coefficient of } x}{\text{Coefficient of } x^3} = \frac{c}{a}$ Product of zeroes $(\alpha\beta\gamma) = -\frac{\text{Constant term}}{\text{Coefficient of } x^3} = -\frac{d}{a}$

MULTIPLE CHOICE QUESTIONS

SECTION A

Q1. If one zero of the quadratic polynomial $x^2 + 3x + k$ is 2, then the value of k is

a) 10 b) -10 c) 5 d) -5

Q2. A quadratic polynomial, the sum of whose zeros is 2 and one zero is 3 is

a) x2-9 b) x2+9 c) x2+3 d) x2-3

Q3. A quadratic polynomial, the sum of whose zeros is -5 and their product is 6 is

a) $x^2 + 5x + 6$ b) $x^2 + 5x + 6$ c) $x^2 - 5x + 6$ d) $-x^2 + 5x + 6$

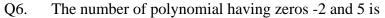
Q4. If one zero of the polynomial $f(x) = (k^2 + 4)x^2 + 13x + 4k$ is the reciprocal of the other, then k =

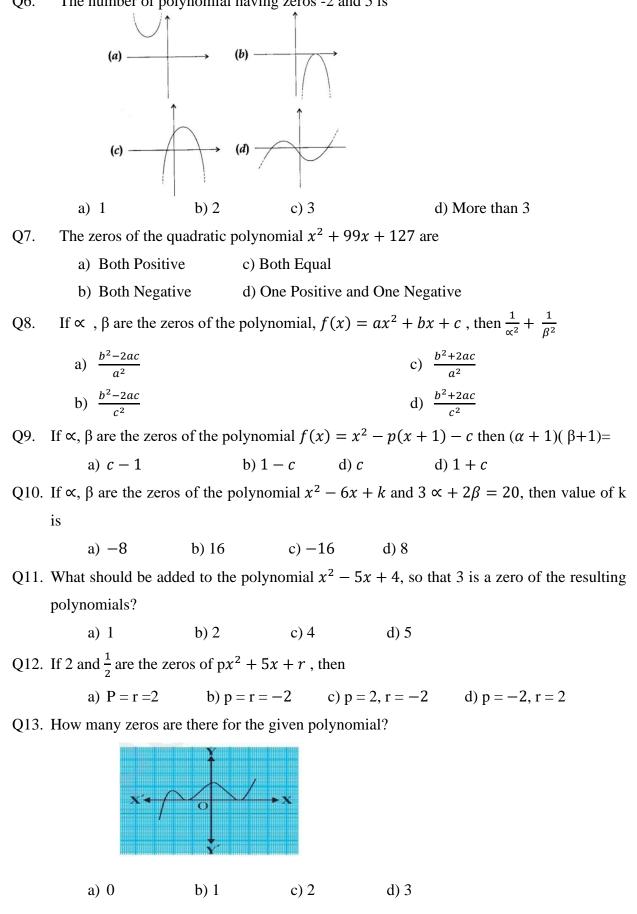
a) 2 b) -2 c) 1 d) -1

Q5. If \propto , β are the zeros of the polynomial $f(x) = x^2 + x + 1$, then $\frac{1}{\alpha} + \frac{1}{\beta} =$

a) 1 b) -1 c) 0 d) None of these









Q14. Which of the following is not the graph of a quadratic polynomial?

(a) 1 b) 2 (c) 3 (d) 3 or more

OBJECTIVE TYPE QUESTIONS (I MARK QUESTIONS)

- Q1. Write the zeros of the polynomial $x^2 x 6$
- Q2. Write a polynomial whose zeros are $(2+\sqrt{3})$ and $(2-\sqrt{3})$
- Q3. If α , β are the zeros of the polynomial, such that $\alpha+\beta=6$ and $\alpha\beta=4$, then write the polynomial.
- Q4. If α and $\frac{1}{\alpha}$ are the zeros of the polynomial $4x^2 2x + (k 4)$, find the value of k.
- Q5. Check whether -2 is a zero of the polynomial $9x^3 18x^2 x 2$
- Q6. Find the zeros of the polynomial $4\sqrt{3}x^2 + 5x 2\sqrt{3}$
- Q7. For what value of k is 3 a zero of the polynomial $2x^2 x + k$?
- Q8. Find a quadratic polynomial with the given numbers are the sum and product of its zeros respectively. $\frac{-1}{4}, \frac{1}{4}$
- Q9. If α , β are the zeros of the polynomial $6y^2 7y + 2$, find a quadratic polynomial whose zeros are $\frac{1}{\alpha}$, $\frac{1}{\beta}$
- Q10. If the sum and product of the zeros of the polynomial $ax^2 6x + c$ is equal to 12 each, find the value of *a* and *c* each.

SHORT ANSWER TYPE QUESTIONS (2 MARKS QUESTIONS) SECTION - B

- Q1. Find the zeroes of the polynomial $2x^2 9$ and verify the relationship between zeros and coefficients.
- Q2. Find a quadratic polynomial the sum and product of whose zeros are 3 and -2/5 respectively.
- Q3. If α and β are zeros of $3x^2 + 5x + 13$, then find the value of $\frac{1}{\alpha} + \frac{1}{\beta}$.
- Q4. Check whether x = -3 is a zero of $x^3 + 11x^2 + 23x 35$.
- Q5. Find p and q if p and q are the zeros of the quadratic polynomial $x^2 + px + q$.
- Q6. If 2 is a zero of $2x^2 + px + 5$, then find the value of *p*.
- Q7. Prove that both zeroes of $x^2 + 99x + 127$ are negative.
- Q8. Find the quadratic polynomial sum of whose zeros is 8 and their product is 12.Hence find the zeroes of the polynomial.
- Q9. For what value of k, -4 is a zero of $x^2 x (2k + 2)$?



- Q10. Find the value of a in the polynomial $2a^2 + 2xa + 5a + 10$ if (x + a) is one of its factors.
- Q11. Show that $x^2 + 4x + 7$ has no zeros.
- Q12. Form a quadratic polynomial one of whose zeros is $2 + \sqrt{5}$ and the sum of zeros is 4.
- Q13. If the zeros of $x^2 kx + 6$ are in the ratio 3:2, find k.
- Q14. If the zeros of the polynomial $x^2 + px + q$ are double in value to the zeros of $2x^2 5x 3$, find p and q.
- Q15. The sum and product of the zeros of $4x^2 27x + 3k^2$ are equal, find the values of k.
- Q16. If α and β are the zeros of the polynomial $p(x) = x^2 + 5x + q$ such that $\alpha \beta = 1$. Find k.
- Q17. If the sum of zeros of th quadratic polynomial $f(t) = kt^2+2t+3k$ is equal to their product, find k.
- Q18. If (x+1) is a factor of $x^2 3ax + 3a 13$, find k.
- Q19. If zeros of the polynomial $x^2 4x + 2p$ are a and 2/a, then find the value of a.
- Q20. If one of the zeros of the quadratic polynomial $f(x) = 14x^2 42k^2x 9$ is negative of the other, find k.

SHORT ANSWER TYPE QUESTIONS (3 MARKS QUESTIONS)

SECTION - C

- Q1. Find the zeroes of the following polynomial by factorisation method and verify the relations between the zeroes and their coefficients
 - i) $7y^2 \frac{11}{3}y \frac{2}{3}$ ii) $\sqrt{3}x^2 + 10x + 7\sqrt{3}$ iii) $4\sqrt{3}x^2 + 5x - 2\sqrt{3}$
- Q2. If the sum of the zeroes of the polynomial $p(x) = (a + 1)x^2 + (2a + 3)x + (3a + 4)$ is -1, then find the product of the zeroes.
- Q3. If (x + a) is a factor of two polynomials $x^2 + px + q$ and $x^2 + mx + n$, then prove that $a = \frac{n-p}{m-P}$
- Q4. Can the quadratic polynomial $x^2 + kx + k$ have equal zeroes for some odd integer k > 1?
- Q5. If one zero of a polynomial $3x^2 8x + 2k + 1$ is seven times the other, find the value of k.



- Q6. If p and q are the zeroes of the polynomial $6y^2 7y + 2$, find a quadratic polynomial whose zeroes are 1/p and 1/q.
- Q7. If α and β are zeroes of the quadratic polynomial $x^2 (k + 6)x + 2(2k 1)$. Find the value of k if $\alpha + \beta = \frac{1}{2} \alpha \beta$.
- Q8. If m and n are zeroes of $ax^2 5x + c$, find the values of a and c if m + n = mn = 10
- Q9. Find the value of k in order that one zero of $3x^2 + (1 + 4k)x + k^2 + 5$ may be one third of the other.
- Q10. The zeroes of $x^2 kx + 6$ are in the ratio 3:2, find k.
- Q11. Find the zeros of the quadratic polynomial $(5u^2 + 10u)$ and verify the relation between the zeros and the coefficients.
- Q12. Find zeroes of the Polynomial $p(x) = 4x^2 + 5\sqrt{2x} 3$ & verify relationship between the zeroes and the co-efficient of the polynomials.
- Q13. Find the zeroes of the following quadratic polynomials $6x^2 3 7x$ and verify the relationship between the zeros and the coefficients.
- Q14. If α , β are zero of quadratic polynomial kx² + 4x + 4, find the values of k such that (α + β)² 2 $\alpha\beta$ = 24
- Q15. If sum of the squares of the zeroes of the quadratic polynomial $f(x) = x^2 8x + k$ is 40, find the value of k.

LONG ANSWER TYPE QUESTIONS (4 MARK QUESTIONS)

SECTION - D

- Q1. If α and β are the zeroes of the quadratic polynomial $p(s) = 3s^2 6s + 4$, find the value of $\frac{\alpha}{\beta} + \frac{\beta}{\alpha} + 2(\frac{1}{\alpha} + \frac{1}{\beta}) + 3\alpha\beta$
- Q2. If the squared difference of the zeroes of the quadratic polynomial $f(x)=x^2 + px + 45$ is equal to 144, find the value of p.
- Q3. If α and β are the roots of the equation $ax^2+bx+c=0$ and if $px^2+qx+r=0$ has roots $\frac{1-\alpha}{\alpha}$ and

$$\frac{1-\beta}{\beta}$$
, then r is

Q4. If a and b are the zeroes of the quadratic polynomial $f(x)=x^2-px+q$, prove that

$$\frac{a^2}{b^2} + \frac{b^2}{a^2} = \frac{p^4}{q^2} - \frac{4p^2}{q} + 2.$$

Q5. If 1 and m are zeroes of the polynomial $p(x)=2x^2-5x+7$, find a polynomial whose zeroes are 21+3 and 2m+3.

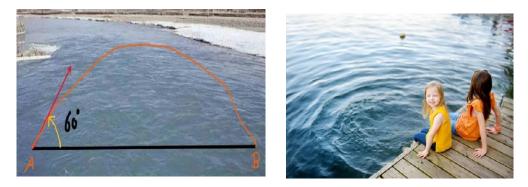


- Q6. Find a quadratic polynomial whose zeroes are reciprocals of the zeroes of the polynomial $f(x) = ax^2 + bx + c$, $a \neq 0$, $c \neq 0$.
- Q7. If the polynomial $16a^4 + 8a^2 15$ have real zeroes, find them.
- Q8. If one zero of the polynomial $p(x) = 2x^2 4kx + 6x 7$ is the negative of other find the zeros of $x^2 kx 1$.

CASE STUDY BASED QUESTIONS

Q9. CASE STUDY 1

Two Friends Geeta and Sita were playing near the river. So, they decide to play a game in which they have to throw the stone in the river, and whoever will throw the stone at maximum distance, win the game.



Geeta Starts first and throws the stone in the river. During her throw, her hand was making an angle of 60° with the Horizontal plane. Sita throws at 45° .

- (a) The shape of trajectory formed by stone when Geeta & Sita throw it in the river, is:
 - i. Straight Line

- iii. Parabola
- iv. Semi circle
- (b) If we make a mathematical equation of the path followed by stone when Geeta & Sita threw it in the river, then the resulting mathematical equation would be:
 - i. Linear

ii. Circle

iii. Quadratic

ii. Cubic

- iv. Bi-Quadratic
- (c) Let there be a Polynomial $y=2x^2-3x+1$, then the curve formed by this Polynomial would be:
 - i. Parabola Open Upward
 - ii. Parabola Open Downward

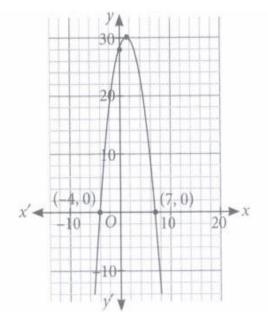
- iii. Hyperbola Open Upwardiv. Hyperbola Open downward
- (d) There is a Polynomial $y=x^2+x+1$. It will intersect the x-axis at:
 - i. Two Real Points
 - ii. One Real Point
 - iii. Three Real Points
- (e) It will not intersect the x-axis.y-intercept of Polynomial can be found by
 - i. Putting y=0 in given Polynomial
 - ii. Putting y=1 in the given Polynomial
 - iii. Putting x=0 in the given Polynomial.
 - iv. Putting x=1 in the given Polynomial.

Q10. CASE STUDY 2



Two friends Trisha and Rohan during their summer vacations went to Manali. They decided to go for trekking. While trekking they observes that the trekking path is in the shape of a parabola. The mathematical representation of the track is shown in the graph.





information answer the following questions

Based on the above information, answer the following questions.

a)	The ze	croes of the polynomial whose graph is given	n, are	
	i.	4, 7	iii.	4,3
	ii.	-4, 7	iv.	7,10
b)	What	will be the expression of the given polynomia	ial p (x)
	i.	$x^2 - 3x + 38$		
	ii.	$-x^2 + 4x + 28$		
	iii.	$x^2 - 4x + 28$		
	iv.	$-x^2 + 3x + 28$		
c)	The pr	oduct of zeroes of the given polynomial is		
	i.	-28	iii.	-30
	ii.	28	iv.	30
d)	If $f(x$	$= x^2 - 13x + 1$, then f(4) =		
	i.	35	iii.	36
	ii.	-35	iv.	-36
FD	KEV			

ANSWER KEY

MCQ (1 MARK)		
Q NO	ANSWER	
1	(b) Since 2 is zero P(2)=0 P(2) = $2^2 + 3x^2 + k = 0$ which gives $k = -10$	
2	(a) Given $\alpha + \beta = 0$ $\alpha = 3 \ so \ \beta = -3$	
	$p(x) = k(x^2 - (\alpha + \beta)x + \alpha\beta)$	
	$p(x) = k(x^2 - 9)$	
3	(a)	
	$P(x) = k(x^2 - (-5x) + 6)$	
	$P(x) = k(x^2 + 5x + 6)$	



	when $k = 1$ $p(x) = x^2 + 5x + 6$
4	(a) Let the zeros be α , $\frac{1}{\alpha}$
	So $\alpha X \frac{1}{\alpha} = 1 = \frac{4k}{k^2 + 4}$
	cross multiplying we get $k^2 - 4k + 4 = 0 \implies (k-2)^2 = 0$ which
	gives $k = 2$
5	(b) $\frac{1}{\alpha} + \frac{1}{\beta} = \frac{\alpha + \beta}{\alpha \beta} = \frac{-1}{1} = -1 \{\alpha + \beta = -1 \text{ and } \alpha \beta = 1\}$
6	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
U	$P(x) = k(x^{2} - (-2 + 5)x + -2X5) = k(x^{2} = 3x - 10)$
	Since k can take infinite number of values, there can be more than three
7	polynomials.
7	(b) Since the sum and product are both positive, the numbers will be both positive. So the zeros will be both negative.
8	(b)
	$\frac{1}{\alpha^2} + \frac{1}{\beta^2} = \frac{\alpha^2 + \beta^2}{(\alpha\beta)^2}$
	$\alpha^{2} + \beta^{2} = (\alpha + \beta)^{2} - 2\alpha\beta = (\frac{-b}{2})^{2} - 2X\frac{c}{2} = \frac{b^{2} - 2ac}{2}$
	$\alpha^{2} + \beta^{2}$ $b^{2} - 2ac$ c $b^{2} - 2ac$ a^{2} $b^{2} - 2ac$
	$\alpha^{2} + \beta^{2} = (\alpha + \beta)^{2} - 2\alpha\beta = (\frac{-b}{a})^{2} - 2X\frac{c}{a} = \frac{b^{2} - 2ac}{a^{2}}$ $\frac{\alpha^{2} + \beta^{2}}{(\alpha\beta)^{2}} = \frac{b^{2} - 2ac}{a^{2}} \div (\frac{c}{a})^{2} = \frac{b^{2} - 2ac}{a^{2}}X\frac{a^{2}}{c^{2}} = \frac{b^{2} - 2ac}{c^{2}}$
9	(b)
	$P(x) = x^{2} - p(x+1) - c = x^{2} - px - (p+c)$
	$\{a = 1 \ b = -p, \ c = -(p+c)\}\$ (\alpha + 1)(\beta + 1) = \alpha\beta + (\alpha + \beta) + 1
	(a + 1)(p + 1) = ap + (a + p) + 1 = $\frac{c}{c} + \frac{-b}{-b} + 1$
	a a
10	$=\frac{-(p+c)}{1} + \frac{-(-p)}{1} + 1 = 1 - c$
10	(c) $P(x) = x^2 - 6x + k$ $a = 1$, $b = -6$, $c = k$
	$\alpha + \beta = \frac{-(-6)}{1} = 6 \dots \dots$
	Given $3\alpha + 2\beta = 20 \dots \dots \dots \dots \dots \dots (2)$ $\alpha \beta = \frac{1}{a} - \frac{1}{1} - \kappa$
	Multiplying equation (1) by 3 and subtracting from (2) we get $\beta = -2$.
	Substituting this in equation (1) get $\alpha = 8$ So $k = \alpha\beta = -2X8 = -16$
11	(b) $P(x) = x^2 - 5x + 4$ $P(x) + 2 = x^2 - 5x + 4 + 2 = x^2 - 5x + 6 =$
11	$ \begin{array}{c} (0) & I(x) = x \\ (x-3)(x-2) \end{array} $
	So the zeros are 3, 2
10	1 -5 r
12	(b) Given $\alpha = 2$ and $\beta = \frac{1}{2}$ $\alpha + \beta = \frac{-5}{p}$ and $\alpha\beta = \frac{r}{p}$
	$\alpha + \beta = 2 + \frac{1}{2} = \frac{5}{2} = \frac{-5}{p}$ Cross multiplying, we get $p = -2$
13	$\alpha\beta = \frac{r}{p} = 1$ Cross multiplying, we get $r = p = -2$ (d) Since the graph touched the X-axis at three different points, the polynomial
	will have three zeros.
14	(c) A quadratic polynomial will have at the most 2 zeros. The third polynomial
	has 3 zeros. So it is not a quadratic polynomial.



	OBJECTIVE QUESTIONS (1 MARK)		
Q NO	ANSWER		
1	$x^{2} - x - 6 = (x - 3)(x + 2)$ so the zeros are 3 and -2		
2	Polynomial = $K(x^2 - (\alpha + \beta)x + \alpha\beta)$		
	$= K(x^{2} - (2 + \sqrt{3} + 2 - \sqrt{3})x + (2 + \sqrt{3})(2 - \sqrt{3}))$		
	$=K\left(x^{2}-(4)x+2^{2}-(\sqrt{3})^{2}\right)=K\left(x^{2}-4x+(4-3)\right)$		
	$=K(x^2-4x+1)$		
3	$\frac{-K(x - 4x + 1)}{P(x) = K(x^2 - (\alpha + \beta)x + \alpha\beta)} = K(x^2 - 6x + 4)$		
4	Given $\alpha, \frac{1}{\alpha}$ are the zeros of the polynomial. Product of the zeros $=\frac{c}{a}=\frac{k-4}{4}$		
	$\alpha X \frac{1}{\alpha} = \frac{k-4}{4}$		
	$\alpha \qquad 4_{k-4}$		
	$1 = \frac{k-4}{4}$		
5	Cross multiplying we get k = 8 $f(x) = 9x^3 - 18x^2 - x - 2$ If -2 is a zero then $f(-2) = 0$		
5	$f(-2) = 9X(-2)^3 + 18X(-2)^2 - (-2) - 2$		
	= 9X(-8) + 18X(4) + 2 - 2		
	= -72 + 72 + 2 - 2 = 0		
6	Since $f(-2) = 0$ -2 is a zero of the given polynomial.		
0	. $P(x) = 4\sqrt{3}x^2 + 5x - 2\sqrt{3}$ Sum= 5 and product $= 4\sqrt{3}X - 2\sqrt{3} = -8X3 = -24$		
	Sum= 5 and product = $4\sqrt{5}x - 2\sqrt{5} = -8x5 = -24$ The numbers are -3 and $+8$		
	By splitting the middle term, we get		
	$P(x) = 4\sqrt{3}x^2 + 8x - 3x - 2\sqrt{3}$		
	$= 4x(\sqrt{3}x+2) - \sqrt{3}(\sqrt{3}x+2) = (\sqrt{3}x+2)(4x-\sqrt{3})$		
	The zeros are $\frac{-2}{\sqrt{3}}$ and $\frac{\sqrt{3}}{4}$		
7	$P(x) = 2x^2 + x + k$ Given 3 is a zero so $P(3) = 0$		
	$P(3) = 2 X (3)^{2} + 3 + k = 0$ 2 X 9 + 3 + k = 0		
8	$21 + k = 0 \text{which gives} k = -21$ $\frac{-1}{4}, \ \frac{1}{4}P(x) = k(x^2 - \left(\frac{-1}{4} + \frac{1}{4}\right)x + \frac{-1}{4}X\frac{1}{4})$		
	$= k \left(x^{2} - 0x - \frac{1}{16} \right) = k \left(x^{2} - \frac{1}{16} \right)$		
9	If $k = 16$ $P(x) = 16x^2 - 1$ Given $P(y) = 6y^2 - 7y + 2$ here $\alpha + \beta = \frac{7}{6}$ and $\alpha\beta = \frac{2}{6}$		
	The given zeros are $\frac{1}{\alpha}$ and $\frac{1}{\beta}$ sum of zeros $= \frac{1}{\alpha} + \frac{1}{\beta} = \frac{\alpha + \beta}{\alpha \beta} = \frac{7}{2}$		
	Product of zeros $=\frac{1}{\alpha} X \frac{1}{\beta} = \frac{1}{\alpha\beta} = \frac{1}{\frac{2}{6}} = \frac{6}{2}$		
	The new polynomial is $P(y) = k(y^2 - (sum)y + product)$		
	$P(y) = k(y^2 - (\frac{\gamma}{2})y + \frac{6}{2})$		
10	When k = 2 $P(y) = 2y^2 - 7y + 6$ $P(x) = ax^2 - 6x + c$		
10	$P(x) = ax^{2} - 6x + c$ given $\alpha + \beta = 12$		
	$\frac{6}{a} = 12 \text{ which gives } a = \frac{6}{12} = \frac{1}{2}$		
	$\frac{-12}{a}$		



		0	C		
	$\alpha \beta = 12$ which give	$rs \frac{c}{a} = 1$	$2 = \frac{c}{\frac{1}{2}} = 12$		
	which gives $c = 12$	$\times \frac{1}{2} = 6$	2		
	SHORT ANS	WER TY	PE QUESTIONS (2	MARKS))
Q NO	ANSWER			,	
1	$\pm \frac{3}{\sqrt{2}}$				
2	$x^2 - 15x - 2$				
3	5				
4	$\frac{1}{13}$ x = -3 is not a zero				
5					
6	p = 1; q = -2 . $a = -\frac{13}{2}$				
7	4	mularia	$x_{-1} = 12$ 077		
8	Applying quadratic for $x^2 - 8x + 12$; zero				
8 9	k=9 10. $a = -2$	<i>is alt</i> 0,2	<u>ل</u>		
10	a = -2				
11	we cannot find two nu	mbers a	and b with sum 4 and	product 7.	So polynomial
	has no zeros			•	1 0
12	one zero is $2 + \sqrt{5}$ sum is 4, other root is $2 - \sqrt{5}$;				
	Quadratic polynomial is $x^2 - 4x - 1$				
13	±5				
14	p = 5, q = -6				
15	$k = \pm \frac{3}{2}$				
16	k=6				
17	k=-2/3				
18	a=2				
19	a=1				
20	$\frac{K=0}{\text{SHORT AN}}$	SWFD	TYPE QUESTIONS(3 MADE	S)
Q NO	ANSWER	Q NO	ANSWER	Q NO	ANSWER
1	i) $y = \frac{14}{21}, -\frac{1}{7}$	6	$\frac{1}{2}(2y^2 - 7y + 6)$	11	u = -2, 0
			2 2 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7		
	ii) $x = -\sqrt{3}, -\frac{7}{\sqrt{3}}$				
	iii) $x = -\frac{2}{\sqrt{3}}, \frac{3}{4\sqrt{3}/2}$				
2	Product = -2	7	k = 7	12	$X = \frac{1}{2\sqrt{2}}, -\frac{3}{\sqrt{2}}$ $X = \frac{3}{2}, \frac{-1}{3}$
3	Correct proof	8	$a = \frac{1}{2}$ and $c = 5$	13	$x = \frac{3}{2}, \frac{-1}{3}$
4	The quadratic	9	$k = \frac{79}{8}$	14	$k = -1, \frac{2}{3}$
	polynomial cannot		δ		3
	have equal zeros				
	for any odd integer $k > 1$				
L	N / 1	1	1	1	

5 $k = -\frac{1}{9}$ 10 $k = \pm 5$ $k = 12$ LONG ANSWER TYPE QUESTIONS(4 MARKS)Q NOANSWER1Sum of zeroes = $\alpha + \beta$ $= \frac{-b}{a}$ $= -(\frac{-6}{3})$ $= 2$ (i)Product of zeroes = $\alpha\beta$ $= \frac{c}{a}$ $= \frac{4}{3}$ $=$	
$\begin{array}{c cccc} \hline \mathbf{Q} \ \mathbf{NO} & \mathbf{ANSWER} \\ \hline 1 & \text{Sum of zeroes} = \alpha + \beta & = \frac{-b}{a} = -\left(\frac{-6}{3}\right) = 2 & \dots \\ & \text{Product of zeroes} = \alpha\beta & = \frac{c}{a} & = \frac{4}{3} & -\dots \\ & \text{Product of zeroes} = \alpha\beta & = \frac{c}{a} & = \frac{4}{3} & -\dots \\ & \text{Now, } \frac{\alpha}{\beta} + \frac{\beta}{\alpha} + 2\left(\frac{1}{\alpha} + \frac{1}{\beta}\right) + 3\alpha\beta & = \frac{\alpha^2 + \beta^2}{\alpha\beta} + 2\left(\frac{\alpha + \beta}{\alpha\beta}\right) + 3\alpha\beta \\ & = \frac{(\alpha + \beta)^2 - 2\alpha\beta}{\alpha\beta} + 2\left(\frac{\alpha + \beta}{\alpha\beta}\right) \\ & = \frac{(\alpha + \beta)^2 - 2\alpha\beta}{\alpha\beta} + 2\left(\frac{2}{3}\right) + 3\left(\frac{4}{3}\right) \\ & = \frac{1 + 3 + 4}{\alpha\beta} = \frac{-b}{\alpha\beta} \\ & = \frac{(\alpha + \beta)^2 - 2\alpha\beta}{\frac{4}{3}} + 2\left(\frac{2}{3}\right) + 3\left(\frac{4}{3}\right) \\ & = 1 + 3 + 4 = 8 \end{array}$ 2 $\begin{array}{c} f(\mathbf{x}) = \mathbf{x}^2 + \mathbf{p}\mathbf{x} + 45 \\ \text{Sum of zeroes} = \alpha + \beta & = \frac{-b}{\alpha} = -\mathbf{p} (\mathbf{i}) \\ \text{Product of zeroes} = \alpha\beta & = \frac{c}{a} & = 45 \dots (\mathbf{i}\mathbf{i}) \\ \text{Given } (\alpha - \beta)^2 = 144 \\ (\alpha + \beta)^2 - 4\alpha\beta & = 144 \\ (\alpha + \beta)^2 - 4\alpha\beta & = 144 \\ P^2 = 144 + 180 & = 3 \\ P = \sqrt{3}24 = 18 \end{array}$ 3 $\begin{array}{c} \text{Since } \alpha \text{ and } \beta \text{ are the roots of the equation } \mathbf{a}\mathbf{x}^2 + \mathbf{b}\mathbf{x} + \mathbf{c} = 0, \text{ so,} \\ \alpha + \beta = \frac{-b}{a}, \alpha\beta = \frac{c}{a} \end{array}$	
1 Sum of zeroes = $a+\beta = \frac{-b}{a} = -(\frac{-6}{3}) = 2$ (i) Product of zeroes = $a\beta = \frac{c}{a} = \frac{4}{3}$ (ii) Now, $\frac{\alpha}{\beta} + \frac{\beta}{\alpha} + 2(\frac{1}{\alpha} + \frac{1}{\beta}) + 3 \alpha\beta = \frac{\alpha^2 + \beta^2}{\alpha\beta} + 2(\frac{\alpha + \beta}{\alpha\beta}) + 3 \alpha\beta$ $= \frac{(\alpha + \beta)^2 - 2\alpha\beta}{\alpha\beta} + 2(\frac{\alpha + \beta}{\alpha\beta})$ $= \frac{(2)^2 - 2(\frac{4}{3})}{\frac{4}{3}} + 2(\frac{2}{\frac{4}{3}}) + 3(\frac{4}{3})$ = 1 + 3 + 4 = 8 2 $f(x) = x^2 + px + 45$ Sum of zeroes = $\alpha + \beta = \frac{-b}{a} = -p$ (i) Product of zeroes = $\alpha\beta = \frac{c}{a}^2 = 45(ii)$ Given $(\alpha - \beta)^2 = 144$ $(\alpha + \beta)^2 - 4\alpha\beta = 144$ $(-p)^2 - 4(45) = 14$ $P^2 = 144 + 180 = 3$ $P = \sqrt{324} = 18$ 3 Since a and β are the roots of the equation $ax^2 + bx + c = 0$, so, $\alpha + \beta = \frac{-b}{a}, \alpha\beta = \frac{c}{a}$	
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a a	
The equation with roots $\frac{1-\alpha}{\alpha}$ and $\frac{1-\beta}{\beta}$ can be written as	
$x^{2} - \left\{\frac{1-\alpha}{\alpha} + \frac{1-\beta}{\beta}\right\} x + \left\{\frac{1-\alpha}{\alpha} * \frac{1-\beta}{\beta}\right\} = 0 \dots 1$	
Now, sum of zeroes, $\left\{\frac{1-\alpha}{\alpha} + \frac{1-\beta}{\beta}\right\} = \frac{\alpha+\beta-2\alpha\beta}{\alpha\beta}$	
$= \frac{\alpha + \beta}{\alpha \beta} + \frac{-2 \alpha \beta}{\alpha \beta} = \frac{\alpha + \beta}{\alpha \beta} - 2, \qquad \dots $	
$=\frac{-b}{c}-2=\frac{-b-2c}{c}$, since $a+\beta=\frac{-b}{a}$, $a\beta=\frac{c}{a}$	
Product of zeroes	
$\frac{1-\alpha}{\alpha} * \frac{1-\beta}{\beta} = \frac{1-(\alpha+\beta)+\alpha\beta}{\alpha\beta} = \frac{1-\frac{-b}{\alpha}+\frac{c}{\alpha}}{\frac{c}{\alpha}} = \frac{a+b+c}{c} \dots 3$	
Putting 2 and 3 in 1	
The required equation is $x^2 - \left\{\frac{-b-2c}{c}\right\}x + \frac{a+b+c}{c} = 0$	
$cx^{2} + (b + 2c) x + (a + b + c) = 0 - (i)$	
On comparing equation (i) with the equation given $px^2 + qx + r = 0$, $r = a + b + c$.	
4 Sum of zeroes = $a+b=p$	

SHE.



	Product of zeroes $= ab = q$
	$\frac{a^2}{b^2} + \frac{b^2}{a^2} = \frac{a^4 + b^4}{a^2b^2} = \frac{(a^2 + b^2)^2 - 2a^2b^2}{a^2b^2}$
	$=\frac{[(a+b)^2-2ab]^2-2a^2b^2}{a^2b^2} = \frac{[p^2-2q]^2-2q^2}{a^2}$
	$= \frac{p^4 - 4p^2q + 4q^2 - 2q^2}{q^2} = \frac{p^4 - 4p^2q + 2q^2}{q^2}$
	$= \frac{p^{4}}{q^{2}} - \frac{-4p^{2}q}{q^{2}} + \frac{2q^{2}}{q^{2}}$ $= \frac{p^{4}}{q^{2}} - \frac{-4p^{2}q}{q^{2}} + 2$
5	$l + m = \frac{5}{2}$
	$lm=\frac{7}{2}$
	a polynomial whose zeroes are $2l + 3$ and $2m + 3$ is
	$x^{2} - (2l + 3 + 2m + 3)x + (2l + 3)(2m + 3)$ = $x^{2} - [2(l + m) + 6)]x + (4lm + 6(l + m) + 9)$
	$= x^{2} - 5x + 6x + 14 + 15 + 9$
	$= x^2 + x + 38$
6	Let α and β be the zeroes of the polynomial $f(x) = ax^2 + bx + c$.
	So, $\alpha + \beta = -b/a$
	lphaeta=c/a
	According to the given, $\frac{1}{\alpha}$ and $\frac{1}{\beta}$ are the zeroes of the required quadratic polynomial.
	Now, the sum of zeroes = $(1/\alpha) + (1/\beta)$
	$= (\alpha + \beta)/\alpha\beta$ $= (-b/a)/(c/a) = -b/c$
	Product of two zeroes = $(1/\alpha)(1/\beta) = 1/\alpha\beta = 1/(c/a) = a/c$
	The required quadratic polynomial = $k[x^2 - (sum of zeroes)x + (product of zeroes)]$
	$= k[x^2 - (-b/c)x + (a/c)]$
	$= k[x^{2} + (b/c) + (a/c)]$
7	The polynomial $16a^4 + 8a^2 - 15 = (4a^2)^2 + 2(4a^2) - 15$
	$Put 4a^2 = x$
	$x^2 + 2x - 15 = 0$
	$x^2 + 5x - 3x - 15 = 0$
	x(x+5) - 3(x+5) = 0
	(x+5)(x-3) = 0
	x = -5, x = 3
	If $x = -5$, $a = \sqrt{-5/2}$
	$\Pi \Lambda = 3, u + 5/2$



	If $x = 3$, $a = \frac{\sqrt{3}}{2}$				
8	$p(x) = 2x^2 - 4kx + 6x - 7$				
	let the zeroes be a, -a sum of zeroes $= a + -a = 0$				
	$2x^2 - 4kx + 6x - 7 = 2x^2 - x(4k - 6) - 7$ Sum of zeroes = $(4k-6)/2 = 2k-3$				
	But $2k-3 = 0$				
	K = 3/2				
	Now, $x^2 - kx - 1 = x^2 - \frac{3}{2}x - 1 = 2x^2$	-3x - 2			
	CASE STUDY BASED QUESTIONS				
9 CAS	9 CASE STUDY 1		CASE STUDY 2		
Q NO	ANSWER	Q NO	ANSWER		
А	(i) parabola	a	(b) -4,7		
В	(ii) Quadratic	b	$(d) - x^2 + 3x + 28$		
С	(iii) parabola open upward	с	-28		
D	It will not intersect the x- axis	d	-35		
Е	Putting $x = 0$, in the given polynomial				



LINEAR EQUATIONS IN TWO VARIABLES

An equation which can be put in the form ax + by + c = 0, where *a*, *b* and *c* are real numbers, and *a* and *b* are not both zero ($a^2 + b^2 \neq 0$), is called a linear equation in two variables *x* and *y*.

Each solution (*x*, *y*) of a linear equation in two variables, ax + by + c = 0, corresponds to a point on the line representing the equation, and vice versa.

The general form of a pair of linear equations is

 $a_1x + b_1y + c_1 = 0$

 $a_2x + b_2y + c_2 = 0$

Ratio comparison Graphical Algebraic Consistent/ representation interpretation Inconsistent $\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$ Intersecting lines Exactly one solution consistent (unique) one solution $\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$ dependent Coinciding lines Infinite solution (consistent) infinitely many solutions $\frac{\overline{a_1}}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$ Parallel lines no solution Inconsistent no solution

Interpretation of the pairs of equations

Algebraic Methods:

Substitution Method

Following are the steps to solve the pair of linear equations by substitution method:

 $a_1x + b_1y + c_1 = 0 \dots$ (i) and $a_2x + b_2y + c_2 = 0 \dots$ (ii)



Step 1: We pick either of the equations and write one variable in terms of the other

Step 2: The expression obtained in Step1 should be substituted in the other equation to get a linear equation in one variable

Step 3: Solve this equation and get the value of one variable

> Algebraic Methods:

a) Substitution Method

Following are the steps to solve the pair of linear equations by substitution method:

 $a_1x + b_1y + c_1 = 0 \dots (i)$ and $a_2x + b_2y + c_2 = 0 \dots (ii)$

Step 1: We pick either of the equations and write one variable in terms of the other

Step 2: The expression obtained in Step1 should be substituted in the other equation to get a linear equation in one variable

Step 3: Solve this equation and get the value of one variable

Step 4: Substitute this value in the equation obtained in Step 1 to obtain the value of the other variable.

b) Elimination Method

Step 1: First multiply both the equations by some suitable non-zero constants to make the coefficients of one variable (either x or y) numerically equal.

Step 2: Then add or subtract one equation from the other so that one variable gets eliminated.

 $\Box \Box$ If you get an equation in one variable, go to Step 3.

 $\Box \Box$ If in Step 2, we obtain a true statement involving no variable, then the original pair of equations has infinitely many solutions.

 $\Box \Box$ If in Step 2, we obtain a false statement involving no variable, then the original pair of equations has no solution, i.e., it is inconsistent.

Step 3: Solve the equation in one variable (x or y) so obtained to get its value.

Step 4: Substitute this value of x (or y) in either of the original equations to get the value of the other variable.

MULTIPLE CHOICE QUESTIONS

SECTION A

Q1. The value of 'k' for which the system of equations 4x + ky + 8 = 0 and 2x + 2y + 3 = 0

2 = 0 has a unique solution is



				LOUID FORMULA PROPERTY
	a) k=3	b) k ≠ 4	c) $k \neq 0$	d) k=0
Q2.	The solution of the	equation $x + y = 5 a^{2}$	nd x - y = 5 is	
	a) (0,5)	b) (5,5)	c) (5,0)	d) (10 ,5)
Q3.	The pair of linear ed	quations $x = 0$, $x = -$	-5 has	
	a) One solution	b) two solution c)	infinite no: of solution	d) no solution
Q4.	For what value of 'l	x' do the equations $3x$	-y + 8 = 0 and $6x - 3$	-ky + 16 = 0 represent
	coincident lines			
	a) $\frac{1}{2}$	b) $-\frac{1}{2}$	c) 2	d) -2
Q5.	The pair of linear ed	quations $3x + 5y = 3$	3 and 6x + ky = 8	do not have a solution if k
	a) = 5	b) = 10	c) ≠10	d) ≠ 5
Q6.	The number of solu	tions of $3^{x+y} = 243$ d	and $243^{x-y} = 3$ is	
	a) 0	b) 1	c) 2	d) None
Q7.	If $x = a, y = b$ is t	he solution of the equa	ations $37x + 43y = 12$	x^3 , $43x + 37y = 117$,
	then $a^3 + b^3 =$			
	a) -7	b) 7	c) 9	d) -9
Q8.	The value of k for v	which the line $5x + 7y =$	= 3 and 15x + 21y = k co	incide is
	a) 9	b)5	c) 7	d) 18
Q9.	If $217x + 131y =$	913 and $131x + 22^{\circ}$	7y = 827 then $x + y$	=
	a) 5	b) 6	c) 7	d) 18
Q10). The pair of equatio	ns $y = 0$ and $y = -$	5 has	
	a) One solution	b) two solution	c) infinite no.of solu	tion d) no solution
Q11	. If the system $kx - kx = kx - kx - kx - kx - kx - kx - $	5y = 2, 6x + 2y =	7 has no solution, then	k =
	a) -10	b) -5	c) -6	d) -15
Q12	2. 8 chairs and 5 table	es cost ₹10500. While	5 chairs & 3 tables cost	6450. Cost of one table
	a) 750 b) 900	c) 850 d) 600		
Q13			x + ky = 5 has a un	ique solution when
	x = 2, y = 1 then	k =		
	a) -2	b) 3	c) -3	d) 4
Q14		quations $3x + 7y =$	k; 12x + 2ky = 4k	+ 1 do not have any
	solution if			
-	a) k = 7	b) k = 14		d) k = 28
Q15			3x + 2y = 5 is cons	
	a) $K = 9$	b) k = -9	c) k ≠ -9	d) k ≠ 7



Q16. If $2x + 3y = 0$ and $4x - 3y = 0$ then $x + y =$					
a) 0	b) -1	c) 1	d) 2		
Q17. If (6, k) is a solution of the equation $3x + y = 22$ then $k =$					
a) - 4	b) 4	c) 3	d) -3		
Q18. If $3x + 2y = 13$ and	d 3x - 2y = 5 then x	+y =			
a) 5	b)3	c) 7	d) 11		
Q19. The pair of equation $x = a$, $y = b$ represent lines which are					
a) Parallel	b) intersect at (b, a)	c) coincide	d) intersect at(a, b)		
	11				

Q20. The equation x - y = 0.9 and $\frac{11}{x+y} = 2$ have the solution

a) x = 5, y = 1 b) x = 2.3, y = 3.2 c) x = 3, y = 2 d) x = 3.2, y = 2.3

OBJECTIVE TYPE QUESTIONS

- Q1. In how many points do the lines represented by the equations x y = 0 and x + y = 0 intersect?
- Q2. What is the value of 'a' for which the equations y = x and y = ax have infinitely many solutions
- Q3. State whether or not the lines represented by the equations x + 1 = 0 and 2x + 2 = 0 are coincident?
- Q4. What is the number of solutions of the pair of equations x = 0; y = 0?
- Q5. Do the equations y = x and y = x + 3 represent parallel lines?
- Q6. Find the value of (x + y)if, 3x 2y = 5 and 3y 2x = 3
- Q7. Sum of two numbers is 35 and their difference is 13, find the numbers
- Q8. Find the value of 'p' for which the pair of linear equations 2px + 3y = 7: 2x + y = 6 has exactly one solution
- Q9. Write whether the following pair of linear equations is consistent or not.
- Q10. 2x + y + 9 = 0, x + 3y + 7 = 0
- Q11. Solve for x and y: 99x + 101y = 499,101x + 99y = 501
- Q12. Find whether the lines representing the following pair of linear equations are intersecting, parallel or coinciding. 2x 3y + 6 = 0; 4x 5y + 2 = 0
- Q13. The value of k for which the equations kx + y = 6 and 6x + 2y = 12 will have infinitely many solutions is
- Q14. Express 'y' in terms of 'x' of the equation. 3x + 5y = 11. check whether (3,4) satisfies the given equation or not.



- Q15. Express 'x' in terms of y of the equation 3x-y =2 also check whether (-1,3) satisfies the equation or not?
- Q16. Two positive numbers differ by 3 and their product is 54. Find the no.s
- Q17. If x = a, y = b is the solutions of the equations x y = 2 and x + y = 4 find a &b.
- Q18. The sum of the digits of a two-digit number is 9. If 27 is added to it the number gets reversed. The number is
- Q19. For what value of k do the equations 3x y + 8 = 0 & bx ky + 16 = 0 represent coincident lines.
- Q20. How many solutions do the equations y = 0, y = -7 posses?
- Q21. Find the values of (x + y) (x y) when 28x + 17y = 73, 17x + 28y = 62

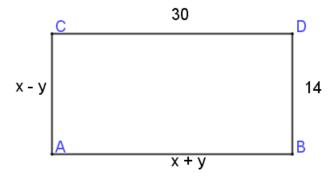
SHORT ANSWER TYPE QUESTIONS (2 MARKS)

SECTION B

- Q1. Solve: 99x + 101y = 499: 101x + 99y = 501
- Q2. Find the value of k for which the pair of linear equations kx + 3y = k 2 and 12x + ky = k has no solution
- Q3. Without drawing the graph, find out whether the lines representing the following pair of linear equations intersect at a point, are parallel or coincident.

$$18 x - 7y = 24$$
; $\frac{9}{5}x - \frac{7}{10}y = \frac{9}{10}$

- Q4. Anu's father is three times as old as Anu. After five years, his age will be two and half times as old as Anu. Represent this situation algebraically only.
- Q5. In the given fig, ABCD is a rectangle. Find the value of x and y?



- Q6. If sum of two positive numbers is 108 and the difference of these numbers is 8, then find the numbers.
- Q7. Solve the following pair of linear equations by substitution method:

 $\mathbf{i} \quad 3x + 2y - 7 = 0$

ii 4x + y - 6 = 0



Q8. Solve the pair of linear equations by elemination method:

- i x y + 1 = 0ii 4x + 3y - 10 = 0
- Q9. Find the value of k for which the given system of equations has infinitely many solutions:
 - i (k-3) x + 3 y = k
 - **ii** k x + k y = 12

Q10. For which value of a and b does the following pair of linear equations has infinite number of solutions?

- i 2x 3y = 7
- ax + 3y = b
- Q11. Write a pair of linear equations which has a unique solution x = 2 and y = -1. How many such pairs are possible?

Q12. Solve for x and y:

- i $mx ny = m^2 + n^2;$
- ii x y = 2n
- Q13. Is the system of linear equations 2x + 3y 9 = 0 and 4x + 6y 18 = 0 consistent? Justify your answer.

Q14. Solve for x and y:

- i $\frac{x}{a} + \frac{y}{b} = 2$ ii $ax - by = a^2 - b^2$
- Q15. For which value of a and b does the following pair of linear equations has infinite number of solutions?
 - i 2x + 3y = 7
 - ii a(x + y) b(x y) = 3a + b 2
- Q16. There are 20 vehicles cars and motorcycles in a parking area. If there are 56 wheel together, how many cars and motorcycles are there.
- Q17. If x 4 is a factor of $x^3 + ax^2 + 2bx 24$ and a b = 8, find the value of a and b.
- Q18. Are the following pair of linear equations consistent? Justify your answer.

 $2ax + by = a; 4ax + 2by - 2a = 0; a, b \neq 0$

Q19. If 2x + y = 23 and 4x - y = 19, find the values of 5x - 3y and y - 2x.



Q20. Find the solutions of the pair of linear equations 5x + 10y - 50 = 0 and x + 8y = 10. Hence find the value of m if y = mx + 5.

SHORT ANSWER TYPE QUESTIONS (3 MARKS)

SECTION C

Q1. Solve by elimination method:

3x + 4y = 102x - 2y = 2

Q2. Find the two-digit numbers whose sum is 75 and difference is 15

- Q3. The age of the father is twice the sum of the ages of his 2 children. After 20 years, his age will be equal to the sum of the ages of his children. Find the age of the father
- Q4. On reversing the digit of a two-digit number, number obtained is 9 less than three times the original number. If the difference of these two numbers is 45, find the original number

Q5. Solve: ax + by = a - b and bx - ay = a + b

- Q6. The larger of the supplementary angles exceeds the smaller by 18° . Find the angles
- Q7. A fraction becomes $\frac{1}{3}$ when 2 is subtracted from the numerator and it becomes $\frac{1}{2}$ when 1 is subtracte from its denominator. Find the fraction.

Q8. Solve by elimination:

a. x - y + 1 = 0 and 4x + 3y - 10 = 0

- b. 3x 4y = 15 and 2x 2y = 8
- Q9. Solve for x and y:

$$\frac{x}{a} + \frac{y}{b} = 2 \text{ and}$$
$$ax - by = a^2 - b^2$$

Q10. Solve for *x* and *y* by method of elimination:

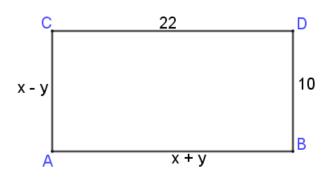
$$47x + 31y = 63$$

 $31x + 47y = 15$

- Q11. The monthly incomes of A and B are in the ratio 5:4 and their expenditure are in the ratio 7:5. If each save 3000/- per month, find the monthly income of each.
- Q12. Four chairs and three tables cost 2100/- and 5 chairs and 2 tables cost 1750/-. Find the cost of a chair and table respectively

Q13. In the given figure ABCD is a rectangle. Find the value of x and y





- Q14. Yash scored 40 marks in a test, receiving 3 marks for each correct answer and losing 1 mark for each wrong answer. Had 4 marks been awarded for each correct answer and 2 marks been deducted for each wrong answer, then Yash would have scored 50 marks. How many questions were there in the test?
- Q15. The denominator of a fraction is 4 more than twice the numerator. When both the numerator and denominator are decreased by 6, then denominator becomes12 times the numerator. Determine the fraction
- Q16. A man has only 20paisa coins and 25 paisa coins in his purse. If he has 50 coins in all totalling 11.25/-, how many coins of each kind does he have?
- Q17. For each of the following system of equations determine the values of k for which the given system has no solution

$$3x - 4y + 7 = 0$$
$$kx + 3y - 5 = 0$$

Q18. For what value of k, will the following system of equations have infinitely many solutions 2x + 3y = 4

(k+2) x + 6y = 3k + 2

Q19. Determine the values of a and b for which the following system of linear equations have infinite solutions

$$2x - (a - 4)y = 2b + 1;$$

$$4x - (a - 1)y = 5b - 1$$

Q20. A and B each have certain number of oranges. A says to B, "if you give me 10 of your oranges, I will have twice the number of oranges left with you." B replies," if you give me 10 of your oranges, I will have the same number of oranges as left with you. Find the number of oranges with A and B separately.

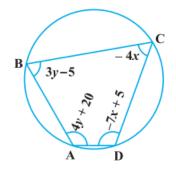
LONG ANSWER TYPE QUESTIONS (4 Marks) SECTION D

Q1. The age of the father is twice the sum of the ages of his two children. After 20 years, his age will be equal to the sum of the ages of his children. Find the age of the father.



- Q2. A boat takes 4 hours to go 44 km downstream and it can go 20 km upstream in the same time. Find the speed of the stream and that of the boat in still water.
- Q3. The sum of the numerator and the denominator of a fraction is 3 less than twice the denominator. If the numerator and the denominator are decreased by one, the numerator becomes half the denominator. Determine the fraction.
- Q4. A number consists of two digits. When the number is divided by the sum of its digits, the quotient is 7. If 27 is subtracted from the number, the digits interchange their places. Find the number.
- Q5. A railway half ticket costs half the full fare, but the reservation charges are the same on a half ticket as on a full ticket. One reserved first-class ticket from the station A to B costs ₹2530. Also one reserved first class ticket and one reserved first class half ticket from A to B costs ₹3810.Find the full first class fare from station A to B and also the reservation charges for a ticket.
- Q6. Given the linear equation 7x 5y 4 = 0. Write another linear equation in two variables such that the geometrical representation of the pair so formed is Intersecting lines, Parallel lines, Coincident lines
- Q7. Two numbers are in the ratio 5:6. If 8 is subtracted from each of the numbers, the ratio becomes 4:5. Find the numbers.
- Q8. There are two examination rooms A and B. If 10 candidates are sent from A to B, the number of candidates in each room is the same. If 20 candidates are sent from B to A, the number of students in A is double the number of students in B. Find the number of students in each room.
- Q9. ABCD is a cyclic quadrilateral. Find the angles of the cyclic quadrilateral.

a.



Q10. Places A and B are 100 km apart on a highway. One car starts from A and another from B at the same time. If the cars travel in the same direction at different speeds, they meet in 5 hours. If they travel towards each other, they meet in one hour. What are the speeds of the two cars?



- Q11. The area of a rectangle decreases by 10 cm², if its length is decreased by 5cm and the breadth is increased by 3 cm. If the length is increased by 5 cm and the breadth is increased by 2 cm, then the area increases by 80 cm². Find the perimeter of the rectangle.
- Q12. Draw the graphs of 2x 3y + 6 = 0 and 2x + 3y 18 = 0. Find the ratio of areas of triangles formed by the given lines with X-axis and Y-axis.
- Q13. Draw the graphs of the equations x y + 1 = 0 and 3x + 2y 12 = 0. Determine the coordinates of the vertices of the triangle formed of these lines and the Y-axis. Shade the triangular region.
- Q14. Determine graphically the vertices of the triangle, the equations of whose sides are given below

$$2y - x = 8; 5y - x = 14; y - 2x = 1$$

- Q15. Draw the graph of the equations x = 3, x = 5 and 2x y 4 = 0. Also find the area of the quadrilateral formed by the lines and the X-axis.
- Q16. Solve the following pair of linear equations:

$$a - bx + a + by = a2 - 2ab - b2$$
$$a + bx + y = a2 + b2$$

CASE STUDY BASED QUESTIONS

17. <u>CASE STUDY -</u>1

Special offers are short-term pricing strategies that businesses, especially shops will adopt to encourage customers to buy from them. During winter season, a shopkeeper sells a jacket at 8% profit and a sweater at 10 % discount thereby getting a sum of ₹1008. If she had sold the jacket at 10 % profit and the sweater at 8 % discount, she would have got ₹1028. Denoting the cost price of one jacket by ₹ x and the list price of one sweater by ₹ y, answer the following situations.





I. Represent the first situation algebraically.

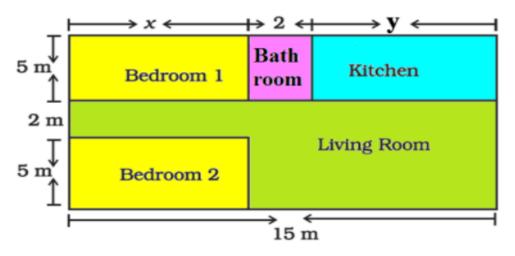
1	\mathcal{U}	2	
a) 12x+10y=11200			c) 12x-10y=11200
b) 10x+12y=11200			d) 10x-12y=1120
-			-

II.	Represent the second situation algebrai	cally
	a) 46x+55y=51400	c) 55x-46y=51400
	b) 55x+46y=51400	d) 46x-55y=51400
III.	The system of linear equations represent	nting both the situations will have.
	a) Infinite number of solutions	c) No Solutions
	b) Unique solution	d) Exactly two solutions
IV.	The graph of the system of linear equat	ions representing both the situations will be
	a) Parallel lines	c) Intersecting lines
	b) Coincident lines	d) None of these

18. CASE STUDY 2:

Apartments have increasingly become the most supplied property type across cities in India. Their popularity can be attributed to reasons including but not limited to contemporary looks, modern day amenities, in-house maintenance and better security. Inaya is planning to buy a 2BHK apartment and the layout is given below.

The design and the measurement has been made such that area bedrooms and kitchen together is 95 sq.m.



1. Which pair of linear equations in two variables does describe this situation.

(a) $x + y = 17$, $3x + y = 15$	(b) $x + y = 27$, $3x + 4y = 95$
(c) $5x + 2y = 15$, $x + 4y = 12$	(d) $2x + y = 19$, $x + y = 13$

2. What is the length of the outer boundary of the layout?



(a) 40 m (b) 54 m (c) 27 m (d) 48 m

3. What is the area of the bedroom 1?

	(a) 30m ²	(b) 40m ²	(c) $55m^2$	(d) 35m ²
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4. What is the cost of laying tiles in kitchen at the rate of \mathbf{E} . 100 per sq.m.

(a) ₹.3000 (b) ₹.3250 (c) ₹.3500 (d) ₹.3750

19. CASE STUDY 3:

An alumni association is an association of former students. These associations often organize social events, publish newsletters or magazines and raise funds for the organisation. The alumni meet of two batches of a college- batch A & batch B were held on the same day in the same hotel in two separate halls "Rose" and "Jasmine". The rents were the same for both the halls. The expense for each hall is equal to the fixed rent of each hall and proportional to the number of persons attending each meet. 50 persons attended the meet in "Rose" hall, and the organisers had to pay \gtrless 10000 towards the hotel charges. 25 guests attended the meet in "Jasmine" hall and the organisers had to pay \gtrless 7500 towards the hotel charges. Denote the fixed rent by \gtrless x and proportional expense per person by \gtrless y.

I. Represe	ent algebra	ically the	situation	in	hall "]	Rose".
------------	-------------	------------	-----------	----	---------	--------

	a) $50x + y = 10000$	c) $x + 50y = 10000$
	b) $50x - y = 10000$	d) $x - 50y = 10000$
II.	Represent algebraically the situation in hall "Jasmi	ne"
	a) $x + 25y = 7500$	c) $25x + y = 7500$
	b) $x - 25y = 7500$	d) $25x - y = 7500$
III.	What is the fixed rent of the halls?	
	a) ₹2500	c) ₹ 4000
	b) ₹3300	d) ₹5000
W	Find the amount the hotel charged per person	

IV. Find the amount the hotel charged per person.

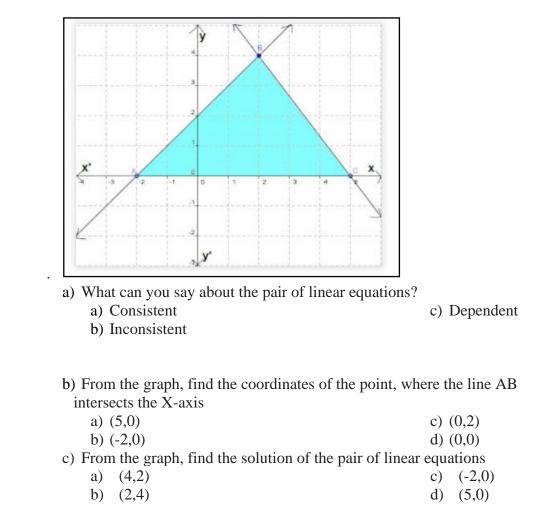
a) ₹ 150	c) ₹130
<i>,</i>	/

b) ₹ 190	d) ₹ 100
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20. CASE STUDY 4:

A pair of linear equations is represented geometrically as shown below.





d)	What	is	the	area	of	the	shaded	region?
----	------	----	-----	------	----	-----	--------	---------

a)	11 sq. units	c)	13 sq. units
b)	12 sq. units	d)	14 sq.units

ANSWERS

	MCQ				Objective		
Q: NO.	ANSWERS	Q: NO	ANSWERS	Q: NO.	ANSWERS	Q: NO.	ANSWERS
1	(b)	11	(d)	1	one	11	intersecting
2	(c)	12	(b)	2	1	12	K = 3
3	(d)	13	(b)	3	yes	13	$y = \frac{11 - 3X}{5}$
4	(c)	14	(b)	4	(0, 0)	14	$x = \frac{y+2}{3}$
5	(b)	15	(a)	5	Yes	15	9&6
6	(b)	16	(a)	6	$\mathbf{x} + \mathbf{y} = 8$	16	A = 3, b = 1
7	(b)	17	(b)	7	24, 11	17	36
8	(a)	18	(a)	8	P ≠ 3	18	K = 2



9	(a)	19	(d)	9	consistent	19	No solution
10	(d)	20	(d)	10	3, 2	20	X + y = 3, x - y =1
HO	RT ANSW	ER TYPE	QUESTIC	ONS (2 MA	RKS)		
Q NO	ANSWER						
1	Add two g	iven equati	ons				
_	x + y = 1	5 (1)					
		two given		ıs			
	x-y = 1						
			(1) + (2)	2)			
			2x = 6 $x = 3$				
	Subx	= 3 in (1)					
2	k 3) y - 2				
2	$\frac{\frac{k}{12} = \frac{3}{k}}{k^2 = 36}$						
	k = +6						
3	<u>18</u> <u>10</u>						
	$\frac{18}{9/5} = \frac{10}{1}$						
	$\frac{-7}{-7} =$: 10					
	$\frac{\frac{-7}{-7/10}}{\frac{24}{9/10}} = \frac{8x}{9}$	 c10 80					
	$\frac{1}{9/10} = \frac{1}{10}$	$\frac{11}{3} = \frac{33}{3}$					
	$\frac{a1}{a2} \neq \frac{b1}{b2}$						
4		ı's age =	Ŷ				
		her's age					
	x = 3y						
	y + 5 = ((1)	۲)				
	2y + 10		5				
5	5x - 2y =						
5	x + y = x - y =						
	2x =						
	x =						
	y = 8	3					
6	x + y =						
	x - y =						
	2x = 1						
	x = 58						
7	y = 50						
'	$\mathbf{X} = \frac{7 - 2y}{3}$	217					
	$4 \times \frac{7-3}{3}$	$\frac{2y}{3} + y - 6$	= 0				
	28 - 83	y + 3y -					
	-5y + 10						
	y = 2 &	x = 1					



0	
8	$(2) \times 4 \rightarrow$
	$4\mathbf{x} - 4\mathbf{y} + 4 = 0$
	$4\mathbf{x} + \mathbf{y} - 6 = 0$
	5y - 10 = 0
	y = 2
	$\begin{array}{c} y = 2 \\ x = 1 \end{array}$
	$\lambda - 1$
0	
9	$\frac{k-3}{k} = \frac{3}{k}$
	k = 6
10	$\frac{2}{a} = -1 = \frac{7}{b}$
	a=-2
	b = -7
11	3x + y = 5
	Infinite number of solution
12	$mx - ny = m^2 + n^2$
	mx - ny = 2 nm
	(2) - (1)
	$(m-n) y = m^2 + n^2 - 2 nm = (m-n)^2$
	Y = m - n
	$\mathbf{x} - (\mathbf{m} - \mathbf{n}) = 2\mathbf{n}$
	$\mathbf{x} = \mathbf{m} + \mathbf{n}$
13	$\frac{2}{4} = \frac{1}{2}$, $\frac{-9}{-18} = \frac{1}{2}$, $\frac{3}{6} = \frac{1}{2}$
	4 2 -18 2 6 2 It has infinite number of solutions. It is consistent.
14	bx + ay = 2 ab
14	$ax - by = a^2 - b^2$
	$(1) \times a$
	$ab x + a^2 y = 2a^2b \tag{3}$
	$(2) \times b$
	$abx - b^2 y = a^2b + b^3$ (4)
	(3) - (4)
	$(a^2 + b^2) y = a^2b + b^3$
	y = b
	Sub y = b in (1)
15	$\frac{x = a}{2x + 3y = 7}$
15	x(a-b) + y(a+b) = 3a + b - 2
	Since it has infinitely many solutions, 2 3 7
	$\frac{2}{a-b} = \frac{3}{a+b} = \frac{3}{3a+b-2}$
	After equating
	a = 5b (1)
	2a - 5b = 6 (2)
	Solve (1) and (2)
	a = 5 and b = 1
16	Let no of cars = x and no of motor cycles = y
	According to our condition
	$x + y = 20 \tag{i}$
	47



	4x + 2y = 56 (ii)
	Solve (i) and (ii)
	x = 8 and $y = 12$
17	Since x - 4 is a factor of $x^3 + ax^2 + 2bx - 24$
	$4^{3} + a \times 4^{2} + 2b \times 4 - 24 = 0$
	a + 2b + 10 = 0 (i)
	$a - b = 8 \tag{ii}$
	Solve (I and (ii)
	a=2, b=-6
18	$\frac{a1}{a2} = \frac{2a}{4a} = \frac{1}{2}$ $\frac{b1}{b2} = \frac{b}{2b} = \frac{1}{2}$
	a2 4a 2 b1 b 1
	$\frac{1}{b^2} = \frac{1}{2b} = \frac{1}{2}$
	$\frac{c1}{c2} = \frac{a}{2a} = \frac{1}{2}$
	It has infinitely many solution, it is consistent $c^2 = 2a + 2$
19	Solve the given equations
1)	x = 7, y = 9
	x = 7, y = 9 So, $5x - 3y = 8$
	y - 2x = -5
20	Solve the given equations
20	x = 10, y = 0
	Sub $x = 10$ and $y = 0$ in $y = mx + 5$
	$0 = m \times 10 + 5$
	m = -1/2

SHORT ANSWER TYPE QUESTIONS (3 MARKS)

ANSWERS: -

1. Ans: 3x + 4y = 10(1)

2x - 2y = 2(2) Multiplying (2) by 2 and adding to (1), we get 7x = 14 x = 2Putting x = 2 in (1), we get 3 (2) + 4y = 10 y = 1Hence x = 2, y=1

2. Let the numbers be x and y.

$$x + y = 75$$
(1)

$$x - y = 15....(2)$$

adding (1) and (2) 2x= 90, x=45.

Putting x=45 in (1), x= 30.

Hence the numbers are x = 30 and y=45

3. Let the present ages of children be **x** years and **y** years respectively.

Present age of father is twice the sum of ages of his 2 children = 2(x+y)(i)



Then by question,

$$(x+20) + (y+20) = 2(x + y) + 20$$
$$x + y + 40 = 2x + 2y + 20$$
$$x + y = 20$$
Putting (x + y) in (i),
$$2(x + y) = 2 \times 20 = 40$$

- 4. let the digit on unit place be x and tens digit be y
 - Then the number = 10y + x

Number formed by reversing the digits = 10x + y

Then,

$$10x + y = 3(10y + x) - 9$$

7x - 29y = -9(i)
Also, x - y = 5
x = y + 5(ii)
(ii) in (i)
9(y + 5) - 29y = -9
y = 44/22 = 2
x = 2+5 = 7

the number = 10(2) + 7 = 27

5. ax + by = a-b....(1)

bx-ay = a+b(2)

solve the equation by using substitution / elimination

then x=1 and y=-1

6. Let x be larger angle and y be smear angle

Then, $x + y = 180^{\circ}$ ----- (1)

 $x-y = 18^0$ ------ (2)

Solving (1) and (2) , we get $x = 99^{0}$ and $y = 81^{0}$

7. Let the fraction be $\frac{x}{y}$

Then,
$$\frac{x-2}{y} = \frac{1}{3} \implies 3x - y$$
....(1)
 $\frac{x}{y-1} = \frac{1}{2} \implies 2x - y = -1$(2)

Solving ,we get x=7 and y=15



Required fraction is $\frac{7}{15}$ 8. (i) x = 1, y = 2(ii) x = 1, y = -39. $\frac{x}{a} + \frac{y}{b} = 2 \Longrightarrow bx + ay = 2ab \dots \dots \dots (i)$ $ax - by = a^2 - b^2$(ii) (i) $\times a \implies abx + a^2y = 2a^2b \dots \dots \dots \dots \dots$ (iii) (ii) \times b \Rightarrow abx - b²y = a²b - b³.....(iv) Solving y = b and x = a10. x = 2 and y = -1By the given conditions 11. 5x-7y=3000(1) 4x-5y=3000(2) Solving, we get x = 2000 /-

Monthly income of A = $5x=5\times2000=10000/-$

Monthly income of $B = 4x = 4 \times 2000 = 8000/-$

12. Let the cost of 1 chair be x /- and that of table be y/-

Then by given condition,

4x+3y=2100(i)

$$5x+2y=1750$$
(ii)

Solving x = 150/- and y = 500/-

Cost of one chair = 150 /- and cost of 1 table = 500/-

13. From the given figure;

$$x - y = 10$$
(i)

$$x + y = 22$$
(ii)

Solving we get , x = 16 and y = 6

14. Let right answer questions attempt by Yash be \mathbf{x} wrong answer questions be y

3x - y = 40....(i) Then. 4x - 2y = 50(ii)

Solving we get x = 15, y = 5

Total number of questions in the test= x + y=15 + 5 = 20

15. Let the fraction be $\frac{x}{y}$

Then, $y = 2x + 4 \implies 2x - y = -4$ (i)



Also,
$$y - 6 = 12(x - 6) \implies 12x - y = 66$$
(ii)

Solving (i) and (ii)

$$x = 7$$
 and $y=18$

Hence the required fraction is $\frac{7}{18}$

x + y = 50(i)

 $20 x + 25y = 1125 \implies 4x + 5y = 225 \dots$ (ii)

Solving, we get x=25 and y=25

Hence there are 24 points of each kind

17. Here
$$a_1 = 3, b_1 = -4, c_1 = 7$$

$$a_2 = k, b_2 = 3, c_2 = -5$$

For no solution, we must have $\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$ We have $\frac{b_1}{b_2} = -\frac{4}{3}$ and $\frac{c_1}{c_2} = -\frac{7}{5}$

Clearly, $\frac{b_1}{b_2} \neq \frac{c_1}{c_2}$. So the given system will have no solution.

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} \Longrightarrow \frac{3}{k} = -\frac{4}{3}$$
$$\Longrightarrow k = -\frac{9}{4}$$

18. A pair of linear equation has infinitely many solutions, if $\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$

Therefore
$$\frac{2}{k+2} = \frac{3}{6} = \frac{4}{3k+2}$$

Solving. k=2

19. A pair of linear equation has infinitely many solutions, if $\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$

Therefore
$$\frac{2}{4} = -\frac{a-4}{-(a-1)} = \frac{2b+1}{5b-1}$$

Solving, a = 7 and b = 3

20. Suppose A has x. oranges and B has y oranges. Then

$$x + 10 = 2(y-10) \implies x - 2y + 30 = 0$$

 $y+10=x-10 \Longrightarrow x-y-20=0$

Solving , we get y=50 and x=70

Hence A has 70 oranges and B has 50 oranges



LONG ANSWER TYPE QUESTIONS- ANSWERS

Qn.No.	Answers
1.	40 years
2.	Speed of the stream=3km/hr
2.	Speed of the boat in still water = 8 km/hr
3.	Fraction 47
4.	Number=63
5.	Full first class fare=₹2500
J.	Reservation Charge =₹30
6.	(i) Any linear equation satisfying the condition
0.	$a1/a2 \neq b1/b2$
	(ii) Any linear equation satisfying the condition
	$a1/a2 = b1/b2 \neq c1/c2$
	(ii) Any linear equation satisfying the condition
	a1/a2 = b1/b2=c1/c2
7.	40,48
8.	100,80
9.	Angle A=70°
	Angle B=120°
	Angle C=60°
	Angle D=110°
10.	60 km/hr, 40 km/hr
11.	46 cm
12.	4:1
13.	(0,6) . (0,1) . (2,3)
14.	$(-4,2) \cdot (-4,2) \cdot (-4,3) \cdot (-4,2)$
15.	8 square units
16.	x=a+b, y=-2aba+b
17.	(i)A $(ii)B$ $(iii)B$ $(iv) B$
18.	(i)D (ii)B (iii)A (iv) C (i)
10.	$\begin{array}{c} (i)D (ii)D (iii)A (iii)D (iv) D \end{array}$
20.	$\begin{array}{c} (i)C (i)A (ii)D (iv)D \\ (i)A (ii)B (iii)B (iv)D \end{array}$
Qn. No.	Hints/Solutions
<u>Qii. No.</u> 1.	Let the present age of his two children be "x" years and "y" years.
1.	Present age of father = $2(x+y)$ (1)
	A.T.Q.
	2x+y+20=x+20+y+20
	2x+y+20=x+20+y+20 2x+2y+20=x+y+40
	2x+2y+20-x+y+40 2x+2y-x-y=40-20
	x+y=20(2)
	Substituting eqn (2) in eqn (1), we get
	Present age of father = 2×20
	= 40 years
2.	Let the speed of the stream = $y \text{ km/hr}$ and
	Speed of the boat in still water = $x \text{ km/hr}$
	Speed of the boat in downstream =
	(x+y)km/hr
	Speed of the boat in upstream =
	(x-y)km/hr
	A.T.Q



	44x+y = 4
	44=4(x+y)
	x+y=11(1)
	Also 20x-y=4
	20=4x-y
	x-y=5(2)
	Adding eqns 1 and 2 we get,
	2x=16
	x=8
	Substituting $x=8$ in eqn(1), we get
	8+y=11
	y=3
	Speed of the stream = 3 km/hr and
	Speed of the boat in still water = 8 km/hr
3	Let the numerator be x and the denominator be y
	Fraction is xy
	According to the first condition
	x+y=2y-3
	x+y-2y=-3
	x-y=-3(1)
	According to the second condition
	x-1=12y-1
	2x-1=y-1 2x 2=x 1
	2x-2=y-1
	2x-y=1(2)
	Subtracting eqn (2) from eqn (1) we get -x=-4
	x=4
	Substituting $x=4$ in equation 2, we get
	2x4-y=1
	$\begin{array}{c} 2x + y - 1 \\ 8 - y = 1 \end{array}$
	y=7
	Fraction is 47
4	Let the digit in ones place be y and the digit in tens place be y.
	Two digit number = $10x+y$
	Two digit number – Tox+y
	Given $10x+yx+y=7$
	$\Rightarrow 10x + y = 7(x + y)$
	$\therefore 10x+y-7x-7y=0$
	3x-6y=0
	x-2y=0(1)
	According to the second condition.
	10x + y - 27 = 10y + x
	10x+y-10y-x=27
	9x-9y=27
	x-y=3(2)
	Equation (1)-(2)
	x-2y-x-y=0-3
	x-2y-x+y=-3
	-y=-3
	y=3
	53



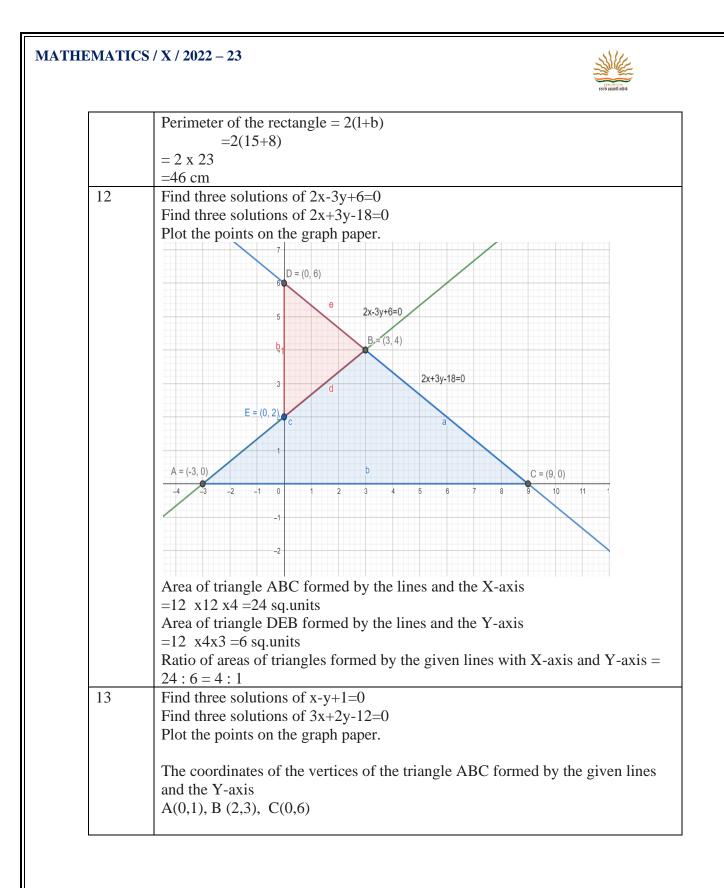
	Substituting $y=3$ in equation (2), we get
	x-3=3
	x=6 Two-digit number =10x+y
	=10x6+3
	=60+3=63
	20y + y - 27 = 10y + 2y
	$\Rightarrow 9y = 27$
	$\Rightarrow y = 3$
	Substitute y value in $eqn(1)$
	we get, $x = 2 \times 3$
	$\Rightarrow x = 6$
	Hence the required number is 63.
5	Let the cost of full fare be $\forall x$ and the cost of half first class fare be $\forall \frac{x}{2}$,
	Δ
	respectively and reservation charges be ₹ y per ticket. Case I
	The cost of one reserved first class ticket from the stations A to B = ₹ 2530
	$x + y = 2530 \dots (i)$
	$x + y = 2550 \dots (1)$
	Case II
	The cost of one reserved first class ticket and one reserved first class half ticket
	from stations
	A to $B = 3810$
	$\Rightarrow x + y + \frac{x}{2} + y = 3810$
	$\Rightarrow x + \frac{x}{2} + y + y = 3810$
	$\Rightarrow \frac{3x}{2} + 2y = 3810$
	Multiplying throughout by 2, we get
	$\Rightarrow 3x + 4y = 7620 \dots (ii)$
	Now, multiplying Eq. (i) by 4 and then subtracting from Eq. (ii), we get
	3x + 4y - 4x - 4y = 7620 - 10120
	-x = -2500
	$\Rightarrow x = 2500$
	On putting the value of x in Eq. (i), we get
	2500+y=2530
	$\Rightarrow y = 30$
	Hence, full first-class fare from stations A to B is
-	₹ 2500 and the reservation for a ticket is ₹ 30.
6.	(i) Any linear equation satisfying the condition
	$a1a2 \neq b1b2$ (ii) Any linear equation satisfying the condition
	(ii) Any linear equation satisfying the condition $\frac{1}{2} - \frac{1}{2} - \frac{1}{2}$
	$a1/a2 = b1/b2 \neq c1/c2$ (ii) Any linear equation satisfying the condition
	(ii) Any linear equation satisfying the condition a1/a2 = b1/b2=c1/c2
7.	Let the two numbers be x and y
/.	According to the first condition
	xy = 56
	Cross multiplying, we get
	6x=5y
	54

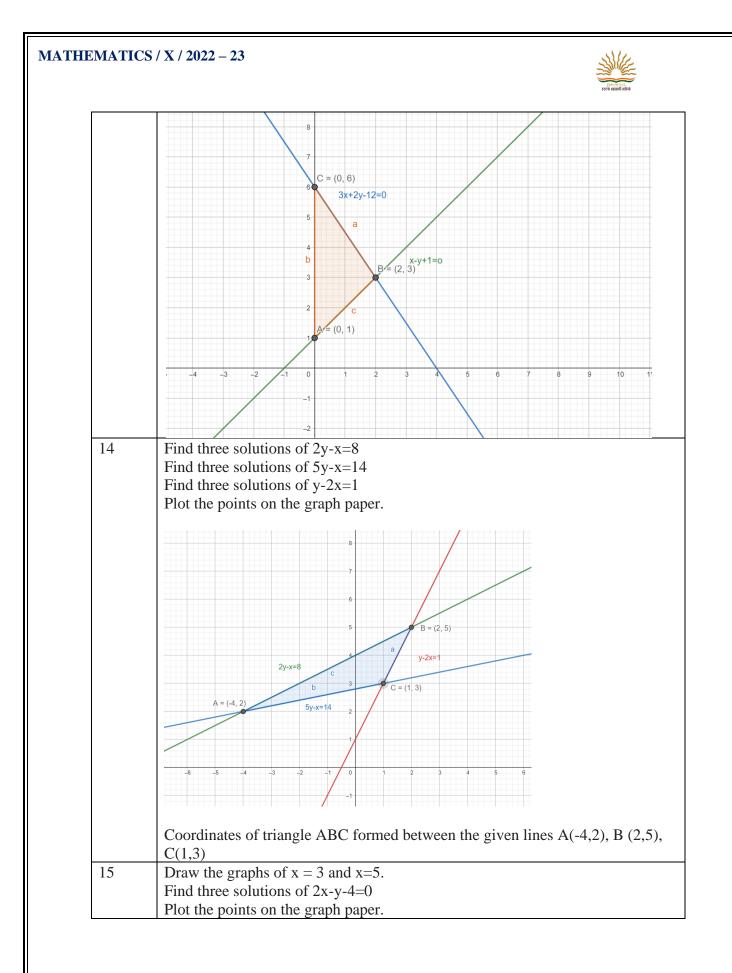


	6x-5y=0(i)
	According to the second condition
	x - 8y - 8 = 45
	Cross multiplying, we get
	5x-8=4y-8
	5x-40=4y-32
	5x-4y=40-32
	5x-4y=8(ii)
	Multiplying eqn (i) by 4, we get
	24x-20y=0 (iii)
	Multiplying eqn (ii) by 5, we get
	25x-20y=40(iv)
	Subtracting eqn (iii)-eqn(iv), we get
	24x-20y-25x+20y=-40
	-x = -40
	x=40
	Substituting $x = 40$ in eqn (i), we get
	$6 \times 40-5y=0$
	240-5y=0 240-5y
	240=5y
	y=48
0	The numbers are 40 and 48.
8.	Let the number of students in room A be x and that in room B be y.
	According to the first condition
	x - 10 = y + 10
	$\Rightarrow x - y = 20 (i)$
	According to the second condition, we get
	x + 20 = 2(y - 20)
	x+20=2y-40
	x-2y=-40-20
	$\Rightarrow x - 2y = -60(ii)$
	Eqn (i) - Eqn (ii) we get,
	x-y-x+2y=20+60
	y=80
	Substituting $y=80$ in eqn (i), we get $x-80=20$
	x=100
	Number of students in room $A = 100$
	Number of students in room $B = 80$
9	We know that the sum of the opposite angles of a cyclic quadrilateral is 180°
	Thus, we have
	$\angle C + \angle A = 180$
	4y + 20 - 4x = 180
	-4x + 4y = 160
	x - y = -40(1)
	And, $\angle B + \angle D = 180$
	3y - 5 - 7x + 5 = 180
	-7x + 3y = 180(2)
	•
	Multiplying
	equation (1) by 3, we get (2)
	3x - 3y = -120(3)
	Adding equation (2) to equation (3), we get



	7			
	-7x + 3x = 180 - 120			
-4x = 60				
	x = -15			
	Substituting this value in equation (1), we get			
	x - y = -40			
	-15 - y = -40 y = 40-15			
	= 25			
	$\angle A = 4y + 20 = 4(25) + 20 = 120^{\circ}$			
	$\angle B = 3y - 5 = 3(25) - 5 = 70^{\circ}$			
	$\angle B = 3y - 5 = 3(25) - 5 = 70^{\circ}$ $\angle C = -4x = -4(-15) = 60^{\circ}$			
	$\angle D = 5-7x$			
	$\angle D = 5 - 7(-15) = 110^{\circ}$			
10	Let x km/hr be the speed of car from point A and			
	y km/hr be the speed of car from point B.			
	If the car travels in the same direction,			
	5x - 5y = 100			
	$\mathbf{x} - \mathbf{y} = 20 \dots $			
	If the car travels in the opposite direction,			
	x + y = 100(ii)			
	Adding equations (i) and (ii), we get			
	2x=120			
	x = 60 km/hr			
	Substituting this in equation (i), we get,			
	60 - y = 20			
	y = 40 km/h			
	Therefore, the speed of car from point $A = 60$ km/hr			
	Speed of car from point $B = 40$ km/hr.			
11	Let the length of the rectangle be x cm and its breadth be y cm			
	Area of the rectangle = $xy cm^2$			
	According to the first condition,			
	x-5y+3=xy-10			
	xy+3x-5y-15=xy-10			
	3x-5y=15-10			
	3x-5y=5(1)			
	According to the second condition,			
	x+5y+2=xy+80			
	xy+2x+5y+10=xy+80			
	2x+5y=70(2)			
	Adding eqns (1) and (2), we get			
	5x=75			
	x=15			
	Substituting $x=15$ in eqn (1), we get			
	Substituting $x=15$ in eqn (1), we get $3 \times 15-5y=5$			
	3 x 15-5y=5			
	3 x 15-5y=5 45-5y=5			
	3 x 15-5y=5 45-5y=5 -5y= -40			
	3 x 15-5y=5 45-5y=5 -5y= -40 y=8			
	3 x 15-5y=5 45-5y=5 -5y= -40			







$f = \begin{cases} 1 \\ a + b + c + b \\ a + c + c + b \\ a + c + c + b \\ a + c + c + c + b \\ a + b $						
AB = OB-OA = 5-3 = 2 AD = 2 BC = 6 Thus, quadrilateral ABCD is a trapezium, then, Area of quadrilateral ABCD = $\frac{1}{2} \times (AB) \times (AD + BC)$ =12 x 2 x (2+6) = 12 = 8 sq units 16 The given equations are (a - b)x + (a + b) y = a ² - 2ab - b ² (a + b)(x + y) = a ² + b ² (a - b)x + (a + b) y = a ² - 2ab - b ² (i) (x + y)(a + b) = a ² + b ² (a + b) x + (a + b) y = a ² + b ² (ii) Subtracting equation (ii) from equation (i), we get (a - b) x - (a + b) x = (a ² - 2ab - b ²) - (a ² + b ²) x(a - b - a - b) = -2ab - 2b ² - 2bx = -2b (b + a) x = b + a Substituting this value in equation (i), we get (a + b)(a - b) + y (a + b) = a ² - 2ab - b ² a ² - b ² + y(a + b) = a ² - 2ab - b ² a ² - b ² + y(a + b) = a ² - 2ab - b ² (a + b) y = -2ab y = -2aba+b CASE STUDY QUESTIONS 17 Let the cost price of one jacket be ₹ x and the list price of one sweater be ₹ y i. According to the first condition, x+8100 x+y-10100 y=1008 108 x 100+90100y=1008 108 x+90 y=100800		X' - 4 - 3 - 2 - 1 0 + 1 - 2 + 3 - 4 - 3 - 2 - 1 0 + 1 - 2 + 3 - 4 - 3 - 2 - 1 0 + 1 - 2 + 3 - 4 - 3 - 2 - 1 - 1 - 1 - 2 + -3 - 4 - 4 - 2 - 4 - 3 - 4 - 4 - 2 - 4 - 3 - 4 - 4 - 2 - 4 - 3 - 4 - 4 - 2 - 4 - 3 - 4 - 4 - 2 - 4 - 3 - 4 - 4 - 2 - 4 - 3 - 4 - 4 - 2 - 4 - 3 - 4 - 4 - 2 - 4 - 3 - 4 - 4 - 4 - 3 - 2 - 1 - 1 - 4 - 2 - 4 - 2 - 4 -				
Area of quadrilateral ABCD = $\frac{1}{2} \times (AB) \times (AD + BC)$ =12 x 2 x (2+6) = 12 = 8 sq units 16 The given equations are (a - b)x + (a + b) y = a ² - 2ab - b ² (a + b)(x + y) = a ² + b ² (a - b) x + (a + b) y = a ² - 2ab - b ² (i) (x + y)(a + b) = a ² + b ² (a + b) x + (a + b) y = a ² + b ² (ii) Subtracting equation (ii) from equation (i), we get (a - b) x - (a + b) x = (a ² - 2ab - b ²) - (a ² + b ²) x(a - b - a - b) = -2ab - 2b ² - 2bx = -2b (b + a) x = b + a Substituting this value in equation (i), we get (a + b)(a - b) + y (a + b) = a ² - 2ab - b ² a ² - b ² + y(a + b) = a ² - 2ab - b ² (a + b) y = -2ab y = -2aba+b CASE STUDY QUESTIONS 17 Let the cost price of one jacket be ₹ x and the list price of one sweater be ₹ y i. According to the first condition, x+8100 x+y-10100 y=1008 108 x 100+90100y=1008 108 x+90 y=100800		AB = OB-OA = 5-3 = 2 $AD = 2$				
= 8 sq units 16 The given equations are (a - b)x + (a + b) y = a ² - 2ab - b ² (a + b)(x + y) = a ² + b ² (a - b) x + (a + b) y = a ² - 2ab - b ² (i) (x + y)(a + b) = a ² + b ² (a + b) x + (a + b) y = a ² + b ² (ii) Subtracting equation (ii) from equation (i), we get (a - b) x - (a + b) x = (a ² - 2ab - b ²) - (a ² + b ²) x(a - b - a - b) = -2ab - 2b ² - 2bx = -2b (b + a) x = b + a Substituting this value in equation (i), we get (a + b)(a - b) + y (a + b) = a ² - 2ab - b ² a ² - b ² + y(a + b) = a ² - 2ab - b ² (a + b) y = -2ab y = -2aba+b CASE STUDY QUESTIONS 17 Let the cost price of one jacket be ₹ x and the list price of one sweater be ₹ y i. According to the first condition, x+8100 x+y-10100 y=1008 108 x 100+90100y=1008 108 x+90 y=100800		Area of quadrilateral ABCD = $\frac{1}{2} \times (AB) \times (AD + BC)$				
16The given equations are (a - b)x + (a + b) y = a² - 2ab - b² (a + b)(x + y) = a² + b² (a - b) x + (a + b) y = a² - 2ab - b²(i) (x + y)(a + b) = a² + b² (a + b) x + (a + b) y = a² + b² (ii) Subtracting equation (ii) from equation (i), we get (a - b) x - (a + b) x = (a² - 2ab - b²) - (a² + b²) x(a - b - a - b) = -2ab - 2b² - 2bx = -2b (b + a) x = b + a Substituting this value in equation (i), we get (a + b)(a - b) + y (a + b) = a² - 2ab - b² a² - b² + y(a + b) = a² - 2ab - b² (a + b) y = -2ab y = -2ab + bCASE STUDY QUESTIONS17Let the cost price of one jacket be ₹ x and the list price of one sweater be ₹ y i. According to the first condition, x+8100 x+y-10100 y=1008 108 x +90 y=100800						
 17 Let the cost price of one jacket be ₹ x and the list price of one sweater be ₹ y i. According to the first condition, x+8100 x+y-10100 y=1008 108 x 100+90100y=1008 108 x+90 y=100800 	16	The given equations are $(a - b)x + (a + b) y = a^2 - 2ab - b^2$ $(a + b)(x + y) = a^2 + b^2$ $(a - b) x + (a + b) y = a^2 - 2ab - b^2$ (i) $(x + y)(a + b) = a^2 + b^2$ $(a + b) x + (a + b) y = a^2 + b^2$ (ii) Subtracting equation (ii) from equation (i), we get $(a - b) x - (a + b) x = (a^2 - 2ab - b^2) - (a^2 + b^2)$ $x(a - b - a - b) = -2ab - 2b^2$ -2bx = -2b (b + a) x = b + a Substituting this value in equation (i), we get $(a + b)(a - b) + y (a + b) = a^2 - 2ab - b^2$ $a^2 - b^2 + y(a + b) = a^2 - 2ab - b^2$ (a + b) y = -2ab				
i. According to the first condition, x+8100 x+y-10100 y=1008 108 x 100+90100y=1008 108 x+90 y=100800		STUDY QUESTIONS				
	17	i. According to the first condition, x+8100 x+y-10100 y=1008 108 x 100+90100y=1008				

		का ते कुरे करपूर केन्द्रीय विश्वस्वय संगटन
	Dividing through out by 9, we get 12x+10 y=11200 Answer : Option A ii. According to the second condition x+10100 x+y-8100 y=1028 110x 100+92100y=1028 110x+92 y=102800 Dividing through out by 2, we get 55x+46y=51400 Answer : Option B iii. Option B – Unique solution iv. Option C – Intersecting lines	
18	Area of Bedroom 1 = 5x Area of bedroom 2 = 5x Area of Kitchen = 5y Area of two bedrooms and Kitchen together is 95 sq. m => 5x + 5x + 5y = 95 10 x+5y=95 => 2x + y = 19(1) Also x + 2 + y = 15 => x + y = 13(2) Answer (i) Option D Ans (ii) Option B Length of the outer boundary of the layout=2(15+12) = 2 x 27 = 54 m Answer (iii) Option A Area of bedroom 1 = 5 x6 = 30 m ² Ans(iv) Option C Area of kitchen = 5 x7 = 35 m ² Cost of laying tiles in the kitchen = 35 x 100 = ₹ 3500	
19	Let us denote the fixed rent by ₹ x and proportional expense per person by ₹ y. i. Algebraic representation of the situation in "Rose" hall x+50 y=10000 Answer- Option C ii. Algebraic representation of the situation in "Jasmine" hall x+25y=7500 Answer- Option A Subtracting the equations represented by (i) and (ii) x+50y-x+25y=10000-7500 25 y=2500 y=100 Substituting y=100 in x+50 y=10000, we get	

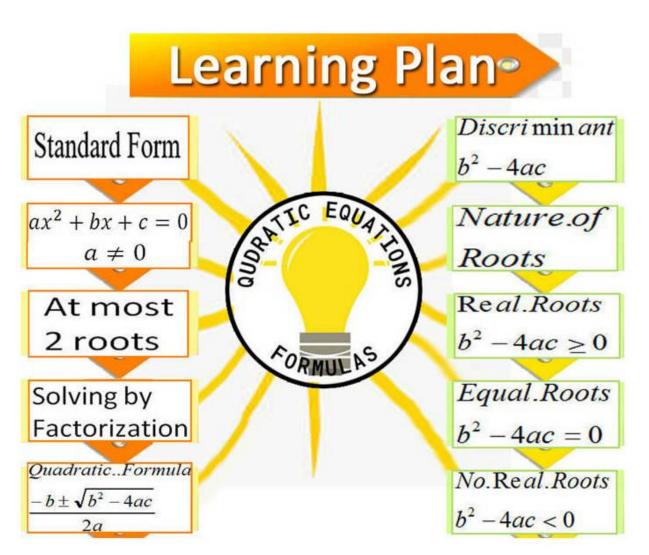


	x+50 x 100=10000		
	x+5000=10000		
	x=5000		
	iii. Answer : Option D		
	iv. Answer : Option D		
20	i. Consistent		
	ii. (-2,0)		
	iii. (2,4)		
	iv. Area of the shaded region = $12 \times 7 \times 4$		
	= 14 sq. units		

CASE STUDY QUESTIONS

SL.NO.	ANSWERS		
	CASE STUDY 1		
1	b) $x + 10y = 75$, $x + 15y = 110$		
2	c) Rs.355		
3	a) $x + 8y = 91$, $x + 14y = 145$		
4	b) Rs.289		
5	(c)		
	CASE STUDY 2		
1	(a) $2x + y = 19$, $x + y = 13$		
2	(c) 54m		
3	(b) area of bedroom = 30 sq.m, area of kitchen = 35 sq.m		
4	(a)75 sq.m		
5	(d)Rs.1750		





LEARNING PLAN

- TOPIC 1: Standard form of a quadratic equation is ax² + bx + c = 0 where a ≠ 0, where a, b, c are real numbers. It has at most two roots generally called as α and β
- TOPIC 2: A Quadratic equation can be solved by Factorisation method
- Quadratic formula. Quadratic formula is, $-b \pm \sqrt{b^2 4ac}$ provided $b^2 4ac \ge 0$
- **TOPIC 3:** $b^2 4ac$ is called DISCRIMINANT.
- **TOPIC 4** : A quadratic equation has
 - ▶ two distinct real roots if $b^2 4ac > 0$
 - ▶ two equal real roots if $b^2 4ac = o$
 - > no real roots if $b^2 4ac < 0$



VERY SHORT ANSWER TYPE & MULTIPLE CHOICE QUESTIONS (1MARK)

SECTION A

Q1.	Q1. What is the positive root of $\sqrt{3x^2 + 6} = 9$				
	(a) 3	(c) 0			
	(b) 5	(d) none of these			
Q2.					
	(a) $\alpha > 3$	(c) $\alpha = 3$			
	(b) α < 3	(d) none			
Q3.	Find the nature of the roots of the Quadratic equ	uation $2x^2 - 4x + 3 = 0$?			
	(a) real roots	(c) equal roots			
	(b) no real roots	(d) none			
Q4.	Find the positive values of k for which the Quad	lratic equation $x^2 + kx + 64 = 0$ and			
	$x^2 - 8x + k = 0$, both will have the real roots?				
	(a) $k = 4$	(c) $k > 16$			
	(b) k =16	(d) k< 4			
Q5.	If the sum of the roots of the quadratic equation 3	$2x^{2} + (2k + 1)x - (k + 5) = 0$ is equal to the			
	product of roots, then the value of k is $(2)^{2}$				
	(a) 2	(c) 4			
06	(b) 3 164	(d) 5			
Q6.	If the equation $x^2 - bx + 1 = 0$ does not possess r				
	(a) $-3 < b \le +3$ (b) $-2 < b \le +2$	(c) $b > 2$ (d) $b < -2$			
07	1	(d) $b < -2$			
Q7.	Find the roots of the quadratic equation $x - \frac{1}{x}$ is				
	(a) $\frac{3}{2}, \frac{-3}{2}$	(c) $\frac{2}{3}$, $\frac{-2}{3}$			
	(b) $\frac{3+\sqrt{13}}{2}$, $\frac{3-\sqrt{13}}{2}$	(d) none			
00					
Q8.	If $(x + 4)(x - 4) = 9$, then the values of x are	(c) 5 5			
	(a) ± 5	(c) 5, 5			
	(b) $\pm \frac{1}{5}$	(d) $\frac{1}{5}, \frac{1}{5}$			
Q9.	How many real roots does the equation $(x + 1)^2$	$-x^2 = 0$ have?			
	(a) 1	(c) 3			
	(b) 2	(d) 4			
Q10	Q10. The product of two successive integral multiples of 5 is 300. Then the numbers are				
	(a) 25, 30 (b) 10, 15				
	(b) 10, 15 () 20, 25				
	(c) 30, 35 (d) 15, 20				
	(d) 15, 20 SHORT ANSWER TYPE QUESTIONS (2 MARKS)				
	<u>SECTION</u>	<u>N B</u>			

Q1. For what value of p for equation $2x^2 + 3x + p = 0$ will have real roots?



- Q2. Find the sum of the roots of the quadratic equation $3x^2 9x + 5 = 0$?
- Q3. If $\frac{1}{2}$ is a root of the equation $x^2 + kx \frac{5}{4} = 0$, then what is the value of k?
- Q4. If the one root of the equation $4x^2 2x + p 4 = 0$ be the reciprocal of other, then what is the value of p?
- Q5. What is the value of k for which the quadratic equation $2x^2 kx + k = 0$ has equal roots?
- Q6. Find the roots of the quadratic equation $x^2 3x = 0$
- Q7. If $p^2x^2 q^2 = 0$, then find the value of x?
- Q8. Find the value of m for which the quadratic equation $(m 1)x^2 + 2(m 1)x + 1 = 0$ has two real and equal roots
- Q9. Solve the following quadratic equation for x: $\sqrt{3} x^2 + 10x + 7\sqrt{3} = 0$
- Q10. The product of Rahana's age (in years) 5 years ago and his age 7 years from now, is one more than twice his present age. Find their present age?
- Q11. Find the roots of the equation $x^2 + x p(p+1) = 0$
- Q12. If 2 is a root of the quadratic equation $3x^2 + px 8 = 0$ and the quadratic equation
- Q13. $4x^2 2px + k = 0$ has an equal root, find the value of k?
- Q14. Find the roots of the quadratic equation $4x^2 4px + (p^2 q^2) = 0$
- Q15. One year ago, father's age was 8times as old as his son and now his age is equal to the square of his son's age. Find the son's age?
- Q16. The sum of a number and its reciprocal is $\frac{5}{2}$. Find the numbers?
- Q17. The product of two consecutive natural numbers is 72. Find the numbers?
- Q18. What is the discriminant of the quadratic equation $7\sqrt{3}x + 10x \sqrt{3} = 0$?
- Q19. If a and b are the roots of the equation $x^2 + ax + b = 0$ then what is the value of a + b?
- Q20. If one root of the equation $2x^2 + kx + 4 = 0$ is 2, then find its other root?
- Q21. What is the discriminant of the quadratic equation: $(x + 5)^2 = 2(5x 3)$

SHORT ANSWER TYPE QUESTIONS (3 MARKS)

SECTION C

- Q1. Find the nature of the roots of the following quadratic equations. If the real roots exist, find them: $2x^2 + 4x 8 = 0$
- Q2. Using the quadratic formula, solve the following quadratic equation for x. $p^2x^2 + (p^2 q^2)x q^2 = 0$



- Q3. If α and β are the roots of the equation $2x^2-6x + a = 0$ and $2\alpha + 5\beta = 12$, find the value of a?
- Q4. If -5 is a root of the quadratic equation $2x^2 + px 15 = 0$ and the quadratic equation $p(x^2 + x) + k = 0$ has equal roots, then find the value of k.
- Q5. Find the positive value of k for which the equation $x^2+kx+64 = 0$ and $x^2-8x+k = 0$ will both have real roots?
- Q6. Solve for x. $\frac{1}{x+1} + \frac{3}{5x+1} = \frac{5}{x+4}$, $x \neq -1$, $-\frac{1}{5}$, -4
- Q7. The sum of ages (in years) of a son and his father is 35 years and product of their ages is 150 years, find their ages.
- Q8. The sum of the squares of two consecutive natural numbers is 421. Find the numbers.
- Q9. A passenger train takes 2 hours less for a journey of 300 km if its speed is increased by 5 km/hr from its usual speed. Find the usual speed of the train?
- Q10. Speed of a boat in still water is 11 km/hr. It can go 12 km upstream and return downstream to the original point in 2 hrs 45 min. Find the speed of the stream?
- Q11. A plane left 30 min late than its scheduled time and in order to reach the destination 1500 km away in time, it has to increase its speed by 100 km/hr from the usual speed. Find its usual speed?
- Q12. A takes 6 days less than the time taken by B to finish a piece of work. If both A and B together can finish it in 4 days, find the time taken by B to finish the work?
- Q13. If $(x^2 + y^2) (a^2 + b^2) = (ax + by)^2$. Prove that $\frac{x}{a} = \frac{y}{b}$
- Q14. Solve the following quadratic equations:
 - a. $2x^2 + 6\sqrt{3} x 60 = 0$ b. $x^2 + 5x - (a^2 + a - 6) = 0$ c. $(x - 1)^2 - 5(x - 1) - 6 = 0$ d. $a^2b^2x^2 + b^2x - a^2x - 1 = 0$
- Q15. Two pipes running together can fill a tank in $11\frac{1}{9}$ minutes. If one pipe takes 5 minutes more than the other to fill the tank, find the time in which each pipe would fill the tank separately

HOT QUESTIONS (3MARK)

Q1. Solve for x. $x^{\frac{2}{3}} + x^{\frac{1}{3}} - 2 = 0$



- Q2. Three consecutive positive integers are such that the sum of the square of the first and the product of the other two is 46, find the integers.
- Q3. If the roots of the quadratic equation (x a) (x b) + (x b) (x c) + (x c) (x a)= 0 are equal, then show that a = b = c.
- Q4. In a rectangular park of dimensions 50 m \times 40 m, a rectangular pond is constructed so that the area of grass strip of uniform width surrounding the pond would be 1184 m². Find the length and breadth of the pond.
- Q5. P and Q are centres of circles of radii 9 cm and 2 cm respectively. PQ = 17 cm. R is the centre of the circle of radius x cm which touches given circles externally. Given that angle PRQ is 90°. Write an equation in x and solve it.

LONG ANSWER TYPE QUESTIONS (4 MARKS) SECTION D

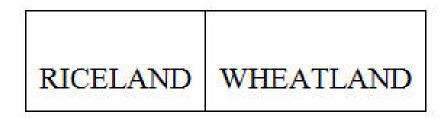
- Q1. Seven years ago, Rahul's age was five times the square of Reena's age. Three years hence, Reena's age will be two fifth of Rahul's age. Find their present ages.
- Q2. The diagonal of a rectangular field is 16metres more than the shorter side. If the longer side is14 metres more than the shorter side, then find the length of the sides of the field.
- Q3. One fourth of a herd of camel was seen in the forest. Twice the square root of the herd had gone to the mountains and the remaining 15 camels were seen on the bank of the river. Find the total number of camels.
- Q4. A train travels 180 km at a uniform speed. If the speed had been 9km/hr more, it would have taken 1 hour less. Find the speed of the train.
- Q5. Rs 9000 were divided equally among certain number of persons. Had there been 20 more persons, each would have got Rs160 less. Find the original number of persons.
- Q6. Two taps running together can fill a tank in $3\frac{1}{13}$ hours. If one tap takes 3 hours more than the other to fill the tank, then how much time will each tap take to fill the tank.
- Q7. Solve the following quadratic equations

 $9x^2 - 9(a+b) x + [2a^2 + 5ab + 2b^2] = 0$

- Q8. Solve for x: $\frac{x-3}{x-4} + \frac{x-5}{x-6} = \frac{10}{3}$, $x \neq 4, 6$
- Q9. A motor boat whose speed is 24 km/hr in still water takes 1 hour more to go 32 km upstream than to return downstream to the same spot. Find the speed of the stream.



Q10. Madhav has a field with total area 1260 square metre. He uses it to grow wheat and rice. The land used to grow wheat is rectangular in shape while the rice land is in the shape of a square as shown in the following figure. The length of wheat land is 3m more than twice the length of Rice land. find the area of wheat land.



CASE STUDY BASED QUESTIONS

CASE STUDY 1

John and Jayant are very close friends. They decided to go to Ranikhet with their families in separate cars. John's car travels at a speed of x km/hr while Jayant's car travels 5km/hr faster than Johan's car. Johan took 4 hours more than Jayant to complete the journey of 400 km.



- The distance covered by Jayant's car in two hours is
 a) 2(x+5) km
 b) (x-5) km
 c) 2(x+10) km
 d) (2x+5) km
- 2. The quadratic equation describing the speed of Johan's car is

a) x ² -5x-500=0	b) $x^{2}+4x-400=0$	c) $x^{2}+5x-500=0$	$d x^2 - 4x + 400 = 0$
<i>a) n c n c o o</i>	O/M		<i>GM M M M</i>

- 3. The speed of Johan's car in km/hr
 - a) 20 b) 15 c) 25 d)10
- 4. The speed of Jayant's car in km/hr
 - a) 25 b) 20 c) 30 d) 15
- 5. Time taken by Jayant to travel 400 km is
 - a) 20 hours b) 40 hours c) 25 hours d) 16 hours

CASE STUDY 2



An Auditorium was booked for School Annual Day Celebrations and the seats are arranged in a particular manner. The number of rows is equal to the number of seats in each row. When the number of rows was doubled and the number of seats in each row was reduced by 10, the total number of seats increased by 300



Based on the above information answer the following questions

- 1. If x is taken as number of row in original arrangement which quadratic equation describe the situation?
 - a) $x^2+20x-300=0$ b) $x^2-20x-300=0$ c) $x^2-20x+300=0$ d) $x^2-10x+300=0$
- 2. Find the number of rows are there in the original arrangement?

a) 20 b) 35 c) 30 d) 40

- 3. How many seats are there in the auditorium in original arrangement?
 - a) 500 b) 600 c) 480 d) 900
- 4. How many seats are there in the auditorium after re-arrangement?

a) 1000 b)1200 c)1500 d)1800

CASE STUDY 3

The speed of a motor boat is 20 km/hr. For covering the distance of 15 km the boat took 1 hour more for upstream than downstream.



1. If the speed of the stream be x km/hr. then speed of the motorboat in upstream will be

a)20 km/hr b)(20+x) km/hr c)(20-x) km/hr d)(x-20) km/hr

2. If the speed of stream is 10 km/hr, and then the speed of the motor boat in downstream is

a) (20+x) km/hr b) (x-20) km/hr c) 20x km/hr d) $\frac{20}{x}$ km/hr



d) $x^2-20x-400=0$

3. The quadratic equation giving the speed of current is

a)
$$x^2+30x-200=0$$
 b) $x^2+20x-400=0$ c) $x^2+30x-400=0$

4. The speed of current is

a) 20km/hr b) 10 km/hr c)15km/hr d)25km/hr

5. Time taken by the motor boat to cover 15 km upstream is

a) 1 hour b) $1\frac{1}{2}$ hours c)2 hours d)3 hours

ANSWER KEY

VERY SHORT ANSWER TYPE QUESTIONS (1MARK)

QN NO	ANS	QN NO	ANS
1	b	6	b
2	a	7	b
3	b	8	a
4	b	9	a
5	с	10	d

ONE MARK QUESTIONS (1)

1.	-5,-2	6.	6 years ,12 years
2.	All values of a greater	7.	Other zero is $-\frac{3}{2}$
	than $\frac{3}{10}$		Z
3.	$\pm\frac{4}{3}$	8.	51/4
4.	$\frac{-9}{4}$	9.	1,2
5.	$5b^2 - 4ac = -31$	10.	13,15

SHORT ANSWER TYPE QUESTIONS (2 MARKS)

QN no	ANS	QN no	ANS	QN no	ANS	QN no	ANS
1	$p \le \frac{9}{8}$	6	$\begin{array}{l} x = 0 \\ x = 3 \end{array}$	11	p, -(p+1)	16	8,9
2	Sum is 3	7	$\pm \frac{q}{p}$	12	k = 1	17	184
3	2	8	$m \neq 1$, m = 2	13	$\frac{p \pm q}{2}$	18	$\begin{array}{c} a+b\\ = -1 \end{array}$



4	P=8	9	$x = -\frac{7}{\sqrt{3}}$,-x = $\sqrt{3}$	14	7years and 49years	19	Other root is 1
5	K=0 and 8	10	6 years	15	$x = 2 \text{ and } x$ $= \frac{1}{2}$	20	-124

SHORT ANSWER TYPE QUESTIONS (3 MARKS) & HOT QUESTIONS

	We have: $2x^2 + 4x - 8 = 0$
	Dividing by 2, we get
	$x^2 + 2x - 4 = 0$ (i)
	Comparing (i) with $ax^2 + bx + c = 0$, $a = 1, b = 2, c = -4$
	$\therefore b^2 - 4ac = (2)^2 - 4(1)(-4)$
	= 4 + 16 = 20 > 0
	Since $b^2 - 4ac > 0$, the given equation has two distinct real roots and they
1.	are given by
	$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
	$x = \frac{2a}{2a}$
	$x = -2\pm\sqrt{(2)^2-4x1x(-4)}$
	x - 2x1
	$x = \frac{-2\pm\sqrt{(2)^2 - 4x1x(-4)}}{2x1}$ $\therefore x = \frac{-2\pm\sqrt{20}}{2}$
	$\Rightarrow x = \frac{-2 \pm 2\sqrt{5}}{2} \Rightarrow x = -1 \pm \sqrt{5}$
	Thus, the required roots $x = -1 + \sqrt{5}$ and $x = -1 - \sqrt{5}$.
2.	$x = \frac{q^2}{p^2}$, $x = -1$
	$\alpha + \beta = -((-6)/2) = 3$
	$2\alpha + 5\beta = 12$
	$2(3-\beta) + 5\beta = 12$
3.	
5.	$ \begin{array}{l} \beta = 2 \\ \text{ie} \ , \alpha = 1 \end{array} $
	$\alpha.\beta = a/2$
	a = 4
	-5 is a root of the quadratic eqn. $2x^2 + px - 15 = 0$
	$\Rightarrow 2(-5)^2 + p(-5) - 15 = 0$
	$\Rightarrow 2(25) - 5p - 15 = 0$
	$\Rightarrow 50-5p-15=0$
	$\Rightarrow 35 - 5p = 0$
	$\Rightarrow 5p = 35 \Rightarrow p = 7$
4	The quadratic equation $px^2 + px + k = 0$ has equal roots.
<u>т.</u>	$\Rightarrow b^2 - 4ac = 0$
	$\Rightarrow p^2 - 4(p)(k) = 0$
	$\Rightarrow 72 - 4(7)(k) = 0$
	$\Rightarrow 49 - 28k = 0$
	$\Rightarrow 28k = 49$
	$\Rightarrow k = 49/28 = 7/4$



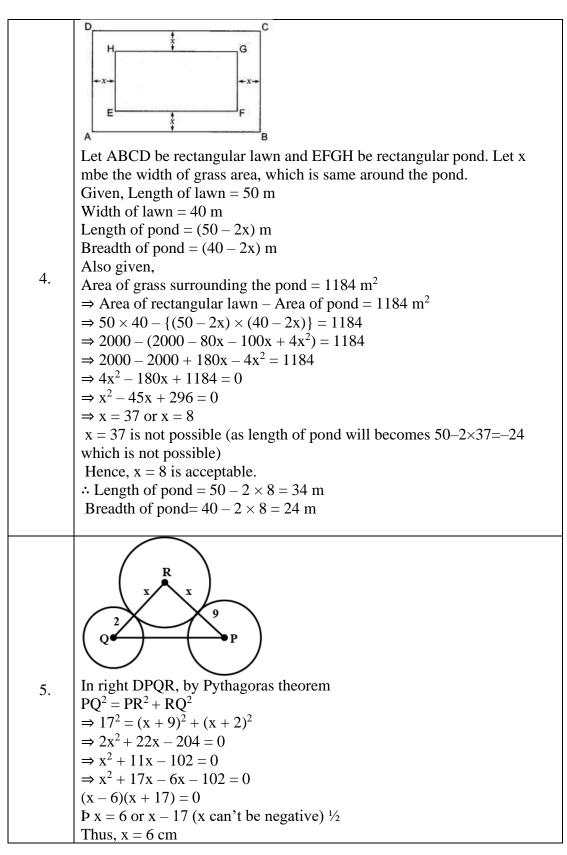
	Here for the equation $x^2+kx+64 = 0$, $D \ge 0$
	$k^2 - 4 \times 64 \ge 0$
	$k^2 \ge 256$
	$k \ge 16$ (1)
5.	Also the equation $x^2-8x+k=0$ we have , $D \ge 0$
5.	$64-4k \ge 0$
	$4k \le 64$
	$k \le 16$ (2)
	The value of satisfying both the eqns is $k = 16$
	We have, $\frac{(5x+1)+3(x+1)}{(x+1)(5x+1)} = \frac{5}{x+4}$
6.	(x+1)(5x+1) $x+417x^2-6x-11=0$
0.	
	$x = \frac{-11}{17}$,1
	Let the age of father be x years and age of son be $35 - x$ years.
	x(35-x) = 150
	$\Rightarrow x^2 - 35x + 150 = 0.1$
7.	$\Rightarrow (x - 30)(x - 5) = 0$
	$\Rightarrow (x = 50)(x = 5) = 0$ $\Rightarrow x = 30 \text{ or } x = 5 \text{ (rejected)}$
	Hence, the age of father = 30 years and the age of son = 5 years
	Let the two consecutive natural numbers be x and $x + 1$
	According to the question, $x^2 + (x + 1)^2 = 421$
	$\Rightarrow x^2 + x^2 + 2x + 1 = 421$
	$\Rightarrow x^2 + x - 210 = 0$
8.	$\Rightarrow (x+15)(x-14) = 0$
	\Rightarrow x + 15 = 0 or x - 14 = 0
	\Rightarrow x = -15 or x = 14
	Rejecting negative value, first number = 14
	and second consecutive number $= 15$
	Let the usual speed be x km/hr.
0	Then $\frac{300}{x} - \frac{300}{x+5} = 2$
9.	$x^2 + 5x - 750 = 0$
	x = -30 or x = 25
	Usual speed = 25 km/hr
	Let the speed of the steam be x km/hr.
	Then $\frac{12}{11+x} + \frac{12}{11-x} = 2\frac{3}{4}$
10.	
	$x=\pm 5$
	Speed of the stream is 5km/hr.
	Let the usual speed be x km/hr.
	Then, $\frac{1500}{x} - \frac{1500}{x+100} = \frac{1}{2}$
11.	$\begin{array}{c} x & x + 100 & 2 \\ x^2 + 100x - 300000 = 0 \end{array}$
	x = -600 or x = 500
	Usual speed of the plane = 500 km/hr
	Let the no of days taken by B to finish the work $=$ x days
	No of days taken by $A = (x-6)$
12.	ie, $\frac{1}{x-6} + \frac{1}{x} = \frac{1}{4}$
	x = 12, x = 2 (not possible) No of days taken by $B = 12$
	No of days taken by $B = 12$



	$C' = (2 + 2)(2 + 12) (- + 1)^2$
	Given, $(x^2 + y^2)(a^2 + b^2) = (ax + by)^2$ $\Rightarrow x^2a^2 + x^2b^2 + y^2a^2 + y^2b^2 = a^2x^2 + b^2y^2 + 2abxy$ $\Rightarrow x^2b^2 + y^2a^2 - 2abxy = 0$
13.	$\Rightarrow (xb - ya)^2 = 0$
	$\Rightarrow (x_0 - y_0) = 0$ $\Rightarrow x_0 = y_0$
	$\Rightarrow x/a = y/a$ $\Rightarrow x/a = y/b$
	(a) $x = -5\sqrt{3}$, $2\sqrt{3}$
	(a) $x = 3 + 3$, $2 + 3$ (b) $x = a - 2$, $x = -(a + 3)$
14.	(c) $x = 0$, 7
	(d) $x = \frac{1}{h^2}, x = \frac{-1}{a^2}$
	Let time taken by pipe A be x minutes. Then time taken by pipe $B = x + 5$
	minutes. In one minute, pipe A will fill 1/x part and in one minute, pipe B will fill
	1/(x+5) part
	Hence, pipes A + B will fill in one minute $=\frac{1}{x} + \frac{1}{x+5}$ part
15.	Now according to the question, $\frac{1}{x} + \frac{1}{x+5} = \frac{9}{100}$
	i.e; $9x^2 - 155x - 500 = 0$
	$\Rightarrow (x - 20)(9x + 25) = 0$
	\Rightarrow x = 20 or x = -25/9
	rejecting negative value, $x = 20$ minutes and $x + 5 = 25$ minutes
	Hence, pipe A will fill the tank in 20 minutes and pipe B will fill it in 25
	minutes.
	ANSWERS TO HOT QUESTIONS
	Let $y = x^{\frac{1}{3}}$
1.	$y^2+y-2=0$
	y = -2, y = 1
	ie, $x = -8$, $x = 1$
	Let the consecutive positive integers be x , $x+1$ and $x+2$.
2.	$x^{2}+(x+1)(x+2)=46$
۷.	$x = 4$ or $x = \frac{-11}{2}$ (rejected)
	Integers are 4,5,6
	Given $(x - a)(x - b) + (x - b)(x - c) + (x - 6)(x - a) = 0$
	$\Rightarrow x^2 - ax - bx + ab + x^2 - bx - cx + bc + x^2 - cx - ax + ac = 0$
	$\Rightarrow 3x^2 - 2(a+b+c)x + ab + bc + ca = 0$
	Now, for equal roots, $D = 0$
	$\Rightarrow 4(a+b+c)^2 - 12(ab+bc+ca) = 0$
3.	$\Rightarrow 4a^{2} + 4b^{2} + 4c^{2} + 8ab + 8bc + 8ca - 12ab - 12bc - 12ca = 0$
5.	$\Rightarrow 2[2a^{2} + 2b^{2} + 2c^{2} - 2ab - 2bc - 2ca] = 0$
	$\Rightarrow 2[(a^2 + b^2 - 2ab) + (b^2 + c^2 - 2bc) + (c^2 + a^2 - 2ca)] = 0$
	$\Rightarrow [(a-b)^{2} + (b-c)^{2} + (c-a)^{2}] = 0$
	$\Rightarrow a - b = 0, b - c = 0, c - a = 0$
	$\Rightarrow a = b, b = c, c = a$ $\Rightarrow a = b = a (Hence Proved)$
1	\Rightarrow a = b = c (Hence Proved)







LONG ANSWER TYPE QUESTIONS (4 MARKS)

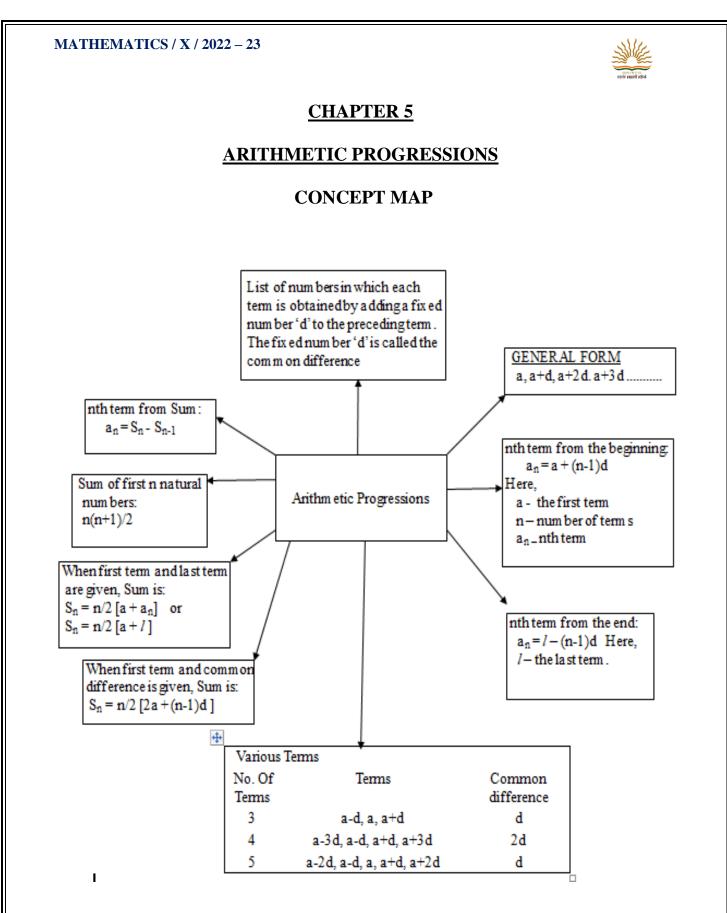
1	Rahul's age=27 years	6	Larger tap=5 hours
	Reena's age=9years		Smaller tap=8 hours



2	10m and 24m	7	$x = \frac{2a+b}{3}$ or $x = \frac{a+2b}{3}$
3	Total number of camels=36	8	$7, \frac{9}{2}$
4	Speed of train=36km/hr	9	Speed of stream=8km/hr
5	Number of persons=25	10	Area=860m ²

CASE STUDY BASED QUESTIONS

CASE STUDY 1	CASE STUDY 2	CASE STUDY 3
1. 2(x+5)km	1.b	1.(20-X)km/hr
2.c	2.30	2.(20+x) km/hr
3. 20km/hr	3.900	3.c
4.25km/hr	4.1200	4.10
5.16 hours		$5.1\frac{1}{2}$ hours



MULTIPLE CHOICE QUESTIONS (1 MARK)

SECTION A

Q1. The common difference of an AP whose n^{th} term is 3n+7

(a) 2

(b) 3



	(c) 4	(d) 5
Q2.	The sum of first n natural numbers is	
	(a) $\frac{n}{2}$	(c) $\frac{n(n+1)}{2}$
	(b) $\frac{n+1}{2}$	2
	$(0) \frac{1}{2}$	(d) $\frac{n(n+1)(n+2)}{2}$
~ •	(e)	
Q3.	The next term of the AP: $\sqrt{8}$, $\sqrt{18}$, $\sqrt{32}$ is	$\langle \rangle 2 2$
	(a) $5\sqrt{2}$ (b) $5\sqrt{3}$	(c) $3\sqrt{3}$ (d) $3\sqrt{5}$
04		(u) 3 v 3
Q4.	The list of numbers -10, -6, -2, 2,is (a) an AP with $d = -16$	
	(b) an AP with $d = 4$	
	(c) c)an AP with $d = -4$	
	(d) not an AP	
Q5.	The 27 th positive odd number is:	
	(a) 50	(c) 52
	(b) 51	(d) 53
Q6.	The common difference of an AP is 5, then the value of	
	(a) 5 (b) 20	(c) 25
07	(b) 20 A man receives Ps. 60 for the first week and Ps. 3 mor	(d) 30
Q7.	A man receives Rs. 60 for the first week and Rs. 3 more week. How much does he earn by the 20th week?	e each week man me preceding
	(a) Rs. 1760	(c) Rs. 1780
	(b) Rs. 1770	(d) Rs. 1790
Q8.	If the first term of an AP is p and the common difference	
	(a) $p + 9q$	(c) $p + 10q$
00	(b) $p + q$	(d) 9p+q
Q9.	If an AP has $a_1=1$, $a_n=20$ and $S_n=399$, then the value of $a_1=20$	
	(a) 20 (b) 32	(c) 38 (d) 40
010	Two APs have the same common difference. The first t	
Q10.	that of the other is -8 . Then the difference between the	
	(a) -1	(c) 7
	(b) – 8	(d) –9

VERY SHORT ANSWER QUESTIONS(1 MARK)

- Q11. For what value of k: 2k, k + 10 and 3k + 2 are in AP?
- Q12. The first, second and last terms of an AP are respectively 4, 7 and 31. How many terms are there in the given AP?
- Q13. Write first four terms of the AP, when first term is 1.25 and common difference is -0.25.

Q14. Find the common difference of an AP in which $a_{18} - a_{14} = 32$.



- Q15. If the nth term of an AP is 2n+1, then find the sum of its first three terms.
- Q16. Find the common difference of the AP $\frac{1}{p}, \frac{1-p}{p}, \frac{1-2p}{p}, \dots$
- Q17. Find the 9th term from the end (towards the first term) of the AP 5, 9, 13, ..., 185.
- Q18. Find the sum of all natural numbers from 1 to 100.
- Q19. In an AP, if the common difference is -4 and the seventh term is 4, then find the first term.
- Q20. Find the missing terms in the given AP 2, -----, 26 -----

SHORT ANSWER QUESTIONS (2Marks questions)

SECTION - B

- Q1. How many terms of the AP 27, 24, 21, ... should be taken so that their sum is zero.
- Q2. Three numbers are in AP and their sum is 24. Find the middle term.
- Q3. Check whether -150 is a term of the AP: 11,8, 5, 2, ...
- Q4. Find the middle term of the AP -11, -7, -3, ..., 45.
- Q5. How many two-digit numbers are divisible by 3?
- Q6. Find the sum: 34+ 32+30+.....+10
- Q7. Which term of the AP 3,15, 27, 39, ... is 132 more than its 54 th term?
- Q8. Find the number of terms of an AP 5, 9,13, ..., 185.
- Q9. Find the sum of all odd numbers between 10 and 200.
- Q10. If the sum of first n terms of an AP is n^2 find the 5th term.
- Q11. Which term of the AP. 20, 17, 14,; is the first negative term?
- Q12. If the sum of first m terms of an AP is $am^2 + bm$, find the common difference.
- Q13. Find the sum of first 8 multiples of 3.
- Q14. Find the number of natural numbers between 101 and 999 which are divisible by both 2 and 5
- Q15. The fourth term of an AP is 11 and the eleventh term is 25. Determine the first term and common difference.
- Q16. If an AP has 8 as the first term, -5 as the common difference and its first 3 terms are 8, A, B, then find A+B.
- Q17. In an AP a=15, d=-3, $a_n=0$, then find the value of n.
- Q18. The sum of first n terms of an AP is given by $S_n = 2n^2 + n$. Then find its nth term .
- Q19. The 4th term of an AP is zero. Prove that 25th term is three times its 11th term.
- Q20. Find the nth term of the AP $\frac{1}{m}$, $\frac{1+m}{m}$, $\frac{1+2m}{m}$,?



SHORT ANSWER TYPE QUESTION (3 Marks Questions) SECTION - C

- Q1. If sum of the 3rd and the 8th terms of an AP is 7 and the sum of the 7th and the 14th terms is –3, find the 10th term.
- Q2. Find the sum of all 3-digit natural numbers which are multiples of 11.
- Q3. In an AP, if $S_n = 3n^2 + 5n$ and $a_k = 164$, find the value of k.
- Q4. The pth term of an AP is $\frac{1}{7}$ (2p-1). Find the sum of its first n terms.
- Q5. How many terms of the AP: 9,17, 25.... must be taken to get a sum of 636?
- Q6. If mth term of an AP is $\frac{1}{n}$ and nth term is $\frac{1}{m}$. Show that (mn)th term of this AP is 1.
- Q7. The sum of the first 9 terms of an AP is 171 and the sum of of its first 24 terms is 996. Find the first term and the common difference.
- Q8. If the sum of first m terms of an A.P. is the same as the sum of its first n terms, then show that the sum of its first (m + n) terms is zero.
- Q9. For what value of n, are the nth terms of two APs: 63, 65, 67, . . . and 3, 10, 17, . . . equal?
- Q10. If the sum of the first 14 terms of an AP is 1050 and its first term is 10, find the 20th term.
- Q11. In an AP, ratio of 4th term and 9th term is 1:3, find the ratio of 12th and 5th term.
- Q12. The 14th term of an A.P. is twice its 8th term. If the 6th term is -8, then find the sum of its first 20 terms.
- Q13. Find the sum of n terms of the series: $(4 \frac{1}{n}) + (4 \frac{2}{n}) + (4 \frac{3}{n}) + \dots$
- Q14. If the 10th term of an A.P. is 52 and the 17th term is 20 more than the 13th term, find A.P.
- Q15. The 5th term of an AP is 20 and the sum of its 7th and 11th terms is 64. Find the common difference of the AP

CASE STUDY BASED QUESTIONS (4 marks questions)

Q1. CASE STUDY QUESTION 1:

India is competitive manufacturing location due to the low cost of manpower and strong technical and engineering capabilities contributing to higher quality production runs. The production of TV sets in a factory increases uniformly by a fixed number every year. It produced 16000 sets in 6th year and 22600 in 9th year.

Based on the above information, answer the following questions:

- i. Find the production during the first year.
- ii. In which year, the production is 29,200.

Q2. CASE STUDY QUESTION 2:



- Your friend Veer wants to participate in a 200m race. He can currently run that distance in 51 seconds and with each day of practice it takes him 2 seconds less. He wants to do in 31 seconds.
- Q1. What is the minimum number of days he needs to practice till his goal is achieved?
- Q2. If nth term of an AP is given by an = 2n + 3 then find the common difference of the AP. O3 CASE STUDY OUESTION 3.

Q3. CASE STUDY QUESTION 3:

- Your elder brother wants to buy a car and plans to take loan from a bank for his car. He repays his total loan of Rs 1,18,000 by paying every month starting with the first instalment of Rs 1000. If he increases the instalment by Rs 100 every month, answer the following:
 - i. Find the amount paid by him in 30th instalment.
 - ii. Find the total amount paid by him after 30 instalments.

LONG ANSWER QUESTIONS (4 MARKS)

SECTION - D

- Q1. The eighth term of an AP is half its second term and the eleventh term exceeds one third of its fourth term by 1. Find the 15th term.
- Q2. An AP consists of 37 terms. The sum of the three middle most terms is 225 and the sum of the last three is 429. Find the AP.
- Q3. In an AP if $S_5+S_7=167$ and $S_{10}=235$, find the AP, where Sn denotes the sum of the first n terms.
- Q4. The sum of the first n terms of an AP whose first term is 8 and the common difference is 20 is equal to the sum of first 2n terms of another AP whose first term is 30 and the common difference is 8. Find n
- Q5. Find an AP whose sum of the first three terms is 21 and the sum of their square is 155.
- Q6. The sum of the third and the seventh terms of an AP is 6 and their product is 8. Find the sum of first sixteen terms of the AP
- Q7. Find the 60th term of the AP 8, 10, 12, ..., if it has a total of 60 terms and hence find the sum of its last 10 terms.

Qn no	Answer	Qn no	Answer
1	3	6	25
2	$\frac{n(n+!)}{2}$	7	Rs. 1770
3	$5\sqrt{2}$	8	p+9q
4	an AP with d=4	9	38
5	53	10	7

ANSWER KEY

MULTIPLE CHOICE QUESTIONS (1mark questions)



11	$k+10=\frac{2k+3k+2}{2}=k+10=\frac{5k+2}{2}$ Also by cross multiplying we get 2(k+10)=5k+2
	2k+20=5k+2, $18=3k$, $k=6$
12	$a_1=4$, $a_2=7$, $a_1=31$, $d=a_2-a_1=7-4=3$
	31=4+(n-1)3,(n-1)3=27,n-1=9,n=10
13	a, a+d, a+2d, a+3d= 1.25, 1, 0.75, 0.50
14	$a_{18} - a_{14} = 32., a+17d-(a+13d)=32, 4d=32, d=32 \div 4=8$
15	$a_n = 2n+1, a_1 = 2x_1+1=3, a_3 = 2x_3+1=7, S_3 = \frac{3}{2}(3+7) = 15$
16	$d = a_2 - a_1 = \frac{1 - p}{p} - \frac{1}{p} = \frac{1 - p - 1}{p} = \frac{-p}{p} = -1$
17	nth term from the end = $l - (n-1)d$, where l is the last term.
	9^{th} term from the end =185-(9-1)4, 185-32=153
18	$\frac{n(n+!)}{2} = \frac{100(100+!)}{2} = 5050$
19	$a_7 = 4, d = -4, a + 6d = 4, a + 6x - 4 = 4, a - 24 = 4, a = 28.$
20	$a_{2=} \frac{a_{1+a_{3}}}{2}$, $a_{2=} \frac{2+26}{2} = 14$, $d=a_{2-}a_{1}=12$, $a_{4=}a_{3}+d = 26+12=38$

SHORT ANSWER QUESTIONS (2 marks questions)

1	The first term (a) = 27, The sum of first n terms (Sn) = 0 Common difference of the A.P. (d) = a2 - a1 = 24 - 27 = -3. On substituting the values in Sn, we get 0 = $\frac{n}{2}[2(27) + (n-1)(-3)]$, 0 = (n)[54 + (n-1)(-3)], 0 = (n)[54 - 3n + 3] \Rightarrow
	$0 = n [57 - 3n]$ Further we have, $n = 0$ Or, $57 - 3n = 0 \Longrightarrow 3n = 57 \Longrightarrow n = \frac{57}{3} = 19$.
	The number of terms cannot be zero. Hence n=19
2	Let the three numbers of the AP be a-d, a, a+d. So a-d +a+a+d= $24 \Longrightarrow$
	$3a=24, a=\frac{24}{3}=8$. Hence the middle term =8.
3	11, 8, 5, 2,150, $a = 11$, $d = 8$ - 11 = -3, $an = -150$, $11 + (n - 1)(-3) = -150$, $11 - 100$
	$3n + 3 = -150$, $-3n + 14 = -150$, $-3n = -150 - 14$, $-3n = -164$, $3n = 164 \therefore n = \frac{164}{3}$,
	Here value of 'n' is not a positive integer. Hence -150 is not a term of the given AP
4	Given AP is -11,-7,-3,,45
	Here $a = -11$, $d = -711 = -7 + 11 = 4$ and last term $1 = 45$
	45 = (-11) + (n - 1)4, $56 = (n - 1)4$, $n - 1 = 14$, Therefore, $n = 15$
	That is there are 15 terms. Hence 8th term is the middle most term of the given AP
	$a_8 = a + 7d = (-11) + 7(4) = 17$. Thus the middle term is 17
5	The Required A.P = 12, 15, 18,
	Common difference = 3, nth term = $a+(n-1)d$, Putting the values in the formula:=>
	$99 = 12 + (n-1)3$, $99 - 12 = 3(n-1)$, $87 = 3(n-1)$, $\frac{87}{3} = n-1$, $29 = n-1$, $29 + 1 = n$, $n = 30$



r	
6	Given, $34 + 32 + 30 + + 10$, first term, $a = 34$, $d = a_2 - a_1 = 32 - 34 = -2$, Let 10 be
	the n^{th} term of this A.P., $a_n = a + (n-1)d$, $10 = 34 + (n-1)(-2)$, $-24 = (n-1)(-2)$,
	$12 = n - 1, n = 13, S_n = \frac{n}{2}(a + l), l = 10, S_n = \frac{n}{2}(34 + 10) = \frac{13}{2}x44 = 286$
7	$a_1 = 3, a_{2=} 15, d = 15 - 3 = 12, 54^{th}$ term of the AP is $a_{54} = a + (54 - 1)d = 3 + 53 \times 12$ = 639, Let n th term of AP be 132 more than 54 th term ,We get, 132 + 639 = 771, $a_n = 771, 771 = 3 + (n - 1)12, 768 = (n - 1)12, (n - 1) = 64, n = 65$, Therefore, the 65 th term will be 132 more than the 54 th term
8	$a_1=5, d=9-5=4, a_n=185, 185=5+(n-1)4, 185=5+4n-4, 185=1+4n, 185-1=16$
	4n, 184 = 4n, n = 184/4 = 46
9	Odd numbers between 10 and 200 are $11,13,15199$. $a_1 = 11$, Last term $l = 199$, d
1	= 2, an $= a + (n-1) d$, 199 $= 11 + (n-1) 2$, 199 $- 11 = (n-1) 2$, 188 $= (n-1) 2$,
	94 = n - 1,95 = n
	Sum of n terms = $\frac{n}{2}(a+1)$, = $\frac{95}{2}(11+199)$ = 9975
10	Given $S_n = n^2$, we know, $a_n = S_n - S_{(n-1)}$, $a_5 = S_5 - S_{(5-1)} = S_5 - S_4 = 5^2 - 4^2 = 25 - 16 = 9$
11	$a_n < 0, 20 + (n-1)-3 < 0, 20-3n+3 < 0, 23-3n < 0, 23 < 3n, \frac{23}{3} < n, 7.6 < n.$ Next natural
11	number greater than 7.6 is 8.Hence 8 th term is the first negative number.
12	$\begin{split} S_m &= am^2 + bm, S_1 = a + b = a_1, S_2 = 4a + 2b = a_1 + a_2 \\ a_2 &= S_2 - S_{1=} 4a + 2b - (a + b) = 3a + b \ , d = a_2 - a_1 = 3a + b - (a + b) = 2a \end{split}$
13	First 8 multiples of 3 are 3, 6, 9, 12, 15, 18, 21, 24 These numbers are in A.P. where a = 3, d = 3 and n = 8, $a_n=24$, $S_n=\frac{n}{2}(a_1+a_n)$, $S_8=\frac{8}{2}(3+24)=4x27=108$
14	Since, the number is divisible by both 2 and 5, means it must be divisible by 10 .AP = 110, 120, 130,, 990, a = 110, d = 10, nth term of the AP = 990 a+(n-1)d=990, 110+(n-1)10=990, (n-1)10=990-110, (n-1)= 880/10, n-1=88, n=88+1, n=89
15	a + 3d = 11(1) a + 10d = 25(2)Subtracting equation (1) from equation (2)
	a + 10d - (a + 3d) = 25 - 11, $7d = 14$, $d = 2$, Putting value of $d=2$ in the equation 2,
	a + 10x2 = 25, a + 20 = 25, a = 25 - 20, a = 5
16	The first term of the AP =8,Common difference $d = -5$ Given that A is the second term. So, $A = 8 + (-5) = 8, 5 = 3$
	Given that A is the second term, So, $A = 8+(-5) = 8-5 = 3$ Given that B is the third term So, $B = 3+(-5) = 3-5 = -2$
	So $(A+B) = 3+(-2) = 3-2 = 1$



First term (a) =15,Common difference (d) = -3,Last term(an) = 0, $0 = 15 + (n - 1)-3$ -15 = -3n + 3, -15 - 3 = -3n, -18 = -3n, n=6
The sum of the first n terms of an A.P. is given by $S_n = 2n^2 + n$, At $n=1$, $S_1 = 2x1^2+1=3$, At $n=2$, $S_2 = 2x2^2+2=10$, Since $a_1=S_1$, $S_2=a_1+a_2$, So, $a_1=3$, $a_1+a_2=10$, $\Rightarrow 3+a_2=10$ so $a_2=7$, $d=7-3=4$, $a_n=3+(n-1)4=4n-1$
$a + 3d = 0$ or $a = -3d(1)$, $a_{25} = a + 24d = -3d + 24d = 21d(2)$ $a_{11} = a + 10d = -3d + 24d = 21d(2)$
$-3d + 10d = 7d \dots(3)$ From (2) and (3), we have $21d=3x7d$, $a_{25} = 3 \times a_{11}$ Hence proved.
$d = \frac{1+m}{m} - \frac{1}{m} = 1$, $a_n = \frac{1}{m} + (n-1)l = \frac{1}{m} + n - 1 = \frac{1+m(n-1)}{m}$
HORT ANSWER TYPE QUESTIONS (3 MARKS QUESTIONS)
Let the first term, common difference of an AP are a and d, respectively. According to the question, $a_3 + a_8 = 7$ and $a_7 + a_{14} = -3$ $\Rightarrow a + (3-1)d + a + (8-1)d=7$ [: $a_1=a + (n-1)d$] And $a + (7 - 1)d + a + (14 - 1)d = - 3$ a + 2d + a + 7d = 7 And $a + 6d + a + 13d = -3$ $2a + 9d = 7 \dots (i)$ And $2a + 19d = -3 \dots (ii)$ On subtracting eq. (i) from eq.(ii), we get; $10d = -10 \Rightarrow d = -1$ 2a + 9(-1) = 7 $\Rightarrow 2a - 9 = 7$ $\Rightarrow 2a = 16 \Rightarrow a = 8$ $\therefore a_{10} = a + (10-1)d$ = 8 + 9(-1) = 8 - 9 = -1
First three-digit number which is a multiple of 11 is 110 Last three-digit number which is a multiple of 11 is 990 the sequence of three-digit numbers which are multiples of 11 are 110, 121, 132, , 990. Clearly, it is an A.P. $\therefore a=110$ $a_n = 990$ $d = 11$ $a_n = a + (n-1)d$, 990=110+(n-1)11 $\frac{880}{11} = n - 1$ 80 = n - 1, $n = 81\therefore sum of all terms of A.P is given byS_n = \frac{n}{2} [a_1 + a_n]$



	$=\frac{81}{2}[110+990]$
	$=\frac{81}{2} \times 1100$
	$= 81 \times 550$
	= 44550
	Hence, the required sum is 44550.
3	$S_n = 3n^2 + 5n$
	$S_1 = 3 \times 1^2 + 5 \times 1 = 8 = a_1$ $S_2 = 3 \times 2^2 + 5 \times 2 = 22 = a_1 + a_2$
	$a_2 = 3 \times 2^{-1} + 3 \times 2^{-2} - 22^{-1} + 42^{-1}$ $a_2 = 22 - 8 = 14 \implies a+d, d = 14-8=6$
4	$a_{k} = 164 \implies 8 + (k-1)6 = 164, \ k=27$ $a_{p} = \frac{(2p-1)}{7}, \ a_{1} = \frac{(2x1-1)}{7} = \frac{1}{7}, \ a_{2} = \frac{(2x2-1)}{7} = \frac{3}{7}, \ d = \frac{3}{7} - \frac{1}{7} = \frac{2}{7}, \ a = \text{First Term} = \frac{1}{7}$
	nth term = $a + (n-1)d = \frac{1}{7} + (n-1)\frac{2}{7}$
	$=\frac{1+2n-2}{7}=\frac{2n-1}{7}$
	Sum of n terms $=\frac{n}{2}$ (First term + nth term)
	$= \frac{n}{2} \left(\frac{1}{7} + \frac{2n-1}{7}\right) = \frac{n}{2} x \frac{1+2n-1}{7} = \frac{n}{2} x \frac{2n}{7} = \frac{n^2}{7}$ Given that first term, a = 9, Common difference, d = 17 - 9 = 8,Sum up to nth
5	
	terms, $S_n = 636$ where $S_n = \frac{n}{2}[2a + (n - 1)d], \ 636 = \frac{n}{2}[2 \times 9 + (n - 1)8]$
	$636 = \frac{n}{2}[18 + 8n - 8], \ 636 = \frac{n}{2}[10 + 8n], \ 636 = n[5 + 4n], \ 636 = 5n + 4n^2,$
	$4n^2 + 5n - 636 = 0, 4n^2 + 53n - 48n - 636 = 0, n (4n + 53) - 12 (4n + 53) = 0$
	(4n + 53)(n - 12) = 0
	Either $4n + 53 = 0$ or $n - 12 = 0$ n = -53/4 or $n = 12$
	n cannot be $-53/4$ because the number of terms can neither be negative nor
	fractional, therefore, $n = 12$
6	Given that, mth term= $\frac{1}{n}$ and nth term=. $\frac{1}{n}$
	then , let a and d be the first term and the common difference of the A.P.
	so $a+(m-1)d=\frac{1}{n}$ (1) and $a+(n-1)d=\frac{1}{m}$ (2).
	subtracting equation (2) from(1) we get, m
	$md-d-nd+d=\frac{1}{2}-\frac{1}{2}$
	$=>d(m-n)=$ $\frac{n-m}{nm}$
	$=>d=\frac{1}{nm}$
	again if we put this value in equation (1) or (2) we get,
	$a+(m-1)\frac{1}{nm}=\frac{1}{n}$, $a=\frac{1}{n}-\frac{1}{nm}(m-1)=\frac{1}{n}-\frac{m}{nm}-(-\frac{1}{nm})=\frac{1}{nm}$
	then, the mn th term of the AP
	$a+(mn-1)d=\frac{1}{nm} +(mn-1)\frac{1}{nm} = \frac{mn}{mn} = 1$
7	hence proved.
7	S ₉ =171, S ₂₄ = 996, $\frac{9}{2}$ [2a + (9-1) d]=171(.1), $\frac{24}{2}$ [2a + (24-1) d]=996(.2)



	$2a+8d = \frac{171x^2}{9} = 2a+8d = 38(3)$ $2a+23d = \frac{996x^2}{24} = 2a+23d = 83(4)$
	Solving (3) and (4) 23d-8d= 83-38, $15d=45$, $d=3$. Put d=3 in equation (3)
	2a + 8x3 = 38, 2a = 38 - 24 = 14, a = 7.
8	Let a be the first term and d be the common difference of the given AP. Then,
	$\mathbf{S}_{\mathbf{m}} = \mathbf{S}_{\mathbf{n}}$
	$\Rightarrow \frac{m}{2} [2a + (m-1)d] = \frac{n}{2} [2a + (n-1)d]$
	$\Rightarrow 2ma + d(m^2 - m) = 2an + d(n^2 - n)$
	$\Rightarrow 2ma - 2na + d(m^2 - m) - d(n^2 - n) = 0$
	$\Rightarrow 2a(m-n) + d(m^2-m) - d(n^2-n) = 0$
	$\Rightarrow 2a(m-n) + d(m^2-n^2) - d(m-n) = 0$
	2a(m-n) + d(m+n)(m-n) - d(m-n) = 0
	$\Rightarrow 2a(m-n) + d(m-n)(m+n-1) = 0$
	$(m-n) 2a+(m+n-1)d=0$ [: $m-n \neq 0$]
	2a+(m+n-1)d=0(i)
	$\therefore S_{m+n} = \frac{m+n}{2} [2a + (m+n-1)d]$
	$S_{m+n} = \frac{m+n}{2} \times 0 = 0$ [from Eq. (i)]
	Hence proved.
9	Let a, d, and A, D be the first term and common different of the 2 A.P.s
/	respectively.
	Here, $a = 63, d = 2$
	A = 3, D = 7
	Given, $a_n = A_n$
	$\Rightarrow a + (n - 1) d = A + (n - 1) D$
	$\Rightarrow 63 + (n - 1) 2 = 3 + (n - 1) 7$
	$\Rightarrow 63 + 2n - 2 = 3 + 7n - 7$
	$\Rightarrow 61 + 2n = 7n - 4$
	$\Rightarrow 5n = 65$
	\Rightarrow n = 13
	\therefore When n is 13, the nth terms are equal
10	i.e., $a_{13} = A_{13}$
10	Here, $S_{14} = 1050$, $n = 14$, $a = 10$.
	We know that $Sn = \frac{n}{2} [2a + (n-1)d]$
	Substituting the values we have,
	$\Rightarrow 1050 = \frac{14}{2}[20 + 13d] \Rightarrow 1050 = 140 + 91 d$
	$\Rightarrow 910 = 91d$
	\Rightarrow d = 10, Therefore, a ₂₀ = 10 + (20 - 1) × 10 = 200
	i.e. 20 th term is 200.
11	a4 1
11	$\frac{a4}{a9} = \frac{1}{3}$
	$\frac{a^3}{a+3d} = \frac{1}{3}$, $(a+3d)3 = (a+8d)$
	a+8d 3 $(a+8d)3a+9d = a+8d$
	2a+d=0
	$d = -2a \dots (1)$
	$\frac{a^{2}}{a5} = \frac{a+11d}{a+4d} = \frac{a+11x-2a}{a+4x-2a} = \frac{a-22a}{a-8a} = \frac{-21a}{-7a} = \frac{3}{1} = 3:1$
10	
12	Let the first term is a and common difference is d



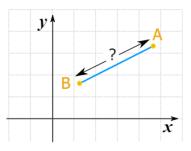
	Here, $a_{14} = 2 a_8$
	Or, $a+13 d = 2(a+7d)$
	a + 13d = 2(a + 7d) a + 13d = 2a + 14d
	-a - d = 0, a = -d(1)
	again $a_6 = -8$
	or $a + 5d = -8$ (2)
	solving eq. (1) and (2) we get
	a = 2, d = -2
	a = 2, a = 2 $S_{20} = 10 (4 + (-38))$
	= 10(4-38)
	= -340
13	Let sum of first n terms be Sn.
15	
	: $\operatorname{Sn} = (4 - \frac{1}{n}) + (4 - \frac{2}{n}) + (4 - \frac{3}{n}) + \dots + up$ to n terms
	= $(4 + 4 + 4 + 4 + 4 +, up to n terms) + (-1/n - 2/n - 3/n, up to n terms)$
	= 4 (1+1+1+1 up to n terms) - $\frac{1}{n}$ (1 + 2 + 3 + 4 up to n terms)
	$=4 n - \frac{1}{n} \times \frac{n(n+1)}{2}$
	$=4n-\frac{n+1}{2}$
	$= \frac{8n - (n + 1)}{2}$ (taking L.C.M)
	$=\frac{7n-1}{2}$
	Therefore, the sum of n terms is $\frac{7n-1}{2}$.
14	2
14	Given, $a_{10} = 52$
	$\Rightarrow a+9d=52$ (1)
	also, $a_{17} = 20 + a_{13}$
	$\Rightarrow a + 16d = 20 + a + 12d$
	$\Rightarrow 16d - 12d = 20$
	\Rightarrow 4d = 20
	$\Rightarrow d=5$
	putting the value of d in eq. (1), we get,
	$\Rightarrow a+9(5)=52$
	\Rightarrow a+45=52
	$\Rightarrow a=7$
	hence, the required AP is 7,12,17,
15	5th term is 20., $a+4d = 20$ (1)
	7th term + 11th term is 64, $a+6d + a + 10d = 64$., $2a + 16d = 64$., $a+8d = 32$ (2)
	solving equations (1) and (2).
	4d = 12, d = 3
L	



<u>UNIT 3</u> <u>COORDINATE GEOMETRY</u>

IMPORTANT FORMULAS & CONCEPTS

DISTANCE FORMULA



Let $A(x_1,y_1)$ and $B(x_2,y_2)$ be two points in the Cartesian plane.

The distance between any two points $A(x_1, y_1)$ and $B(x_2, y_2)$ is given by

$$AB = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

or $AB = \sqrt{(\text{difference of abscissae})^2 + (\text{difference of ordinates})^2}$

Problems based on distance formula

- To show that a given figure is a
- **Parallelogram** prove that the opposite sides are equal
- **Rectangle** prove that the opposite sides are equal and the diagonals are equal.
- **Parallelogram but not rectangle** prove that the opposite sides are equal and the diagonals are not equal.
- **Rhombus** prove that the four sides are equal
- **Square** prove that the four sides are equal and the diagonals are equal.
- **Rhombus but not square** prove that the four sides are equal and the diagonals are not equal.
- **Isosceles triangle** prove any two sides are equal.
- Equilateral triangle prove that all three sides are equal.
- **Right triangle** prove that sides of triangle satisfy Pythagoras theorem.

DISTANCE OF A POINT P(X,Y) FROM ORIGIN.

Since coordinate of origin is (0,0), Then by applying distance formula,

distance from P(x,y) is OP = $\sqrt{x^2 + y^2}$



COLLINEAR POINTS:

A given number of points are said to be collinear if they lie on the same line. To prove that three points A ,B and C are collinear (using distance formula), we need to prove that sum of any two of the distances AB, BC and AC is equal to the third distance.

SECTION FORMULA

The coordinates of the point P (x, y) which divides the line segment joining the points A(x_1 , y_1) and B(x_2 , y_2), internally, in the ratio m:n are

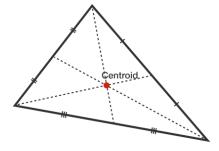


MID POINT FORMULA

If point P(x,y) divides the line segment joining the points A(x_1 , y_1) and B(x_2 , y_2), internally, in the ratio 1:1 (*i.e.* P is the mid point of AB) Then coordinates of point P are given by, P(x, y) = $\frac{x_1+x_2}{2}$, $\frac{y_1+y_2}{2}$

CENTROID OF TRIANGLE

The centroid of a triangle is the center of the triangle. It is referred to as the point of concurrency of medians of a triangle.



The coordinates of the vertices of a triangle are A (x_1 , y_1), B (x_2 , y_2) and C (x_3 , y_3), then centroid C (x, y) of given triangle ABC can be find out using,

$$C(x,y) = (\frac{x_1 + x_2 + x_3}{3}, \frac{y_1 + y_2 + y_3}{3})$$



MULTIPLE CHOICE QUESTIONS

Q1. The distance of the point P (-6, 8) from the	
(a) 14	(c) 8
(b) 6	(d) 10
Q2. If (a, b) is the mid-point of the line segmen	It joining the points A (10, -6) and B $(k, 4)$
and $a - 2b = 18$, the value of k is:	
(a) 40	(c) 4
(b) 22	(d) 36
Q3. The distance between the points ($a \cos \theta$ +	$b \sin \theta$, 0) and (0, $a \sin \theta - b \cos \theta$), is :
(a) $\sqrt{a^2 - b^2}$	(c) $a^2 - b^2$
(b) $a^2 + b^2$	(d) $\sqrt{a^2 + b^2}$
Q4. If the point P $(k, 0)$ divides the line segmen	nt joining the points A (2, -2) and B (-7, 4) in
the ratio 1:2, then the value of k is :	
(a) 1	(c) -1
(b) 2	(d) -2
Q5. If the point P $(6, 2)$ divides the line segmen	nt joining A (6, 5) and B (4, y) in the ratio 3 :
1, then the value of <i>y</i> is :	
(a) 4	(c) 1
(b) 2	(d) 3
Q6. Distance between two points (3, 2) and (6,	6) is:
(a) 5	(c) 2
(b) 3	(d) 8
Q7. The line segment joining the points P (-3, 2	2) and Q $(5, 7)$ is divided by the <i>y</i> - axis in the
ratio:	
(a) 3:1	(c) 3:4
(b) 3 : 2	(d) 3 : 5
Q8. The point P on x - axis is equidistant from t	
(a) (2, 2)	(c) (2, 0)
(b) (0, 2)	(d) (3, 2)
Q9. The mid-point of the line segment joining (2)	-
(a) (-4, -6)	(b) (-4, 2)



(c) $(2, 6)$	(d) (6, -2)
--------------	-------------

Q10. Point A (-1, y) and B (5, 7) lie on a circle with centre O (2, -3y). The values of y are:

- (a) 1, -7 (c) -2, -7
- (b) -2, 7 (d) -1, 7
- Q11. Find the perpendicular distance of A (5, 12) from the *y* -axis.
- Q12. Find the value of *y* for which the distance between the points (2, 3) and (10,*y*) is 10 units.
- Q13. To locate a point Q on line segment AB such that $BQ = \frac{5}{7} \times AB$. What is the ratio of line segment in which AB is divided?
- Q14. Find the distance of the point (-4, -7) from the *y*-axis.
- Q15. If (2, *p*) is the midpoint of the line segment joining the points *A* (6, -5) and *B* (-2, 11), find the value of *p*.
- Q16. If the centre and radius of circle is (3, 4) and 7 units respectively, then what is the position of the point *AB* with respect to circle.
- Q17. If the distance between the points (4, *k*) and (1, 0) is 5, then what will be the possible values of *k*?
- Q18. *ABCD* is a rectangle whose three vertices are *B* (4, 0), *C* (4, 3) and *D* (0, 3). Find the length of one of its diagonals
- Q19. A (5,1), B (1,5) and C (-3, -1) are the vertices of $\triangle ABC$. Find the length of median AD.
- Q20. Find the perimeter of a triangle with vertices (0,4), (0,0) and (3,0).

SHORT ANSWER TYPE QUESTION (2 MARKS) SECTION – B

- Q1. Find the point on the x-axis which is equidistant from the points (2, -5) and (-2, 9)
- Q2. Find the distance of the point P(2, 3) from the x-axis.
- Q3. Find the ratio in which the point (-3, *k*) divides the line-segment joining the points (-5, 4) and (-2, 3). Also find the value of *k*.
- Q4. If A (5,2), B (2, -2) and C (-2, t) are the vertices of a right-angled triangle with $\angle B = 90^{\circ}$, then find the value of t.
- Q5. In what ratio does the point *P* (2, -5) divide the line segment joining A (-3, 5) and B (4, -9).
- Q6. If the point P(x, y) is equidistant from the points A(a + b, b a) and B(a b, a + b), then prove that bx = ay.



- Q7. If the mid-point of the line segment joining A $(\frac{x}{2}, \frac{y+1}{2})$ and B (x + 1, y 3) is C (5, -2), find x, y.
- Q8. Find a point on y-axis which is equidistant from A (6,5) and B (-4, 3).
- Q9. If *A* and *B* are (-2, -2) and (2, -4), respectively, find the coordinates of *P* such that AB = 5AB and *P* lies on the line segment *AB*.
- Q10. Find the third vertex of a Δ , if two of its vertices are at (1, 2) and (3, 5) and the centroid at the origin.
- Q11. In a seating arrangement of desks in a classroom, three students are seated at A (3, 1), B (6,4) and C (8, 6) respectively. Are they seated in line?
- Q12. Name the type of triangle formed by the points A (-5, 6), B (-4, -2) and C (7, 5).
- Q13. Find a relation between x and y such that the point (x, y) is equidistant from the points (7, 1) and (3, 5).
- Q14. Find the mid-point of side BC of $\triangle ABC$, with A(1, -4) and the mid-points of the sides through A being (2, -1) and (0, -1)
- Q15. The coordinates of the points P and Q are respectively (4, -3) and (-1, 7). Find the abscissa of a point R on the line segment PQ such that PRPQ = 35.
- Q16. Write the coordinates of a point on x-axis which is equidistant from the points (-3, 4) and (2, 5).
- Q17. Find the ratio in which the line segment joining the points P (3, -6) and Q (5,3) is divided by the *x* -axis.
- Q18. Check whether (5, -2), (6, 4) and (7, -2) are the vertices of an isosceles triangle.
- Q19. Find the area of a rhombus if its vertices (3, 0), (4, 5), (-1, 4) and (-2, -1) are taken in order.
- Q20. Find the coordinates of a point A, where AB is the diameter of a circle whose centre is (2, -3) and B is (1,4).

<u>SHORT ANSWER TYPE QUESTION (3 MARKS)</u> SECTION – C

- Q1. Determine if the points (1, 5), (2, 3) and (-2, -11) are collinear.
- Q2. Find the values of *y* for which the distance between the points P (2, -3) and Q (10, y) is 10 units.
- Q3. Find the area of a rhombus if its vertices are (3, 0), (4, 5), (-1, 4) and (-2, -1) taken in order.



- Q4. If A (-2,1), B (*a*, 0), C (4, *b*) and D (1, 2) are the vertices of a parallelogram *ABCD*, find the values of *a* and *b*. Hence find the lengths of its sides.
- Q5. If (1, 2), (4, y), (x, 6) and (3, 5) are the vertices of a parallelogram taken in order find x and y.
- Q6. Find the point on the x-axis which is equidistant from (2, -5) and (-2, 9).
- Q7. Find the centre of the circle passing through A (6, -6), B (3, -7) and C (3, -3).
- Q8. Find the coordinates of the points of trisection of the line segment joining (4, -1) and (-2, -3).
- Q9. Find the coordinates of the points which divide the line segment joining A (- 2, 2) and B (2, 8) into four equal parts.
- Q10. Find a relation between x and y such that the point (x, y) is equidistant from the point (3, 6) and (- 3, 4).
- Q11. If two adjacent vertices of a parallelogram are (3,2) and (-1,0) and the diagonals intersect at (2, -5), then find the coordinates of the other two vertices.
- Q12. Find the type of quadrilateral formed by the points (-1, -2), (1, 0), (-1, 2), (-3, 0) and justify your answer.
- Q13. Find the ratio in which the line segment joining A (1, -5) and B (-4, 5) is divided by the *x*-axis. Also find the coordinates of the point of division.
- Q14. Determine the ratio in which the line 2x + y 4 = 0 divides the line segments joining A (2, -2) and B (3,7).
- Q15. If Q (0, 1) is equidistant from P (5, 3) and R (x, 6), find the values of x. Also find the distance QR and PR.

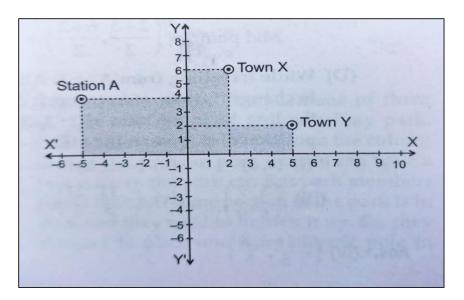
LONG ANSWER TYPE QUESTIONS (4 MARKS)

SECTION – D

- Q1. The vertices of quadrilateral *ABCD* are A (5, -1), B (8,3), C (4, 0) and D (1, -4). Prove that *ABCD* is a rhombus.
- Q2. Find the centre and radius of the circumcircle (i.e., circumcentre and circum-radius) of the triangle whose vertices are (-2, 3), (2, -1) and (4, 0).
- Q3. Find the coordinates of the points of trisection (*i.e.*, *Points dividing in three equal parts*) of the line segment joining the points A (2, -2) and B (-7, 4).
- Q4. An equilateral triangle has one vertex at (3, 4) and another at (-2, 3). Find the coordinates of the third vertex.



- Q5. The three vertices of a parallelogram *ABCD* are *A* (3, -4), *B* (-1, -3) and *C* (-6, 2). Find the coordinates of vertex *D* and find the area of *ABCD*.
- Q6. The base QR of an equilateral triangle PQR lies on x-axis. The co-ordinates of point Q are (-4, 0) and the origin is the mid-point of the base. Find the co-ordinates of the point P and R.
- Q7. Two friends Dalvin and Alice works in the same office in Toronto. In the Christmas vacation, they both decided to go to their home towns represented by *Town X* and *Town Y*. *Town X* and *Town Y* are connected by trains from the same station *C* in Toronto. The situation of *Town X*, *Town Y* and *station A* is shown on the coordinate axis.



Based on the given situation, answer the following questions:

i. What is the distance that Dalvin have to travel to reach his hometown *X*?

(a) $\sqrt{51}$ units	(c) $\sqrt{35}$ units
(b) $\sqrt{53}$ units	(d) $\sqrt{47}$ units

(e)

ii. What is the distance that Alice has to travel to reach her hometown *Y*?

(a) $2\sqrt{26}$ units	(c) $2\sqrt{10}$ units
(b) $\sqrt{107}$ units	(d) $\sqrt{51}$ units

iii. Now, both of them plan to meet at a place between Town X and Town Y, such that it is a mid-point between both. Calculate the coordinates of the mid-point of X and Y.

(a) (1, 3)	(c) (2.5,3)
(b) (2, - 4)	(d) (3.5, 4)

iv. While travelling from A to Y, Alice had to change the train, at a station, it divides the



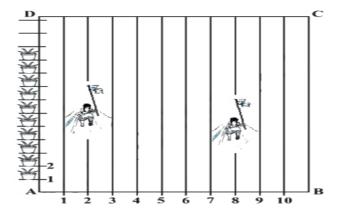
line AY in the ratio of 2: 3, find the position of station on the grid.

(a)
$$\left(0, \frac{7}{9}\right)$$
 (c) $\left(\frac{11}{8}, \frac{17}{3}\right)$
(b) $\left(-\frac{11}{5}, \frac{24}{5}\right)$ (d) (12, 7)

Q8.

To conduct Sport Day activities, in your rectangular shaped school ground *ABCD*, lines have been drawn with chalk powder at a distance of 1m each. 80 flower pots have been placed at a distance of 1 m from each other along *AD*, as shown in figure Hannah runs $\frac{1}{4}$ th the distance AD in the 2nd line and posts a blue flag. Preeta runs $\frac{1}{5}$ th the distance AD on the 8th line and posts a green flag.

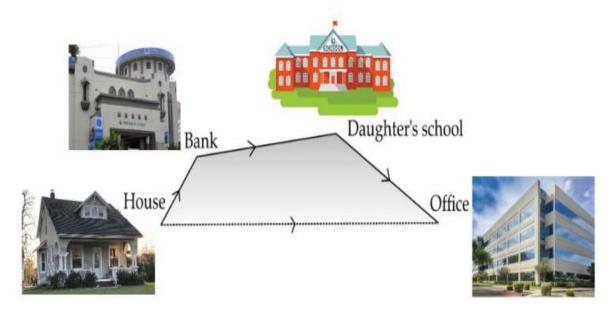
- i. What is the distance between both the flags?
- ii. If Uthara has to post an orange flag exactly halfway between the line segment joining the two flags, where should she post her flag?
- iii. Which mathematical concept is used in the above problem?
- iv. What value is depicted in this problem?



Q9. Find the ratio in which the point P(x, 2) divides the line segment joining the points A (12, 5) and B(4, -3). Also find x.



Q10. Rajeev went out from his house to reach the office. But he had to get some work done before going to the office. So, he first of all went to the bank first, from there he went to his son's school, and then reaches to office. The position of home, school, bank and office on coordinate axis is shown in the following figure:



Now, answer the following questions:

(i) If Rajeev goes directly from bank to his office, how much distance he would travel?

- (ii) How much distance he will travel, if goes directly from home to the office?
- (a) $15\sqrt{7}$ units (b) 10 units (c) $14\sqrt{3}$ units (d) $11\sqrt{5}$ units
- (iii) If at the mid-point of the bank and school, there is a park, what are the coordinates of the park?
- (a) (13, 14) (b) (9,11) (c) (-5, 10) (d) (10, 12)

(iv) Find the distance of the point (-6, 8) from the origin.(a) 8 units(b) 10 units(c) 11 units(d) 9 units

ANSWERS OF SECTION - A					
1. (d) 10	6. (a) 5	11. 5 units	16. Inside the circle		
2. (b) 22	7. (d) 3:5	12. $y = -9$ or $y = 3$	17. $k = \pm 4$		
3. (d) $\sqrt{a^2 + b^2}$	8. (c) (2, 0)	13. 2:5	18. BD = 5		
4. (c) -1	9. (b) (-4, 2)	14. 4 units	19. $\sqrt{37}$ units		



5. (c) 1	10. (d) -1, 7	15. $p = 3$	20.	20. 12				
ANSWERS OF SECTION - B								
1. (-7, 0)	6. bx = ay.	11. Yes		16. $\left(\frac{2}{5}, 0\right)$				
2. 3	7. <i>y</i> = -1	12. Scalene	e Triangle	17. 2:1				
3. Ratio is 2 : 1 & $k =$	$\frac{2}{3}$ 8. (0,9)	13. $x - y = 2$	2	18. Yes				
4. t = 1	9. $\left(\frac{-2}{7}, \frac{-20}{7}\right)$	14. BC = (1, 2)	19. 24 square units				
5. $k = \frac{5}{2}$ or $k = 5:2$	10. (-4, - 7)	15. Absciss	sa of $\mathbf{R} = 1$	20. A (3, -10)				
	ANSWERS OF SECTION - C							
1. Non- collinear	6. (-7,0)		11. (1,-12) and (
2. $y = 3 \text{ or } y = -9$	7. (4,-5)	7. (4,-5) 12		12. Square				
3. 24 square units	8. (2 , -5/3) and	8. (2, -5/3) and (0, -7/3)		13. k =1 and (-3/2, 0)				
4. $a = 1$, $b = 1$ AB = CD = $\sqrt{10}$ uni BC = AD = $\sqrt{10}$ un		9. $\left(-1, \frac{7}{2}\right), (0, 5), \left(1, \frac{13}{2}\right)$		14. 2:9				
5. $x = 6$ and $y = 3$	10. $3x + y - 5 =$	0		or $x = -4$ and $\sqrt{41}$, PR = $\sqrt{82}$				

ANSWERS OF SECTION – D

1. The sides of the quadrilateral AB = BC = CD = AD = 5 units & the

diagonals $AC = \sqrt{2}$ units and $BD = 7\sqrt{2}$ units

As the length of all the sides are equal and the length of the diagonals are not equal.

- \Rightarrow *ABCD* is a rhombus
- 2. Circumcentre of the $\triangle ABC$ is $\left(\frac{3}{2}, \frac{5}{2}\right)$ and Circumradius of $\triangle ABC$ is $\frac{5\sqrt{2}}{2}$
- 3. The coordinates of the points of trisection of the line segment joining A and B are (-1, 0) and (-4, 2)
- 4. Third vertex has the coordinates $\frac{1+\sqrt{3}}{2}, \frac{7-5\sqrt{3}}{2}$ or $\left(\frac{1-\sqrt{3}}{2}, \frac{7+5\sqrt{3}}{2}\right)$



- 15 square units 5.
- Coordinates of P are $(0, 4\sqrt{3})$ or $(0, -4\sqrt{3})$ 6.
- 7. (i) (b) $\sqrt{53}$ units (iii) (d) (3.5, 4) (iv) (b) $\left(-\frac{11}{5}, \frac{24}{5}\right)$ (ii) (a) $2\sqrt{26}$ units
- (i) $\sqrt{61}$ m 8. (iii) Co-ordinate Geometry
 - (ii) $(5, \frac{45}{2})$ (iv) Team Spirit
- Ratio is 3:5 and x = 99.
- 10. (i) (a) $2\sqrt{97}$ units (iii) (b) (9,11)
 - (ii) (d) $11\sqrt{5}$ units (iv) (b) 10 units

HOTS QUESTIONS

1. (1, -1), (0, 4) and (-5, 3) are vertices of a triangle. Check whether it is a scalene triangle, isosceles triangle or an equilateral triangle. Also, find the length of its median joining the vertex (1, -1) the mid-point of the opposite side.

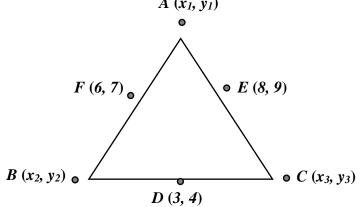
Ans: $\triangle ABC$ is isosceles.

: Length of the median AD is $\frac{\sqrt{130}}{2}$ units.

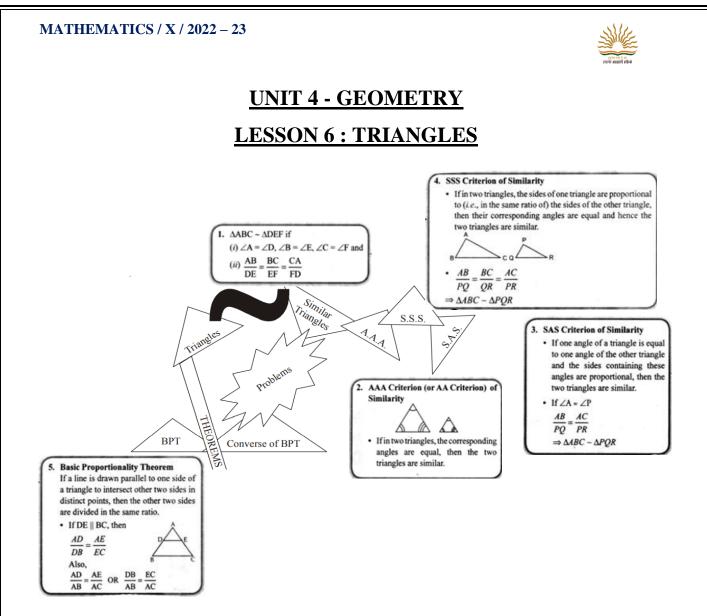
2. The midpoints D, E, F of the sides of a triangle ABC are (3, 4), (8, 9) and (6, 7). Find the coordinates of the vertices of the triangle.

Ans:





Hence, the vertices of the $\triangle ABC$ are A (11, 12), B (1, 2) and C (5, 6)



LEARNING PLAN

- **TOPIC 1**: similar triangles, Definition, examples, Basic proportionality theorem
- TOPIC 2: Criterion of Similarity (AAA, SSS, SAS) Results based on it

TOPIC 1

- Two figures having same shapes (size may or may not same) are called similar figures
- Pair of all regular polygons are similar figures
- All circles are similar figures
- Film 35mm is enlarged into 70mm, and then they are called similar figures.

Similar triangles: If two triangles are said to be similar if

- (a) Their corresponding angles are equal
- (b) Ratio of their corresponding sides are equal/proportional



Basic proportionality Theorem/ Thales Theorem: If a line is drawn parallel to one side of a triangle to intersect the other two sides in distinct points, then the other two sides are divided in the same ratio.

TOPIC 2

Criterion of similarity (AAA, SSS, SAS) and Results related on it.

Revision notes

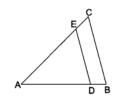
- In two triangles, if the corresponding angles are equal, then the corresponding sides are in the same ratio, then the triangles are similar (AAA similarity criterion)
- If the corresponding sides of any two triangles are proportional, then the corresponding angles are equal and the two triangles are similar (SSS similarity criterion)
- If one angle of a triangle is equal to one angle of the other triangle and the corresponding sides including are proportional. Then the triangle are similar (SAS criterion
- of the other triangle and the corresponding sides including are proportional. Then the triangle are similar (SAS criterion
- The ratio of the areas of two similar triangles is equal to the square of the ratio of their corresponding sides

OBJECTIVE QUESTIONS & MULTIPLE CHOICE QUESTIONS SECTION A (1 MARK)

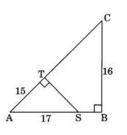
- Q1. Two sides and the perimeter of one triangle are respectively three times the corresponding sides and the perimeter of the other triangle. Are the two triangles similar? Why?
- Q2. A and B are respectively the points on the sides PQ and PR of a \triangle PQR such that PQ = 12.5 cm, PA = 5 cm, BR = 6 cm, and PB = 4 cm. Is AB || QR? Give reason.
- Q3. In triangles PQR and TSM, $\angle P = 55^\circ$, $\angle Q = 25^\circ$, $\angle M = 100^\circ$, and $\angle S = 25^\circ$. Is $\triangle QPR \sim \triangle TSM$? Why?
- Q4. If ABC and DEF are similar triangles such that $\angle A = 47^{\circ}$ and $\angle E = 63^{\circ}$, then the measures of $\angle C = 70^{\circ}$. Is it true? Give reason
- Q5. If triangle ABC is similar to triangle DEF such that 2AB = DE and BC = 8 cm. Then find the length of EF.
- Q6. In an isosceles $\triangle ABC$, if AC = BC and $AB^2 = 2AC^2$, then find $\angle C$.
- Q7. The length of the diagonals of a rhombus are 16 cm and 12 cm. Find the length of side of the rhombus.



- Q8. A man goes 24 m towards West and then 10 m towards North. How far is he from the starting point?
- Q9. $\triangle ABC \sim \triangle DEF$ such that AB = 9.1 cm and DE = 6.5 cm. If the perimeter of $\triangle DEF$ is 25 cm, what is the perimeter of $\triangle ABC$?
- Q10. In Fig., DE || BC. If AD = x, DB = x 2, AE = x + 2 and EC = x 1, find the value of x.



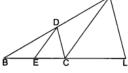
Q11. In the given figure, ∠T and ∠B are right angles. If the length of AT, BC and AS (in centimeters) are 15, 16, and 17 respectively, then the length of TC (in centimeters) is:



(a) 18 (b) 16 (c) 19 (d) 12 Q12. XY is drawn parallel to the base BC of a \triangle ABC cutting AB at X and AC at Y. If AB = 4 BX and YC =2cm, then AY is

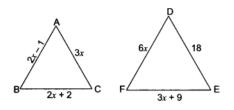
Q13. In \triangle ABC and \triangle DEF, \langle B = \langle E, \langle F = \langle C and AB= 3DE. Then the two triangles are

- (a) Congruent but not similar (c) neither congruent nor similar
- (b) Similar but not congruent (d) none of the above
- Q14. In the given Fig, CD || LA and DE || AC. Find the length of CL, if BE = 4 cm and EC = 2 cm.



Q15. In Fig, if $\triangle ABC \sim \triangle DEF$ and their sides are of lengths (in cm) as marked along with them, then find the lengths of the sides of each triangle





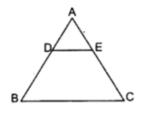
Q16. If in $\triangle ABC$ and $\triangle DEF$, $\frac{AB}{DE} = \frac{BC}{FD}$, then they will be similar, when a) $\angle B = \angle E$ c) $\angle B = \angle D$

b) $\angle A = \angle D$ d) $\angle A = \angle F$

Q17. If in two triangles ABC and DEF, $\frac{AB}{DE} = \frac{BC}{FE} = \frac{CA}{FD}$ then

- a) $\Delta FDE \sim \Delta CAB$ c) $\Delta CBA \sim \Delta FDE$
- b) $\Delta FDE \sim \Delta ABC$ d) $\Delta BCA \sim \Delta FDE$

Q18. In figure, if DE || BC, AD=3 cm, BD= 4 cm and BC= 14 cm, then DE equals





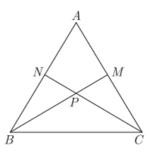
Q19. In $\triangle ABC$, $\angle B=90^{\circ}$, BD perpendicular to AC. If AC= 9cm, AD= 3 cm, then BD is equal to

a)	$2\sqrt{2}cm$	c)	$2\sqrt{3}cm$
b)	$3\sqrt{2}cm$	d)	3√ <u>3</u> cm

Q20. All the congruent figures are similar but the converse is not true. True or false?

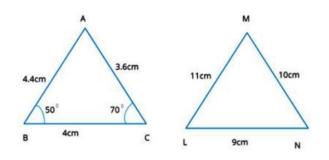
<u>SHORT ANSWER TYPE QUESTION (2 MARKS)</u> <u>SECTION B</u>

Q1. In the figure, AM: MC =3:4, BP:PM =3:2 and BN = 12 cm. Then find AN

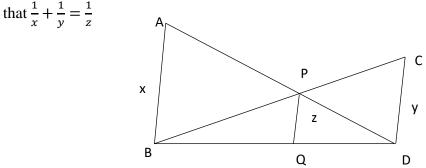




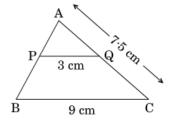
- Q2. If the corresponding Medians of two similar triangles are in the ratio 5 : 7. Then find the ratio of their sides.
- Q3. CM and RN are respectively the medians of $\triangle ABC$ and $\triangle PQR$. If $\triangle ABC \sim \triangle PQR$, then Prove that (a) $\triangle AMC \sim \triangle PNR$ (b) $\frac{CM}{RN} = \frac{AB}{PQ}$
- Q4. Diagonals AC and BD of a trapezium ABCD with AB || DC intersect each other at the pointO. Using a similarity criterion for two triangles, show that OA/OC= OB/OD.
- Q5. Find $\angle M$



Q6. In the adjoining figure, AB PQ CD, AB = x units, CD = y units and PQ = z units. Then prove

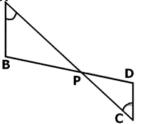


- Q7. A street light bulb is fixed on a pole 6 m above the level of the street. If a woman of height 1.5 m casts a shadow of 3m, what is the length of the shadow of the pole?
- Q8. A 15 metres high tower casts a shadow 24 metres long at a certain time and at the same time, a telephone pole casts a shadow 16 metres long. Find the height of the telephone pole.
- Q9. In Figure, PQ || BC, PQ = 3 cm, BC = 9cm and AC = 7.5 cm. Find the length of AQ

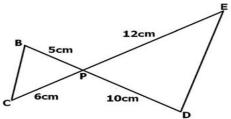




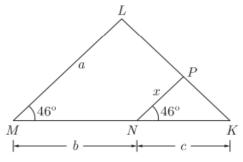
Q10. In the below figure, if $\angle A = \angle C$, AB = 6 cm, BP = 15 cm, AP = 12 cm and CP = 4 cm, then find the lengths of PD and CD.



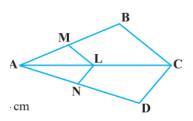
Q11. In the below Figure, BD and CE intersect each other at the point P. Is $\triangle PBC \sim \triangle PDE$? Why?



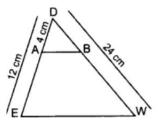
Q12. In the figure find x



Q13. In the figure given, if LM || CB and LN || CD, prove that $\frac{AM}{AN} = \frac{AB}{AD}$.

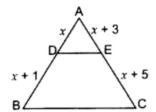


Q14. In ΔDEW , AB || EW. If AD = 4 cm, DE = 12 cm and DW = 24 cm, then find the value of DB.

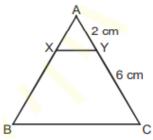


Q15. In $\triangle ABC$, DE || BC, find the value of x.

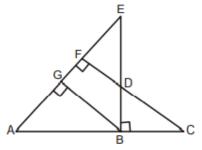




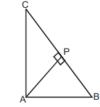
- Q16. If the perimeters of two similar triangles ABC and DEF are 50 cm and 70 cm respectively and one side of $\triangle ABC = 20$ cm, then find the corresponding side of $\triangle DEF$.
- Q17. X and Y are points on the sides AB and AC respectively of a triangle ABC such that = AX/AB=1/4, AY = 2 cm and YC = 6 cm. Find whether XY || BC or not.



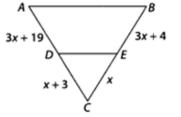
Q18. In given figure, EB perpendicular to AC, BG perpendicular to AE and CF perpendicular to AE. Prove that : (i) \triangle ABG ~ \triangle DCB (ii) BC/BD = BE/ BA



Q19. In triangle ABC, if AP perpendicular to BC and $AC^2 = BC^2 - AB^2$, then prove that $PA^2 = PB \times CP$.



Q20. Find the value of x for which $DE \parallel AB$ is given figure

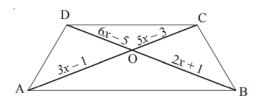




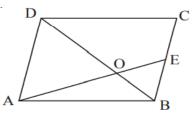
SHORT ANSWER TYPE QUESTION (3 MARKS)

SECTION C

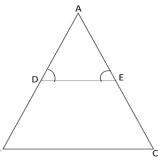
- Q1. In $\triangle ABC$, $DE \parallel BC$ such that AD = 7x 4 cm, AE = 5x 2 cm, DB = 3x + 4 cm and EC = 3x cm. Then find the value of x.
- Q2. In the given figure, AB \parallel DC and diagonals AC and BD intersect at O. If OA = 3x 1 and OB = 2x + 1, OC = 5x 3 and OD = 6x 5, find the value of x.



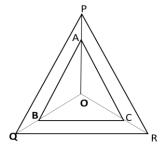
Q3. In the given figure, ABCD is a parallelogram. AE divides the line segment BD in the ratio 1 : 2. If BE = 1.5 cm find BC



Q4. In figure, if $\angle D = \angle E$ and AD /AE = DB / EC, Prove that $\triangle BAC$ is an isosceles triangle.

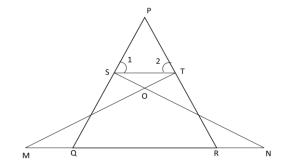


Q5. In figure, A, B, C are points on OP, OQ and OR respectively such that AB || PQ and AC || PR. Show that BC || QR.

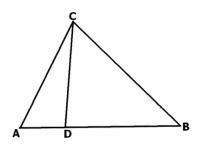


Q6. In figure, $\angle 1 = \angle 2$ and $\triangle NSQ \cong \triangle MTR$, then prove that $\triangle PTS \sim \triangle PRQ$.

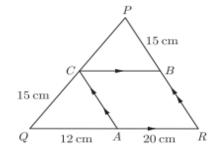




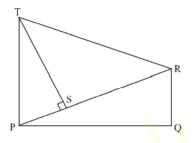
Q7. In the figure, if $\angle ACB = \angle CDA$, AC=8 cm and AD = 3 cm, find BD.



Q8. In the given figure below, CB \parallel QR and CA \parallel PR Also AQ = 12 cm, AR = 20 cm, PB = CQ = 15 cm. Calculate PC and BR.



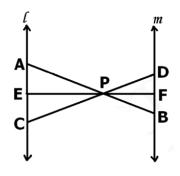
Q9. In the given figure, RQ and TP are perpendicular to PQ, also TS perpendicular to PR . Prove that ST.RQ = PS.PQ.



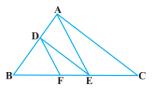
- Q10. In the given figure, RQ and TP are perpendicular to PQ, also TS perpendicular to PR . Prove that ST. RQ = PS. PQ.
- Q11. In the figure, $l \parallel m$ and line segments AB, CD and EF are concurrent at point P. Prove that AE/BF=AC/BD=CE/FD.



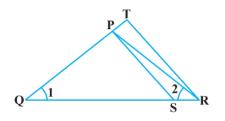




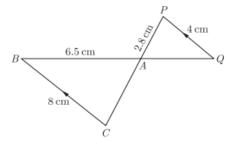
Q12. In the Figure , DE || AC and DF || AE. Prove that $\frac{BF}{BE} = \frac{FE}{EC}$



Q13. In Figure below, $\frac{QR}{QT} = \frac{QS}{PR}$ and $\angle 1 = \angle 2$. Show that $\triangle PQS \sim \triangle TQR$.



Q14. In the given figure, BC || PQ and BC = 8 cm, PQ = 4 cm, BA = 6 5. cm AP = 2 8. cm. Find the length of CA.

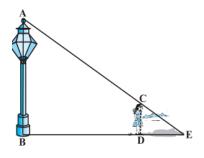


Q15. If $\triangle ABC \sim \triangle DEF$, AB = 4 cm, DE = 6 cm, EF = 9 cm and FD = 12 cm, find the perimeter of $\triangle ABC$.

LONG ANSWER TYPE QUESTIONS (4 MARKS) SECTION D (4 MARKS)

Q1. A girl of height 90 cm is walking away from the base of a lamp-post at a speed of 1.2 m/s. If the lamp is 3.6 m above the ground, find the length of her shadow after 4 seconds.

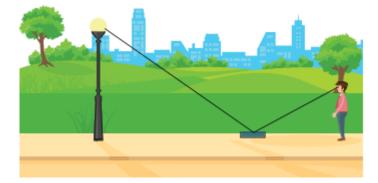




Q2. Aakesh wanted to determine the height of a tree on the corner of his block. He knew that a certain fence by the tree was 4 feet tall. At 3 PM, he measured the shadow of the fence to be 2.5 feet tall. Then he measured the tree's shadow to be 11.3 feet. What is the height of the tree?



Q3. Ramesh places a mirror on level ground to determine the height of a pole (with traffic light fired on it). He stands at a certain distance so that he can see the top of the pole reflected from the mirror. Ramesh's eye level is 1.5 m above the ground. The distance of Ramesh and the pole from the mirror are 1.8 m and 6 m respectively



- 1. Which criterion of similarity is applicable to similar triangles?
 - (a) SSA (b) ASA

(D) ASA	
That is the baight of the polo?	

- 2. What is the height of the pole?
 - (a) 6 metres(b) 8 metres

(c) 5 metres

(c) SSS

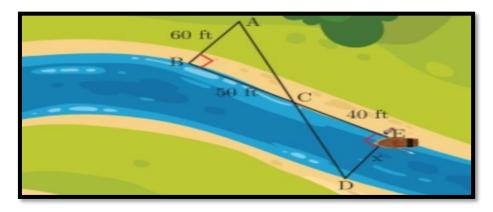
(d) AA

- (d) 4 metres
- 3. Now Ramesh moves behind such that distance between pole and Ramesh is 13 meters. He places mirror between him and pole to see the reflection of light in right position. What is the distance between mirror and Ramesh?



- (a) 7 metres
- (b) 3 metres
- 4. What is the distance between mirror and pole?
 - (a) 9 metres
 - (b) 8 metres

- (c) 5 metres
- (d) 4 metres
- (c) 12 metres
- (d) 10 metres
- Q4. Tania is very intelligent in Maths, she always tries to relate the concept of maths in daily life. One day she plans to cross a river and wants to know how far is the other side; she takes measurement on her side of the river and makes the drawing as shown in the fig

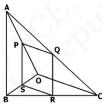


- 1) Which similarity criterion is used in solving the above problem?
- (a) SAS (b) AA (c)SSS (d) None
- 2) Consider the following statement

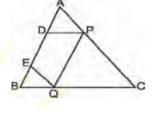
S1: $\angle ACB = \angle DCE$ and S2: $\angle BAC = \angle CDE$ which of the following statements are correct

- (a) S1 and S2 (b) S1 (c) S2 (d) None
- 3) What is the distance *x* across the river
- (a) 96ft (b) 48ft (c) 24ft (d) 16ft
- 4) What is the approximate length of AD shown?
- (a) 120fta (b)160ft (c)140ft (d)100ft
- Q5. If AD and PM are medians of triangles ABC and PQR respectively where Δ ABC ~ Δ PQR, Prove that AB / PQ = AD/PM
- Q6. D is a point on the side BC of a triangle ABC such that \angle ADC = \angle BAC. Show that $CA^2 = CB \times CD$
- Q7. In the figure, if PQRS is a parallelogram, AB || PS and PQ || OC, then prove that OC || SR

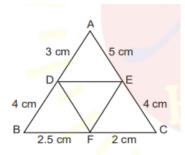




Q8. In the figure, there are two points D and E on side AB of DABC such that AD = BE. If DP || BC and EQ || AC, then prove that PQ || AB



Q9. In the given figure, AD = 3 cm, AE = 5 cm, BD = 4 cm, CE = 4 cm, CF = 2 cm, BF = 2.5 cm, then find the pair of parallel line and hence their lengths



- Q10. CD and GH are respectively the bisectors of \angle ACB and \angle EGF such that D and H lie on sides AB and FE of \triangle ABC and \triangle EFG respectively. If \triangle ABC ~ \triangle FEG, show that:
 - i. CD / GH = AC / FGii. $\Delta DCB \sim \Delta HGE$ iii. $\Delta DCA \sim \Delta HGF$

SL.NO.	ANSWERS
	SECTION A (1 MARK)
1	Since the perimeters and two sides are proportional ∴ The third side is proportional to the corresponding third side. i.e., The two triangles will be similar by SSS criterion.



2	Yes, $\frac{PA}{AQ} = \frac{5}{12.5-5} = \frac{5}{7.5} = \frac{2}{3}$ $\frac{PB}{BR} = \frac{4}{6} = \frac{2}{3}$ Since $\frac{PA}{AQ} = \frac{PB}{BR} = \frac{2}{3}$ $\therefore AB QR$ Fig. 7.4
3	Since, $\angle R = 180^{\circ} - (\angle P + \angle Q)$ = $180^{\circ} - (55^{\circ} + 25^{\circ}) = 100^{\circ} = \angle M$ $\angle Q = \angle S = 25^{\circ}$ (Given) $\triangle QPR \sim \triangle STM$ i.e., $\triangle QPR$ is not similar to $\triangle TSM$.
4	Since $\triangle ABC \sim \triangle DEF$ $\therefore \angle A = \angle D = 47^{\circ}$ $\angle B = \angle E = 63^{\circ}$ $\therefore \angle C = 180^{\circ} - (\angle A + \angle B) = 180^{\circ} - (47^{\circ} + 63^{\circ}) = 70^{\circ}$ \therefore Given statement is true.
5	$\Delta ABC \sim \Delta DEF \text{ (Given)}$ $\therefore \frac{AB}{DE} = \frac{BC}{EF}$ $\frac{AB}{2AB} = \frac{8}{EF} (\because DE = 2AB)$ $\frac{1}{2} = \frac{8}{EF}$ $\therefore EF = 16 \text{ cm}$ $B = \frac{1}{2} = \frac{16}{EF}$
6	AB ² = 2AC ² (Given) AB ² = AC ² + AC ² AB ² = AC ² + BC ² (\therefore AC = BC) Hence AB is the hypotenuse and \triangle ABC is a right angle A. So, \angle C = 90° B
7	\therefore The diagonals of rhombus bisect each other at 90°. ∴ In the right angle ΔBOC BO = 8 cm CO = 6 cm



r	Г
	∴ By Pythagoras Theorem $BC^2 = BO^2 + CO^2 = 64 + 36$ $BC^2 = 100$ BC = 10 cm
8	By Pythagoras Theorem $AC^2 = AB^2 + BC^2 = (24)^2 + (10)^2$ $AC^2 = 676$ AC = 26 m \therefore The man is 26 m away from the starting point. C 10 m B 24 m
9	Since $\triangle ABC \sim \triangle DEF$. $\frac{\text{Perimeter of } \Delta DEF}{\text{Perimeter of } \Delta ABC} = \frac{DE}{AB}$
	$\frac{25}{\text{Perimeter of }\Delta ABC} = \frac{6.5}{9.1}$
	Perimeter of $\triangle ABC = \frac{25 \times 91}{65} = 35 \text{ cm}$
10	In \triangle ABC, we have DE BC, \therefore AD/DB = AE/EC [By Basic Proportionality Theorem] $\Rightarrow x/(x-2) = (x+2)/(x-1)$ $\Rightarrow x(x-1) = (x-2) (x+2)$ $\Rightarrow x^2 - x = x^2 - 4$ $\Rightarrow x = 4$
11	(c) 19
12	(c) 6 cm
13	(b) Similar but not congruent
14	$\Rightarrow \frac{BD}{DA} = \frac{BE}{EC} \qquad (By BPT) \qquad \dots (i)$ In $\triangle ABL \ DC AL$ $\Rightarrow \frac{BD}{DA} = \frac{BC}{CL} \qquad (By BPT) \qquad \dots (ii)$ From (i) and (ii) we get $\frac{BE}{EC} = \frac{BC}{CL} \qquad \Rightarrow \frac{4}{2} = \frac{6}{CL} \qquad \Rightarrow CL = 3 \text{ cm}$



15	$\Delta ABC \sim \Delta DEF \text{ (Given)}$ therefore, $\frac{AB}{DE} = \frac{BC}{EF} = \frac{CA}{FD}$ So, $\frac{2x-1}{18} = \frac{2x+2}{3x+9} = \frac{3x}{6x}$ Now, taking $\frac{2x-1}{18} = \frac{3x}{6x}$, we have B $\frac{2x-1}{18} = \frac{1}{2}$ $\Rightarrow 4x - 2 = 18$
	$\Rightarrow x = 5$ $\therefore AB = 2 \times 5 - 1 = 9, BC = 2 \times 5 + 2 = 12$ $CA = 3 \times 5 = 15, DE = 18, EF = 3 \times 5 + 9 = 24$ and FD = 6 \times 5 = 30 Hence, AB = 9 cm, BC = 12 cm, CA = 15 cm DE = 18 cm, EF = 24 cm, FD = 30 cm
16	(c) $\angle B = \angle D$
17	(a) $\Delta FDE \sim \Delta CAB$
18	(b) 6 cm
19	(b) $3\sqrt{2}cm$ $\Delta ABC \sim \Delta ADB, \Delta ABC \sim \Delta BDC$ Then, $\Delta ADB \sim \Delta BDC$. So, $\frac{AD}{BD} = \frac{DB}{DC} = \frac{AB}{BC}$
20	True
	SECTION B (2 MARKS)
1	Draw MR parallel to CN which meets AB at the point R. $\frac{BN}{NR} = \frac{BP}{PM}$ Since PN MR (BPT) $\frac{12}{NR} = \frac{3}{2}$ Then, NR=8 cm. $\frac{AR}{RN} = \frac{AM}{MC}$ Since RM NC $\frac{AR}{R} = \frac{3}{4}$ Then, AR= 6 cm AN=AR+RN=6+8=14 cm.
2	5:7
3	Since $\triangle ABC \sim \triangle PQR$, $\frac{AB}{PQ} = \frac{BC}{QR} = \frac{AC}{PR}$ Also, $\angle A = \angle P$ Since $\angle A = \angle P$, $\frac{AB/2}{PQ/2} = \frac{AM}{PN} = \frac{AC}{PR}$ implies (a) $\triangle AMC \sim \triangle PNR$ (SAS)



	(b) $\frac{CM}{RN} = \frac{AC}{PR} = \frac{AB}{PQ}$
4	
4	$\angle OAB = \angle OCD, \angle OBA = \angle ODC$, alternate interior angles.
	$\Delta OCD \sim \Delta OAB$
	$\frac{OC}{OA} = \frac{OD}{OB} = \frac{CD}{AB}$
5	$\frac{AB}{ML} = \frac{4.4}{11} = 0.4$ $\frac{AC}{LN} = \frac{3.6}{9} = 0.4$ $\frac{BC}{MN} = \frac{4}{10} = 0.4$ $\Delta ABC \sim \Delta LMN \text{ (SSS)}$ $\angle M = \angle B = 50^{0}.$
6	In $\triangle ABD$, PQ AB . Then, $\frac{PQ}{AB} = \frac{DQ}{BD}$ ie, $\frac{z}{x} = \frac{DQ}{BD}$ (i)
	In $\triangle BCD$, PQ CD . Then, $\frac{PQ}{CD} = \frac{BQ}{BD}$
	ie, $\frac{z}{y} = \frac{BQ}{BD}$ (ii) Adding (i) and (ii),
	$\frac{z}{x} + \frac{z}{y} = \frac{DQ}{BD} + \frac{BQ}{BD} = \frac{DQ + BQ}{BD} = \frac{BD}{BD} = 1$ Then, $\frac{1}{x} + \frac{1}{y} = \frac{1}{z}$
7	Let AB be the pole and PQ be the height of the woman. $\angle ABC = \angle PQR = 90^{\circ}, \angle ACB = \angle PRS$ $\triangle ABC \sim \triangle PQR$ (AA)
	$\frac{AB}{PQ} = \frac{BC}{QR} = \frac{AC}{PR}$
	$\frac{6}{1.5} = \frac{BC}{3}$
	Length of shadow of the pole= $BC=12 \text{ m}$.
8	10 meters.
9	Since $\angle APQ = \angle ABC$, $\angle AQP = \angle ACB$ Then, $\triangle APQ \sim \triangle ABC$ (AA) $\frac{AP}{AB} = \frac{PQ}{BC} = \frac{AQ}{AC}$ $\frac{3}{9} = \frac{AQ}{7.5}$ $AQ = \frac{3 \times 7.5}{9} = 2.5 \ cm$



10	CD=2 cm, PD=5 cm.
11	$\frac{PB}{PD} = \frac{5}{10} = \frac{1}{2}, \frac{PC}{PE} = \frac{6}{12} = \frac{1}{2}, \ \angle BPC = \angle DPE(\text{vertically opposite angles})$ $\Delta PBC \sim \Delta PDE \text{ Using SAS similarity criteria.}$
12	$\frac{\Delta \text{KNP}}{\frac{KN}{KM}} \sim \frac{\Delta \text{KML Using AA similarity}}{\frac{KN}{KM}} = \frac{PN}{LM}$. Then, $\frac{c}{b+c} = \frac{x}{a}$. That is, $x = \frac{ac}{b+c}$
13	$\frac{AM}{MB} = \frac{AL}{LC} (1)$ $\frac{AL}{LC} = \frac{AN}{ND} (2)$ $\frac{MB}{AM} + 1 = \frac{ND}{AN} + 1$ $\frac{AB}{AM} = \frac{AD}{AN}$
14	$\frac{\frac{DA}{DE}}{\frac{4}{12}} = \frac{\frac{DB}{DW}}{\frac{24}{24}}$ $DB = 8 cm$
15	$\frac{x}{x+1} = \frac{x+3}{x+5}$ $x = 3$
16	$\frac{Perimeter(\Delta ABC)}{Perimeter(\Delta DEF)} = \frac{AB}{DE}, \text{ since}\Delta ABC \sim \Delta DEF$ Let AB= 20 cm $\frac{50}{70} = \frac{20}{DE}$ DE=28 cm
17	$\frac{AX}{AB} = \frac{1}{4}$ $AX = 1k, AB = 4k$ $BX = AB - AX = 4k - 1k = 3k$ $\frac{AX}{XB} = \frac{1k}{3k} = \frac{1}{3}$ $\frac{AY}{YC} = \frac{2}{6} = \frac{1}{3}$ $XC \text{ parallel to BC}$
18	$ \begin{array}{c} \angle 2 = \angle 5, \ \angle 6 = \angle 4 \\ \Delta ABG \sim \Delta DCB \text{ (AA)} \\ \angle 1 = \angle 3 \\ \angle ABE = \angle 5 \\ \Delta ABE \sim \Delta DBC \text{ (AA)} \\ \frac{BC}{BD} = \frac{BE}{BA} \end{array} \qquad $



19	$AC^{2}=BC^{2} - AB^{2}$ $AC^{2}+AB^{2}=BC^{2}.$ $\angle BAC=90^{0}.$ $\Delta APB \sim \Delta CPA \text{ (Converse of BPT)}$ $\frac{AP}{CP} = \frac{PB}{PA}$ $PA^{2}=PB.CP$
20	$\frac{x+3}{3x+19} = \frac{x}{3x+4}$ (x + 3)(3x + 4) = x(3x + 19) x=2
	SECTION C (3 MARKS)
1	$\frac{7x-4}{3x+4} = \frac{5x-2}{3x}$ $3x^2 - 13x + 4 = 0$ x=4,1/3 If $x=1/3$, $7x-4=-5/3<0$, not possible. Therefore, $x=4$
2	x= 2
3	OB/OD = BE/AD $\frac{1}{2} = 1.5/AD$ AD = 3 cm. As $AD = BC$, $BC = 3$ cm
4	$\frac{AD}{DB} = \frac{AE}{EC}$ $\frac{DB}{AD} + 1 = \frac{EC}{AE} + 1$ $\frac{AB}{AD} = \frac{AC}{AE} \dots \dots \dots \dots (i)$ Since $\angle ADE = \angle AED$, $AD = AE$ Then from(i), $AB = AC$ and $\triangle ABC$ is isosceles.
5	Since AB PQ, $\frac{OA}{AP} = \frac{OB}{BQ}$ (i) (BPT) Since AC PR, $\frac{OA}{AP} = \frac{OC}{CB}$ (ii) (BPT)
	From (i) and (ii) $\frac{OB}{BQ} = \frac{OC}{CR}$
	Then, BC QR.
6	Given, $\triangle NSQ \approx \triangle MTR$ Then, by CPCT, $\angle NQS = \angle MRT$ ie, $\angle PRQ = \angle PQR$ (1) In $\triangle PST$, $\angle P + \angle 1 + \angle 2 = 180^{\circ}$



$2P + 2\angle 1 = 180^{\circ}(2)$ In $\triangle PQR$, $\angle P + \angle PQR + \angle PRQ = 180^{\circ}$ $\angle P + 2\angle PQR = 180^{\circ}(3)$ Equating (2) and (3), $\angle P + 2\angle 1 = \angle P + 2\angle PQR$ $\angle PQR = \angle 1$ So, $\angle PST = \angle PQR$ $\square PTS$ and $\triangle PRQ$, $\angle P = \angle P = \text{common angle.}$ From (4) $\angle PST = \angle PQR$ Therefore, $\triangle PTS \sim \triangle PRQ$ (AA) 7 BD = 55/3 cm 8 $\frac{PC}{rQ} = \frac{PA}{Rq}$ (BPT) $\frac{PC}{15} = \frac{20}{12}$ Then, $PC = \frac{15\times20}{12} = 25$ cm In $\triangle PQR$, CB QR $\frac{PC}{rQ} = \frac{PB}{R}$ (BPT) $\frac{25}{15} = \frac{15}{25}$ Then, $PC = \frac{15\times15}{25} = 9$ cm 9 $\angle 1 + \angle 2 + \angle 4 = 180^{\circ}.$ $\angle 1 = 90^{\circ} - 22$ (i) Since TP perpendicular to PQ, $\angle TPQ = 90^{\circ}.$ $\angle 2 + \angle 3 = 90^{\circ} = \angle 2.$ (ii) From (i) and (ii), $\angle 1 = \angle 3$ In $\triangle RQP \sim \triangle PST$ (AA) $\frac{ST}{rP} = \frac{PS}{RQ}$ Then, $ST.RQ = PS.PQ$ 10 Statement and proof of the theorem. 11 $\angle EAP = \angle FPP, \angle APE = \angle FPB$, Then $\triangle AEP \sim \triangle BFP$ (AA) $So, \frac{AF}{RP} = \frac{EP}{RP} = \frac{AP}{RP}$ (ii) $\angle ECP = \angle DPP, \angle CPE = \angle FPB$, Then $\triangle ACP \sim \triangle BFP$ (AA) $\frac{EP}{RQ} = \frac{CP}{RP} = \frac{AP}{RP}$ (ii) $\angle ACP = \angle BPP, \angle CAP = \angle PBD$, Then $\triangle ACP \sim \triangle BDP$ (AA) $\frac{EP}{RP} = \frac{CP}{RP} = \frac{AP}{RP}$ (ii) $\angle ACP = \angle BPP, \angle CAP = \angle PBD$, Then $\triangle ACP \sim \triangle BDP$ (AA) $\frac{ACP}{RP} = \frac{BP}{RP} = \frac{AP}{RP}$ (ii) $\angle ACP = \angle BPP, \angle CAP = \angle PBD$, Then $\triangle ACP \sim \triangle BDP$ (AA) $\frac{AF}{RP} = \frac{PP}{RP} = \frac{AP}{RP}$ (ii)		
$2P + 2\angle PQR = 180^{\circ}(3)$ Equating (2) and (3), $\angle P + 2\angle I = \angle P + 2\angle PQR$ $\angle PQR = \angle I$ So, $\angle PST = \angle PQR$ $In \triangle PTS and \triangle PRQ$, $\angle P = \angle P = common angle$. From (4) $\angle PST = \angle PQR$ Therefore, $\triangle PTS \sim \triangle PRQ$ (AA) 7 BD = 55/3 cm 8 $\frac{PC}{CQ} = \frac{RA}{AQ}$ (BPT) $\frac{PC}{TS} = \frac{20}{12}$ Then, $PC = \frac{15\times20}{12} = 25 cm$ In $\triangle POR$, CB QR $\frac{PC}{CQ} = \frac{PB}{RR}$ (BPT) $\frac{25}{15} = \frac{15}{RR}$ Then, $BR = \frac{15\times15}{25} = 9 cm$ 9 $\angle I + \angle 2 + \angle 4 = 180^{\circ}$. $\angle I = 90^{\circ} - \angle 2$ (i) Since TP perpendicular to PQ, $\angle TPQ = 90^{\circ}$. $\angle 2 + \angle 3 = 90^{\circ}$. $\angle 3 = 90^{\circ} = \angle 2$ (ii) From (i) and (ii), $\angle I = 23$ In $\triangle RQP$ and $\triangle PST$, $\angle I = \angle 3$, $\angle 4 = \angle 5$ $\triangle RQP \sim \Delta PST$ (AA) $\frac{ST}{QP} = \frac{PS}{RQ}$ Then, ST.RQ = PS. PQ 10 Statement and proof of the theorem. 11 $\angle EAP = \angle FBP$, $\angle APE = \angle FPB$, Then $\triangle AEP \sim \triangle BFP$ (AA) So, $\frac{AE}{BP} = \frac{EP}{PP} = \frac{AP}{PP}$ (ii) $\angle ECP = \angle FDP$, $\angle CP = \angle FPD$, $\angle APE = \angle FPD$, Then $\triangle CEP \sim \triangle DFP$ (AA) $\frac{SP}{PP} = \frac{CE}{DT}$ (ii) $\angle ACP = \angle BDP$, $\angle CAP = \angle PBD$, Then $\triangle ACP \sim \triangle BDP$ (AA) $\frac{AC}{P} = \frac{CP}{DP} = \frac{AP}{PP}$ (iii)		$\angle P + 2\angle 1 = 180^{\circ}$ (2)
Equating (2) and (3), $\angle P + 2\angle I = \angle P + 2\angle PQR$ $\angle PQR = \angle I$ So, $\angle PST = \angle PQR$ (4) In $\triangle PTS$ and $\triangle PRQ$, $\angle P = \angle P = \text{common angle.}$ From (4) $\angle PST = \angle PQR$ Therefore, $\triangle PTS \sim \triangle PRQ$ (AA) 7 BD = 55/3 cm 8 $\frac{PC}{CQ} = \frac{RA}{AQ}$ (BPT) $\frac{PC}{TS} = \frac{2B}{BR}$ Then, $PC = \frac{15\times20}{12} = 25$ cm In $\triangle PQR$, CB QR $\frac{PC}{CQ} = \frac{PB}{BR}$ (BPT) $\frac{25}{15} = \frac{15}{BR}$ Then, $BR = \frac{15\times15}{25} = 9$ cm 9 $\angle I + \angle 2 + \angle 4 = 180^{\circ}.$ $\angle I = 90^{\circ} - \angle 2(i)$ Since TP perpendicular to PQ, $\angle TPQ = 90^{\circ}.$ $\angle 2 + \angle 3 = 90^{\circ}.$ $\angle 3 = 90^{\circ} = \angle 2(ii)$ From (i) and (ii), $\angle I = \angle 3$ In $\triangle RQP \simeq \Delta PST$ (AA) $\frac{ST}{QP} = \frac{PB}{RQ}$ Then, ST.RQ= PS. PQ 10 Statement and proof of the theorem. 11 $\angle EAP = \angle FBP, \angle APE = \angle FPB$, Then $\triangle AEP \sim \triangle BFP$ (AA) $\frac{BP}{PT} = \frac{CE}{PT} = \frac{AP}{BP}$ (ii) $\angle ACP = \angle BDP, \angle CAP = \angle PBD$, Then $\triangle ACP \sim \triangle BDP$ (AA) $\frac{AC}{BD} = \frac{CP}{PP} = \frac{AP}{BP}$ (iii)		In $\triangle PQR$, $\angle P + \angle PQR + \angle PRQ = 180^{\circ}$
		$\angle P + 2\angle PQR = 180^{\circ} - \dots $ (3)
In $\triangle PTS$ and $\triangle PRQ$, $\angle P = \angle P = \text{common angle.}$ From (4) $\angle PST = \angle PQR$ Therefore, $\triangle PTS \sim \triangle PRQ$ (AA) 7 BD = 55/3 cm 8 $\frac{PC}{CQ} = \frac{RA}{AQ}$ (BPT) $\frac{PC}{TS} = \frac{20}{12}$ Then, $PC = \frac{15 \times 20}{12} = 25 \text{ cm}$ In $\triangle PQR$, CB QR $\frac{PC}{CQ} = \frac{PB}{BR}$ (BPT) $\frac{25}{15} = \frac{15}{15}$ Then, $BR = \frac{15 \times 15}{25} = 9 \text{ cm}$ 9 $\angle 1 + \angle 2 + \angle 4 = 180^{\circ}.$ $\angle 1 = 90^{\circ} - \angle 2 \dots \dots \dots (i)$ Since TP perpendicular to PQ, $\angle TPQ = 90^{\circ}.$ $\angle 2 + \angle 3 = 90^{\circ}.$ $\angle 3 = 90^{\circ} = \angle 2 \dots \dots \dots (i)$ From (i) and (ii), $\angle 1 = \angle 3$ In $\triangle RQP \approx \triangle PST$ (AA) $\frac{ST}{QP} = \frac{PS}{RQ}$ Then, ST.RQ = PS. PQ 10 Statement and proof of the theorem. 11 $\angle EAP = \angle FBP, \angle APE = \angle FPB$, Then $\triangle AEP \sim \triangle BFP$ (AA) So, $\frac{AE}{BF} = \frac{EP}{FP} = \frac{AP}{BP} \dots \dots (i)$ $\angle ECP = \angle FDP, \angle CPE = \angle FPD$, Then $\triangle ACP \sim \triangle BFP$ (AA) $\frac{EP}{P} = \frac{CF}{PF} \dots \dots (ii)$ $\angle ACP = \angle BDP, \angle CAP = \angle PBD$, Then $\triangle ACP \sim \triangle BDP$ (AA) $\frac{AC}{DP} = \frac{CP}{PP} = \frac{AP}{BP} \dots \dots (ii)$		Equating (2) and (3), $\angle P + 2\angle 1 = \angle P + 2\angle PQR$
		$\angle PQR = \angle 1$ So, $\angle PST = \angle PQR$ (4)
From (4) $\angle PST = \angle PQR$ Therefore, $\triangle PTS \sim \triangle PRQ$ (AA) 7 BD = 55/3 cm 8 $\frac{PC}{CQ} = \frac{RA}{AQ}$ (BPT) $\frac{PC}{TS} = \frac{20}{12}$ Then, $PC = \frac{15 \times 20}{12} = 25 \ cm$ In $\triangle PQR$, CB QR $\frac{PC}{CQ} = \frac{PB}{R}$ (BPT) $\frac{25}{15} = \frac{15}{15}$ Then, $BR = \frac{15 \times 15}{25} = 9 \ cm$ 9 $\angle 1 + \angle 2 + \angle 4 = 180^{\circ}$. $\angle 1 = 90^{\circ} - \angle 2$ (i) Since TP perpendicular to PQ, $\angle TPQ = 90^{\circ}$. $\angle 2 + \angle 3 = 90^{\circ}$. $\angle 3 = 90^{\circ} = \angle 2$ (ii) From (i) and (ii), $\angle 1 = \angle 3$ In $\triangle RQP \ ad \ APST$ (AA) $\frac{ST}{QP} = \frac{PS}{RQ}$ Then, $ST.RQ = PS. PQ$ 10 Statement and proof of the theorem. 11 $\angle EAP = \angle FBP$, $\angle APE = \angle FPB$, Then $\triangle AEP \sim \triangle BFP$ (AA) So, $\frac{AE}{BF} = \frac{EP}{PP} = \frac{AP}{BP}$ (ii) $\angle ECP = \angle FDP$, $\angle CPE = \angle FPD$, Then $\triangle CEP \sim \triangle DFP$ (AA) $\frac{EP}{PP} = \frac{CP}{BP} = \frac{AP}{BP}$ (ii) $\angle ACP = \angle BDP$, $\angle CAP = \angle PBD$, Then $\triangle ACP \sim \triangle BDP$ (AA) $\frac{BP}{PP} = \frac{CP}{BP} = \frac{AP}{BP}$ (ii)		In \triangle PTS and \triangle PRQ,
Therefore, $\Delta PTS \sim \Delta PRQ$ (AA)7BD = 55/3 cm8 $\frac{PC}{CQ} = \frac{RA}{AQ}$ (BPT) $\frac{PC}{15} = \frac{20}{12}$ Then, $PC = \frac{15 \times 20}{12} = 25 cm$ In ΔPQR , CB QR $\frac{PC}{CQ} = \frac{PB}{BR}$ (BPT) $\frac{25}{15} = \frac{15}{BR}$ Then, $BR = \frac{15 \times 15}{25} = 9 cm$ 9 $\mathcal{L}1 + \mathcal{L}2 + \mathcal{L}4 = 180^{0}$. $\mathcal{L}1 = 90^{0} - \mathcal{L}2$		$\angle P = \angle P = $ common angle.
7BD = 55/3 cm8 $\frac{PC}{CQ} = \frac{RA}{AQ}$ (BPT) $\frac{PC}{15} = \frac{20}{12}$ Then, $PC = \frac{15 \times 20}{12} = 25 cm$ In ΔPQR , CB QR $\frac{PC}{CQ} = \frac{PB}{BR}$ (BPT) $\frac{25}{15} = \frac{15}{BR}$ Then, $BR = \frac{15 \times 15}{25} = 9 cm$ 9 $\mathcal{L}1 + \mathcal{L}2 + \mathcal{L}4 = 180^{0}$. $\mathcal{L}1 = 90^{0} - \mathcal{L}2$ (i) Since TP perpendicular to PQ, $\mathcal{L}TPQ = 90^{0}$. $\mathcal{L}2 + \mathcal{L}3 = 90^{0}$. $\mathcal{L}3 = 90^{0} = \mathcal{L}2$		
$\frac{Pc}{cq} = \frac{RA}{AQ} (BPT)$ $\frac{Pc}{cq} = \frac{20}{12} \text{Then, } PC = \frac{15 \times 20}{12} = 25 \ cm$ $\ln \Delta PQR, CB \parallel QR$ $\frac{Pc}{Cq} = \frac{PB}{BR} (BPT)$ $\frac{25}{25} = \frac{15}{15} \text{Then, } BR = \frac{15 \times 15}{25} = 9 \ cm$ $9 \angle 1 + \angle 2 + \angle 4 = 180^{0}.$ $\angle 1 = 90^{0} - \angle 2 \qquad \dots \dots (i)$ Since TP perpendicular to PQ, $\angle TPQ = 90^{0}.$ $\angle 2 + \angle 3 = 90^{0}.$ $\angle 3 = 90^{0} = \angle 2 \qquad \dots \dots (ii)$ From (i) and (ii), $\angle 1 = \angle 3$ In $\triangle RQP$ and $\triangle PST, \ \angle 1 = \angle 3$, $\angle 4 = \angle 5$ $\triangle RQP \sim \triangle PST (AA)$ $\frac{ST}{qP} = \frac{PS}{RQ} \text{Then, } ST.RQ = PS. PQ$ $10 \text{Statement and proof of the theorem.}$ $11 \angle EAP = \angle FBP, \ \angle APE = \angle FPB, \text{ Then } \triangle AEP \sim \triangle BFP (AA)$ $\frac{FP}{FP} = \frac{CP}{DF} = \frac{AP}{BP} \qquad \dots \dots (ii)$ $\angle ACP = \angle BDP, \ \angle CAP = \angle PBD, \text{ Then } \triangle ACP \sim \triangle BDP (AA)$ $\frac{AC}{BP} = \frac{CP}{BP} = \frac{AP}{BP} \qquad \dots (ii)$		Therefore, $\triangle PTS \sim \triangle PRQ$ (AA)
$\frac{PC}{15} = \frac{20}{12} \text{Then, } PC = \frac{15 \times 20}{12} = 25 \ cm$ $\ln \Delta PQR, CB \parallel QR$ $\frac{PC}{CQ} = \frac{PB}{BR} (BPT)$ $\frac{25}{15} = \frac{15}{BR} \text{Then, } BR = \frac{15 \times 15}{25} = 9 \ cm$ $9 \angle 1 + \angle 2 + \angle 4 = 180^{0}.$ $\angle 1 = 90^{0} - \angle 2 \qquad \dots \dots \dots (i)$ Since TP perpendicular to PQ, $\angle TPQ = 90^{0}.$ $\angle 2 + \angle 3 = 90^{0}.$ $\angle 2 + \angle 3 = 90^{0}.$ $\angle 2 = 22 \qquad \dots \dots \dots (ii)$ From (i) and (ii), $\angle 1 = \angle 3$ $\ln \Delta RQP \text{ and } \Delta PST, \ \angle 1 = \angle 3 \ \angle 4 = \angle 5$ $\Delta RQP \sim \Delta PST (AA)$ $\frac{ST}{QP} = \frac{PS}{RQ} \qquad \text{Then, } ST.RQ = PS. PQ$ $10 \text{Statement and proof of the theorem.}$ $11 \angle EAP = \angle FBP, \ \angle APE = \angle FPB, \text{ Then } \Delta AEP \sim \Delta BFP (AA)$ $So, \ \frac{AE}{BF} = \frac{EP}{BP} = \frac{AP}{BP} \qquad \dots \dots (i)$ $\angle ECP = \angle FDP, \ \angle CPE = \angle FPD, \text{ Then } \Delta AEP \sim \Delta DFP (AA)$ $\frac{EP}{FP} = \frac{CE}{DF} \qquad \dots \dots (ii)$ $\angle ACP = \angle BDP, \ \angle CAP = \angle PBD, \text{ Then } \Delta ACP \sim \Delta BDP (AA)$ $\frac{AC}{BD} = \frac{CP}{BP} = \frac{AP}{BP} \qquad \dots \dots (iii)$	7	BD = 55/3 cm
$ \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c}$	8	$\frac{PC}{15} = \frac{20}{12} \text{Then,} PC = \frac{15 \times 20}{12} = 25 \ cm$ In $\triangle PQR$, CB QR $\frac{PC}{CQ} = \frac{PB}{BR} \text{(BPT)}$
11 $\angle EAP = \angle FBP, \angle APE = \angle FPB, \text{ Then } \Delta AEP \sim \Delta BFP \text{ (AA)}$ So, $\frac{AE}{BF} = \frac{EP}{FP} = \frac{AP}{BP}$ (i) $\angle ECP = \angle FDP, \angle CPE = \angle FPD, \text{ Then } \Delta CEP \sim \Delta DFP \text{ (AA)}$ $\frac{EP}{FP} = \frac{CE}{DF}$ (ii) $\angle ACP = \angle BDP, \angle CAP = \angle PBD, \text{ Then } \Delta ACP \sim \Delta BDP \text{ (AA)}$ $\frac{AC}{BD} = \frac{CP}{DP} = \frac{AP}{BP}$ (iii)	9	$ \begin{array}{l} \angle 1 = 90^{0} - \angle 2 \dots (i) \\ \text{Since TP perpendicular to PQ, } \angle \text{TPQ} = 90^{0}. \\ \angle 2 + \angle 3 = 90^{0}. \\ \angle 3 = 90^{0} = \angle 2 \dots (ii) \\ \text{From (i) and (ii), } \angle 1 = \angle 3 \\ \text{In } \Delta \text{RQP and } \Delta \text{PST, } \angle 1 = \angle 3 \\ \Delta \text{RQP} \sim \Delta \text{PST} (AA) \end{array} $
So, $\frac{AE}{BF} = \frac{EP}{FP} = \frac{AP}{BP}$ (i) $\angle \text{ECP} = \angle \text{FDP}$, $\angle \text{CPE} = \angle \text{FPD}$, Then $\triangle \text{CEP} \sim \triangle \text{DFP}$ (AA) $\frac{EP}{FP} = \frac{CE}{DF}$ (ii) $\angle \text{ACP} = \angle \text{BDP}$, $\angle \text{CAP} = \angle \text{PBD}$, Then $\triangle \text{ACP} \sim \triangle \text{BDP}$ (AA) $\frac{AC}{BD} = \frac{CP}{DP} = \frac{AP}{BP}$ (iii)	10	Statement and proof of the theorem.
BF = DF = BD	11	So, $\frac{AE}{BF} = \frac{EP}{FP} = \frac{AP}{BP}$ (i) $\angle ECP = \angle FDP$, $\angle CPE = \angle FPD$, Then $\triangle CEP \sim \triangle DFP$ (AA) $\frac{EP}{FP} = \frac{CE}{DF}$ (ii) $\angle ACP = \angle BDP$, $\angle CAP = \angle PBD$, Then $\triangle ACP \sim \triangle BDP$ (AA)
12 In $\triangle ABC$, given as, DE AC Then, BD/DA = BE/EC(i) (BPT)	12	In $\triangle ABC$, given as, DE AC Then, BD/DA = BE/EC(i) (BPT)



	In $\triangle BAE$, given as, DF AE Then, BD/DA = BF/FE(ii) (BPT) From equation (i) and (ii), we get BE/EC = BF/FE , Then BF/BE= FE/EC.
13	In ΔPQR , $\angle PQR = \angle PRQ$ $\therefore PQ = PR$ (i) QR/QT = QS/PRUsing equation (i), we getQR/QT = QS/PQIn ΔPQS and ΔTQR , by equation (ii), QR/QS = QT/QP , $\angle PQS = \angle TQR$ $\therefore \Delta PQS \sim \Delta TQR$ [By SAS similarity criterion]
14	$\angle ACB = \angle APQ, \ \angle ABC = \angle AQP, \ Then \ \Delta ABC \sim \Delta AQP (AA)$ $\frac{AB}{AQ} = \frac{BC}{QP} = \frac{AC}{AP}$ $\frac{6.5}{AQ} = \frac{8}{4} = \frac{AC}{2.8}$ $AC = \frac{8 \times 2.8}{4} = 5.6 \ cm$
15	Since $\triangle ABC \sim \triangle DEF$, $\frac{AB}{DE} = \frac{BC}{EF} = \frac{AC}{DF} = \frac{Perimeter(\triangle ABC)}{Perimeter(\triangle DEF)}$ $\frac{4}{6} = \frac{BC}{9} = \frac{AC}{12} = \frac{Perimeter(\triangle ABC)}{27}$ Perimeter($\triangle ABC$)= 18 cm.
	SECTION D (4 MARKS)
1	Let AB denote the lamp-post and CD the girl after walking for 4 seconds away from the lamp- post. DE is the shadow of the girl. Let DE be x metres. Now, BD = $1.2 \text{ m} \times 4 = 4.8 \text{ m}$. Note that in \triangle ABE and \triangle CDE, \angle B = \angle D (Each is of 90° because lamp-post as well as the girl are standing vertical to the ground) and \angle E = \angle E (Same angle) So, \triangle ABE ~ \triangle CDE (AA similarity criterion) Therefore, BE / DE = AB/ CD i.e., $4.8 + x/x = 3.6$ /0.9 (90 cm = 90/ 100 m = 0.9 m) i.e., $4.8 + x = 4x$ i.e., $3x = 4.8$ i.e., $x = 1.6$ So, the shadow of the girl after walking for 4 seconds is 1.6 m long.
2	Height of the tree is 18 feet
3	Q1. (d) AA Q2. (c) 5 metres Q3. (b) 3 metres Q4. (d) 10 metres
4	Q1. b) AA Similarity Q2. a) S1 and S2 both Q3. b) 48 ft Q4. c) 140 ft



5	We know that the corresponding sides of similar triangles are in proportion.
	$\therefore AB/PQ = AC/PR = BC/QR(i)$
	Also, $\angle A = \angle P$, $\angle B = \angle Q$, $\angle C = \angle R$ (ii) $B \xrightarrow{\ \ D \ \ C} Q \xrightarrow{\ \ M \ \ R}$
	Since AD and PM are medians, they will divide their opposite sides.
	\therefore BD = BC/2 and QM = QR/2(iii)
	From equations (i) and (iii), we get
	AB/PQ = BD/QM(iv)
	In $\triangle ABD$ and $\triangle PQM$, From equation (ii), we have $\angle B = \angle Q$
	From equation (iv), we have, $AB/PQ = BD/QM$
	$\therefore \Delta ABD \sim \Delta PQM$ (SAS similarity criterion)
	\Rightarrow AB/PQ = BD/QM = AD/PM
6	In $\triangle OPQ$, $AB \parallel PQ$ OA/AP = OB/BQ(i) (BPT)
	In $\triangle OPR$, AC PR , OA/AP = OC/CR(ii) (BPT)
	From equation (i) and (ii), we get, $OB/BQ = OC/CR$
	In $\triangle OQR$, BC QR. (converse of Basic Proportionality Theorem)
7	$\frac{OP}{PA} = \frac{OS}{SB}, \text{ Since AB} PS$ $\frac{AP}{OP} = \frac{AQ}{QC}, \text{ Since PQ} OC$ $\frac{OP}{AP} = \frac{QC}{AQ}$
	$\frac{AP}{SB} = \frac{QC}{AQ} \dots \dots \dots (i)$
	Since PQRS is a parallelogram, QR AB
	Then, $\frac{CQ}{AQ} = \frac{CR}{BR}$ (ii)
	From (i) and (ii), $\frac{OS}{SB} = \frac{CR}{BR}$ Then, SR OC
8	In $\triangle ABC$, DP BC, EQ AC, $\frac{AD}{DB} = \frac{AP}{PC}$ (i) (BPT) $\frac{BE}{EA} = \frac{BQ}{QC}$ (BPT)
	$\frac{AD}{DB} = \frac{BQ}{QC} \dots (ii) \text{ Since AD} = BE, EA = DB$
	From (i) and (ii), $\frac{AP}{PC} = \frac{BQ}{QC}$ Then, PQ AB (Converse of BPT)
9	$\frac{EC}{EA} = \frac{4}{5} \text{ and } \frac{CF}{FB} = \frac{2}{2.5} = \frac{4}{5}$ $\frac{EC}{EA} = \frac{CF}{FB}$



	In $\triangle ABC$, EF AB (Converse of BPT) $\frac{CE}{CA} = \frac{4}{4+5} = \frac{4}{9}$ $\frac{CF}{CB} = \frac{2}{2+2.5} = \frac{2}{4.5} = \frac{4}{9}$ $\frac{EC}{CA} = \frac{CF}{CB}, \angle ECF = \angle ACB$ $\triangle CFE \sim \triangle CBA (SAS)$ $\frac{EF}{AB} = \frac{CE}{CA}$ $\frac{EF}{7} = \frac{4}{9}$ $EF = \frac{28}{9} cm, AB = 7 cm.$
10	From the given condition, $\triangle ABC \sim \triangle FEG$.
	$\therefore \angle A = \angle F, \angle B = \angle E, \text{ and } \angle ACB = \angle FGE$
	Since, $\angle ACB = \angle FGE$ $\therefore \angle ACD = \angle FGH$ (Angle bisector)
	$\therefore \angle ACD = \angle FOH \text{ (Aligie bisector)} \qquad B \longrightarrow C \qquad E \longrightarrow G$ And, $\angle DCB = \angle HGE \text{ (Angle bisector)}$
	In \triangle ACD and \triangle FGH,
	$\angle A = \angle F, \ \angle ACD = \angle FGH$
	$\therefore \Delta ACD \sim \Delta FGH$ (AA similarity criterion)
	\Rightarrow CD/GH = AC/FG
	(ii) In $\triangle DCB$ and $\triangle HGE$,
	$\angle DCB = \angle HGE$ (Already proved), $\angle B = \angle E$ (Already proved)
	$\therefore \Delta DCB \sim \Delta HGE$ (AA similarity criterion)
	(iii) In Δ DCA and Δ HGF,
	$\angle ACD = \angle FGH$ (Already proved), $\angle A = \angle F$ (Already proved)
	$\therefore \Delta DCA \sim \Delta HGF$ (AA similarity criterion
1	

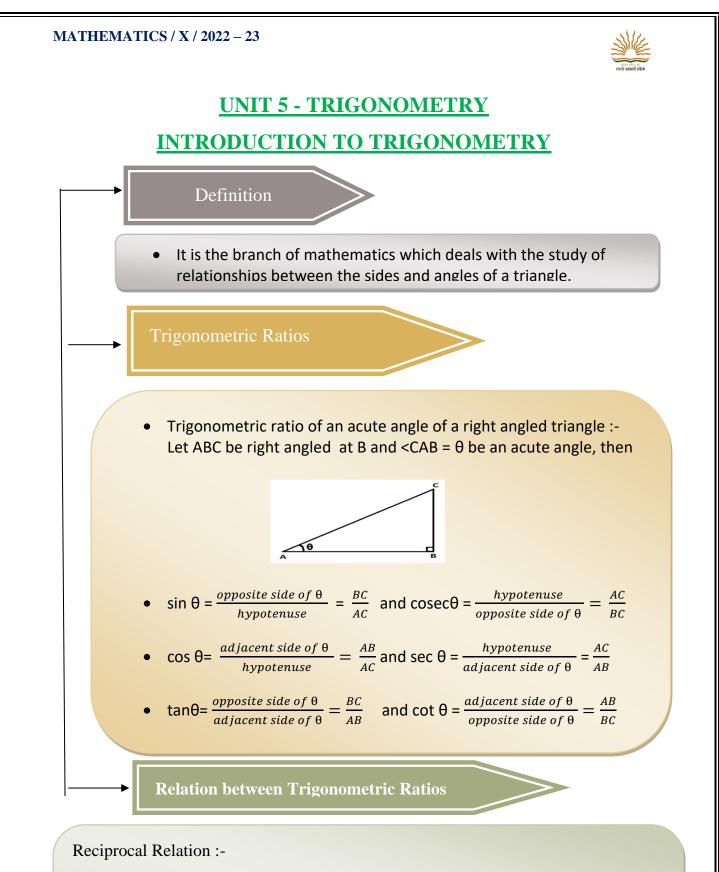
ANSWERS OF SECTION - A				
1. (d) 10	6. (a) 5	11. 5 units	16.	Inside the circle
		(13, 14)		
2. (b) 22	7. (d) 3:5 (5,8)	12. $y = -9$ or $y = 3$	17.	$k = \pm 4$
	(5, 8)			

119

(13, 26)



3. (d) $\sqrt{a^2 + b^2}$	8. (c) (2, 0)	13. 2:5	18.	BD = 5	
4. (c) -1	4. (c) -1 9. (b) (-4, 2)		19.	$\sqrt{3}7$ units	
5. (c) 1	10. (d) -1, 7	15. $p = 3$	20.	12	
	ANSWERS	OF SECTION - B	I		
1. (-7, 0)	6. bx = ay.	11. Yes	11. Yes		
2. 3	7. <i>y</i> = -1	12. Scalene	Triangle	17. 2:1	
3. Ratio is $2:1 \& k =$	$=\frac{2}{3}$ 8. (0,9)	13. $x - y = 2$	2	18. Yes	
4. t = 1	9. $\left(\frac{-2}{7}, \frac{-20}{7}\right)$	14. BC = (1	14. BC = $(1, 2)$ 19. uni		
5. $k = \frac{5}{2}$ or $k = 5:2$	10. (-4, - 7)	15. Absciss	15. Abscissa of $R = 1$		
	ANSWERS (OF SECTION - C	, ,		
1. Non- collinear	6. (-7,0)		11. (1,-12) a	and (5,-10)	
2. $y = 3$ or $y = -9$	7. (4,-5)	7. (4,-5)		12. Square	
3. 24 square units	8. (2, -5/3) an	id (0, -7/3)	13. k =1 a	nd (-3/2, 0)	
	4. $a = 1, b = 1$ $AB = CD = \sqrt{10}$ units $BC = AD = \sqrt{10}$ units $9. \left(-1, \frac{7}{2}\right), (0, 5),$		14. 2:9		
5. $x = 6$ and $y = 3$	10. $3x + y - 5 =$	= 0		or $x = -4$ and $\sqrt{41}$, PR = $\sqrt{82}$	



•
$$\sin \theta = \frac{1}{\cos ec\theta} \implies \cos ec\theta = \frac{1}{\sin \theta} \implies \sin \theta \cdot \csc \theta = 1$$

• $\cos \theta = \frac{1}{\cos ec\theta} \implies \sec \theta = \frac{1}{\sin \theta} \implies \cos \theta \cdot \sec \theta = 1$

secθ

•
$$\tan \theta = \frac{1}{\cot \theta} \implies \cot \theta = \frac{1}{\tan \theta} \implies \tan \theta . \cot \theta = 1$$

cos θ



MULTIPLE CHOICE QUESTIONS SECTION A

- Q1. If $\cos \theta = \frac{1}{2}$ then $\cos \theta$ -sec θ is equal to
- Q2. If $\sin \theta = x$ and $\sec \theta = y$, then $\tan \theta$ is equal to
- Q3. If $\cos A = \frac{3}{5}$, find the value of 9 +9 $\tan^2 A$

Q4. If $0 \le A$, $B \le 90^{\circ}$ such that $Sin A = \frac{1}{2}$ and $Cos B = \frac{1}{2}$, A + B =

- Q5. In a \triangle ABC, right angled at B, the value of Sin (A +C) is
- Q6. In \triangle ABC, right angled at B,sin A = $\frac{7}{25}$, then the value of cos C is
- Q7. If $\tan \theta = \sqrt{3}$, then the value of $\sec^2 \theta + \csc^2 \theta$ is
- Q8. If $\cos \theta = \frac{1}{\sqrt{2}}$, then the value of $\frac{1 + \tan \theta}{\sin \theta}$ is
- Q9. The value of $\sin^2 30^0 + \cos^2 45^0 + \cos^2 30^0$ is
- Q10. The value of $\sqrt{1 + \tan^2 \theta}$ is

VERY SHORT ANSWER QUESTIONS (1mark each)

- Q1. Find the value of $(\sin 30 + \cos 30) (\sin 60 + \cos 60)$
- Q2. If $\sin \theta$ Cos $\theta = 0$, find the value of θ
- Q3. $\triangle ABC$ is right angled at C, and $AC = \sqrt{3} BC$, prove that $\angle ABC = 60^{\circ}$
- Q4. If 2 Sin $3x = \sqrt{3}$, then find the value of x
- Q5. If Sin A + Sin²A=1 then find $\cos^2 A + \cos^4 A$

Q6. If
$$\tan(A - B) = \frac{1}{\sqrt{2}}$$
 and $\tan(A + B) = \sqrt{3}$, find the value of A and B

Q7. Evaluate $\frac{1-tan^2 \, 45^0}{1+tan^2 \, 45^0}$

Q8. If $\cos \alpha = \frac{1}{2}$ and $\tan \beta = \frac{1}{\sqrt{3}}$, find $\sin(\alpha + \beta)$ where α and β are both acute angles.

Q9. If $\sin \theta_1 + \sin \theta_2 + \sin \theta_3 = 3, 0 < \theta_1, \theta_2, \theta_3 \le 90^o$, find the value of $\cos \theta_1 + \cos \theta_2 + \cos \theta_3$

Q10. If $(1 + \sin A)(1 - \sin A) = \frac{3}{4}$, find the value of sec A

SHORT ANSWER TYPE QUESTIONS (2marks questions) SECTION B

- Q1. If $\tan\beta = \frac{24}{7}$, then the value of $\sin\beta + \cos\beta$ is
- Q2. If $\tan 3x = \sin 45^{\circ} \cos 45^{\circ} + \sin 30^{\circ}$ then value of x is



- Q3. In triangle ABC ,right angled triangled at B, AB =5cm and $<ACB=30^{\circ}$, then the length of the side AC is
- Q4. Given that the $\sin\beta = \sqrt{3/2}$ and the $\cos\alpha = 0$, then the value of $\beta \alpha$ is
- Q5. In a triangle ABC i, right angled at C if $<A=30^{\circ}$, AB=40 units find BC
- Q6. The value of $\frac{\cos 30 + \sin 60}{1 + \cos 60 \sin 30}$
- Q7. If in a triangle ABC right angled at B, AB =6 units and BC=8 units then the value of the sinA cosC+cosAsinC
- Q8. In triangle OPQ, right angled at P, OP= 7*cm*, and the OP-PQ= 1*cm*, the value of sinQ is
- Q9. If $x = 2\cos^2 \alpha$ and $y = 2\sin^2 \alpha + 1$ then the value of x + y
- Q10. If $\tan \beta = \frac{a}{b}$, then the value of
- Q11. In triangle ABC right angled at B if <A= <C then value of sinA sinB + cos A cosB will be
- Q12. Triangle PQR is right angled at Q, if PQ =5cm and RQ = 10cm then the value of sinP x cosP is
- Q13. If $\sec \alpha = 5/7$, then the value of $\frac{1-tana}{1+tana}$
- Q14. The value of $(\sin \alpha + \cos \alpha)^2 + (\cos \alpha \sin \alpha)^2$
- Q15. In right triangle ABC, right angled at B, $\langle ACB = \emptyset, AB = 2 \text{ cm} \text{ and } BC = 1 \text{ cm} \text{ then}$ the value of $\sin^2 \emptyset + \tan^2 \emptyset$

Q16. If 4tan $\alpha = 3$ find the value of $\frac{5sina - 3\cos a}{5\sin a + 2\cos a}$

Q17. The value of α and β if sin $(\alpha + 2\beta) = \sqrt{3}/2$ and cos $(\alpha + 4\beta) = 0$

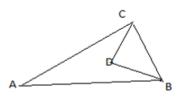
Q18. If
$$\cot \alpha = 7/8$$
, then the value of $\frac{(1+\sin \alpha)(1-\sin \alpha)}{(1+\cos \alpha)(1-\cos \alpha)}$

- Q19. If 8tanx=15 then find sinx cosx
- Q20. In triangle PQR right angled at Q, PQ= 3 cm and PR = 6cm Determine $\angle PRQ$

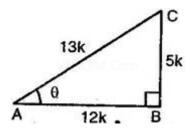
SHORT ANSWER TYPE QUESTIONS (3marks questions) SECTION C

- Q1. In \triangle DEF, $\angle E = 90^\circ$, DF DE =2 cm and EF = 6 cm. Find cos D + sin D.
- Q2. In the figure, $\angle ACB = 90^\circ$, $\angle BDC = 90^\circ$, CD = 4 cm, BD = 3 cm and AC = 12 cm. Find Cos A – Sin A

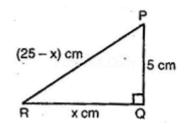




Q3. Given sec $\Theta = \frac{13}{12}$, calculate all other trigonometric ratios.



Q4. In \triangle PQR, right angled at Q, PR + QR = 25 cm and PQ = 5 cm. Determine the values of sin P, cos P and tan P



Q5. Express the trigonometric ratios sin A, sec A and tan A in terms of cot A.

Q6. Prove that
$$\frac{\cot\theta - \tan\theta}{\cos\theta\sin\theta} = \csc^2\theta - \sec^2\theta$$

- Q7. Prove that $(cot\theta cosec\theta)^2 = \frac{1 cos\theta}{1 + cos\theta}$
- Q8. Prove that: $(\csc \Theta \sin \Theta) (\sec \Theta \cos \Theta) (\tan \Theta + \cot \Theta) = 1$

Q9. Prove that: $\frac{\cos A}{1-\tan A} + \frac{\sin A}{1-\cot A} = \sin A + \cos A$

Q10. If $\tan A + \cot A = 2$, then find the value of $\tan^2 A + \cot^2 A$

Q11. If b cos
$$\theta$$
 = a, then Prove that Cosec θ + Cot $\theta = \sqrt{\frac{b+a}{b-a}}$

Q12. If
$$\sin \theta = \frac{3}{5}$$
 evaluate $\frac{\csc \theta - \cot \theta}{2 \cot \theta}$

Q13. Evaluate:
$$\frac{2\cos^2 60+3\sec^2 30-2\tan^2 45}{\sin^2 30+\cos^2 45}$$

Q14. If $sin(A+2B) = \frac{\sqrt{3}}{2}$ and cos(A+4B) = 0. A > B and $(A+4B) \le 90$. Then find the value of A and B

Q15. Prove that
$$\frac{\sin\theta}{1+\cos\theta} + \frac{1+\cos\theta}{\sin\theta} = 2 \csc\theta$$



LONG ANSWER TYPE QUESTIONS (4 MARK QUESTIONS) SECTION D

Q1. If sin (A+B) =1 and tan (A+B) = $\frac{1}{\sqrt{3}}$. Find the value of

(i) $\tan A + \cot B$

(ii) sec A + cosec B

Q2. Prove that : $\frac{\tan^3\theta}{1+\tan^2\theta} + \frac{\cot^3\theta}{1+\cot^2\theta} = \sec\theta\csc\theta - 2\sin\theta\cos\theta$

Q3. If cosec A + cot A = m, Show that $\frac{m^2-1}{m^2+1} = \cos A$

Q4. Evaluate: $4 (\sin^4 30^\circ + \cos^4 60^\circ) - 3 (\cos^4 45^\circ - \sin^4 90^\circ)$

Q5. RPQ is a right-angled triangle at Q. If
$$PQ = 5$$
 cm and $RQ = 10$ cm, find

- (i) $\sin^2 P$
- (ii) $\cos^2 R$ and $\tan R$
- (iii) $\sin P x \cos P$
- (iv) $\sin^2 P \cos^2 P$

Q6. If $\sec \theta + \tan \theta = p$, then find the value of $\csc \theta$

Q7. If $2 \csc^2 30^\circ + Y \sin^2 60^\circ - \frac{3}{4} \tan^2 30^\circ = 10$, find value of Y

Q8. If
$$a \sin^2 x + b \cos^2 x = c$$
, $b \sin^2 y + a \cos^2 y = d$ and $a \tan X = b \tan Y$, then find $\frac{a^2}{b^2}$

Q9. Prove that :
$$\sqrt{\frac{1+\sin\theta}{1-\sin\theta}} + \sqrt{\frac{1-\sin\theta}{1+\sin\theta}} = 2\sec\theta$$

Q10. In an acute angled triangle ABC, if $sin (A+B-C) = \frac{1}{2} and cos (B+C-A) = \frac{1}{\sqrt{2}}$. Find $\angle A, \angle B, \angle C$

CASE STUDY BASED QUESTIONS

CASE STUDY QUESTION 1

Doing swing ball in a cricket match turns the ball and can put the batsman in danger. Our two famous bowlers Ashwin and Akash, throws the ball at an angle of A and B respectively. The relation between A and B are such that $sin(A - B) = \frac{1}{2}$ and cos(A + B) = 0, $0^{\circ} < A + B \le 90^{\circ}$, A > B

- 1. What is the measure of $\angle A$?
 - (a) 30° (b) 45° (c) 60° (d) 90°
- 2. What is the measure of $\angle B$?



(d)

(a) 30° (b) 45° (c) 60°

90°

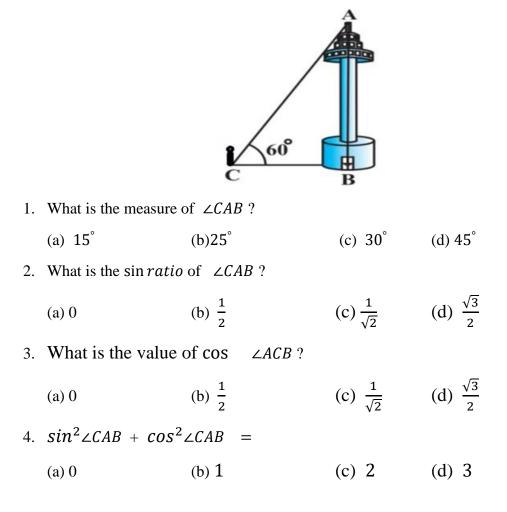
3. Now on the bases of value of A and B derived find cosec (A - B)

- (a) 0 (b) 2 (c) $\sqrt{2}$ (d) $\frac{2}{\sqrt{3}}$
- 4. What is the value of sec *B*?
 - (a) 0 (b) 1 (c) \propto (d) $\frac{2}{\sqrt{3}}$
- 5. If $sin\theta = \frac{a}{b}$, then $cos\theta$ is equal to:

(a) $\frac{b}{\sqrt{b^2 - a^2}}$ (b) $\frac{b}{a}$ (c) $\frac{a}{\sqrt{b^2 - a^2}}$ (d) $\frac{\sqrt{b^2 - a^2}}{b}$

CASE STUDY QUESTION 2

In the month of November, Akshay notices a tower built near his colony's playground. He sees that it is being held by a wire, attached to the top of the tower. The wire makes an angle of 60° with the ground. Using these Information find the answers to the following questions

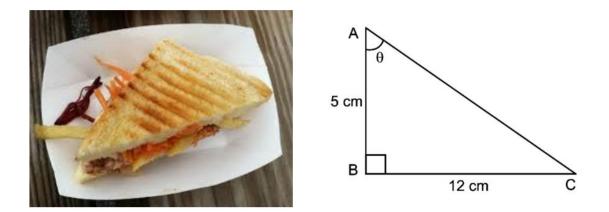




- 5. What is the value of tan 90?
 - (a) 0 (b) 1 (c) $\frac{1}{2}$ (d) not defined

CASE STUDY 3

Mohan, a class X student is a big foodie. Once his mother has made a sandwich for him. A thought has come into his mind by seeing a piece of sandwich. He thought if he increases the base length and height, he can eat a bigger piece of sandwich.



Answer the following questions accordingly:

- 1. If the length of the base is 12 cm and the height is 5 cm then the length of the hypotenuse of that sandwich is:
 - (a) 17 cm (b) 7 cm (c) 169 cm (d) 13
- 2. 2. What will be the value of cosine of the angle between hypotenuse and the height of sandwich?
 - (a) $\frac{5}{13}$ cm (b) $\frac{12}{13}$ cm (c) $\frac{13}{5}$ cm (d) $\frac{13}{12}$ cm
- 3. If he increases the base length to 15 cm and the hypotenuse to 17 cm, then the height of the sandwich is :
 - (a) 7 cm (b) 8 cm (c) 32 cm (d) none of

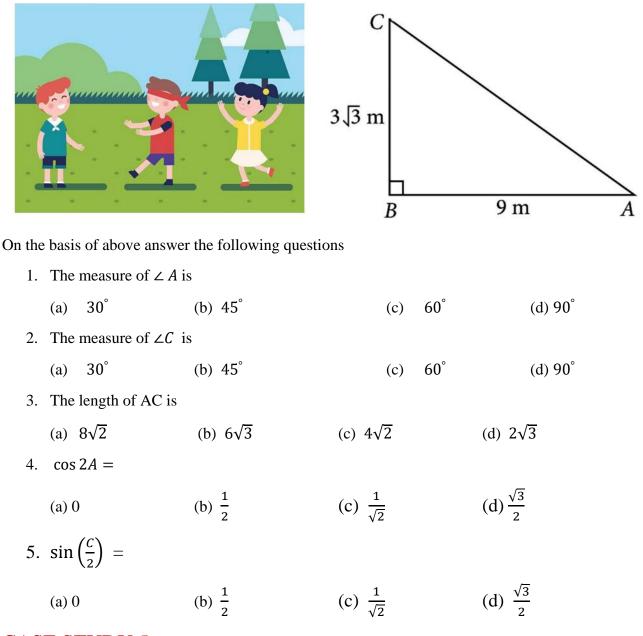
these

- 4. If the value of tan θ is $\sqrt{3}$, then sin- equals to:
 - (a) $\frac{1}{\sqrt{2}}$ (b) $\frac{\sqrt{3}}{2}$ (c) $\frac{1}{2}$ (d) 1
- 5. The value of $\tan 45^\circ + \cot 45^\circ$
 - (a) 1 (b) 2 (c) 3 (d) 4

CASE STUDY 4



Three friends Ashwin, Bhagath & Amal are playing hide and seek in a park. Ashwin, Bhagath hide in the shrubs and Amal have to find both of them. If the positions of three friends are at A, B and C respectively as shown in the figure and forms a right-angled triangle, such that AB =9 m, BC= $3\sqrt{3}$ m and $\angle B = 90^\circ$. Now answer the following questions

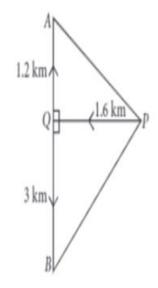


CASE STUDY 5

Two aeroplanes leave an airport, one after the other. After moving on runway, one flies due North and other flies due South. The speed of two aeroplanes are 400 km/hr and 500 km/hr respectively. Considering PQ as runway and A and B are any points in the path followed by two planes







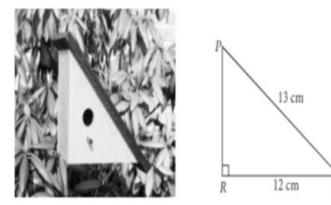
On the basis of above answer the following questions

1.	Find $\tan \theta$, if $\angle AP$	Q= heta		
	(a) $\frac{3}{4}$	(b) $\frac{1}{2}$	(c) $\frac{1}{\sqrt{2}}$	(d) $\frac{\sqrt{3}}{2}$
2.	Find the value of co	ot B		
	(a) $\frac{3}{4}$	(b) $\frac{15}{4}$	(c) $\frac{3}{8}$	(b) $\frac{15}{8}$
3.	Find the value of tar	n A		
	(a) $\frac{3}{4}$	(b) $\frac{4}{3}$	(c) $\frac{1}{\sqrt{2}}$	(d) $\frac{\sqrt{3}}{2}$
4.	Find the value of sec	A		
	(a) 0	(b) $\frac{5}{3}$	(c) $\frac{1}{\sqrt{2}}$	(d) $\frac{\sqrt{3}}{2}$
5.	Find cosec B			
	(a) $\frac{17}{8}$	(b) $\frac{8}{17}$	(c) $\frac{12}{5}$	(d) $\frac{5}{12}$

CASE STUDY 6

Raji a student of class10 has to made a project. She decides to make a bird house which is triangular in shape. She uses cardboard to make the bird house as shown in the figure. Considering the front side of bird house as a right-angled triangle PQR, right angled at R, answer the following questions



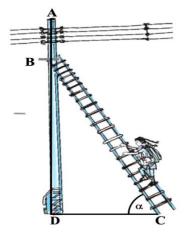


On the basis of above answer the following questions

- 1. If $\angle PQR = \theta$, the $\cos \theta =$
 - (a) $\frac{12}{13}$ (b) $\frac{13}{12}$ (c) $\frac{12}{5}$ (d) $\frac{5}{12}$
- 2. Find the value of sec θ
 - (a) $\frac{12}{13}$ (b) $\frac{13}{12}$ (c) $\frac{12}{5}$ (d) $\frac{5}{12}$
- 3. Find the value of $\frac{\tan\theta}{1+\tan^2\theta}$
 - (a) $\frac{60}{169}$ (b) $\frac{169}{60}$ (c) $\frac{12}{5}$ (d) $\frac{5}{12}$
- 4. The value of $\cot^2 \theta \csc^2 \theta$ (a) 0 (b) 1 (c) 2 (d) -1
- 5. The value of $sin^2\theta + cos^2\theta$ (a) 0 (b) 1 (c) 2 (d) -1

CASE STUDY 7

Raj is an electrician in a village. One day power was not there in entire village and villagers called Raj to repair the fault. After thorough inspection he found an electric fault in one of the electric pole of height 5 m and he has to repair it. He needs to reach a point 1.3m below the top of the pole to undertake the repair work





On the	basis of above, answe	er the following questi	on	
1.	When the ladder is in horizontal, find the ar	_	α such that $\sqrt{3}$ ta	an $\alpha + 2 = 5$ to the
	(a) 30°	(b)45°	(c) 60°	(d) 90°
2.	How far from the foo 1.73)	ot of the pole should h	e place the foot	of the ladder? (Use 3 =
	(a) 2.89 m	(b) 2.14 m	(c) 3 m	(d) none of these
3.	In the above situation	, find the value of <i>si</i>	$n \propto \cos \frac{\alpha}{2} - \cos \frac{\alpha}{2}$	$s \propto sin \frac{\alpha}{2}$
	(a) 0	(b) 1	(c) $\frac{1}{2}$	(d) none of these

4. In the above situation if BD = 3 cm and BC = 6 cm. Find α

- (a) 45° (b) 30° (c) 60° (d) none of these
- (a) $\frac{17}{15}$ (b) $\frac{15}{17}$ (c) $\frac{15}{8}$ (d) $\frac{8}{17}$

ANSWERS

MULTIPLE CHOICE QUESTIONS SECTION – A

5. If $15 \cot \alpha = 8$. The value of $\sin \alpha$ is

Q NO	ANSWERS	Q NO	ANSWER
Q1.	(b) $\frac{-3}{2}$	Q6.	(d) 7
Q2.	(a) xy	Q7.	(d) 8
Q3.	(c) 25	Q8.	(a)
Q4.	(c) 90°	Q9.	(c)
Q5.	(b)1	Q10.	(b)

VERY SHORT ANSWER

Q NO	ANSWER
1	$(\sin 30 + \cos 30) - (\sin 60 + \cos 60) = \frac{1}{2} + \frac{\sqrt{3}}{2} - \frac{\sqrt{3}}{2} - \frac{1}{2} = 0$
2	$\sin\theta$ - $\cos\theta$ =0,
	There fore $\sin\theta = \cos\theta, \theta = 45$
3	Tan B = $\frac{AC}{BC} = \frac{\sqrt{3}BC}{BC} = \sqrt{3}$ Tan 60 = $\sqrt{3}$, there fore <b =60<="" td="">
4	$2 \sin 3x = \sqrt{3}, \sin 3x = \frac{\sqrt{3}}{2}$
	Sin $60 = \frac{\sqrt{3}}{2}$, $3x = 60$, there fore $x = \frac{60}{3} = 20$



5		$\sin^2 A = \cos^2 A$ $\cos^4 A$, ThereforeCo	$\cos^2 A + \cos^4 A = \sin^2 A$	$\mathbf{A} + \mathbf{Sin}^2 \mathbf{A} = 1$
6	tan(A – B	$() = \frac{1}{\sqrt{3}}$, A - B =	$= 30^{0}$ (1)	
		$(+B) = \sqrt{3}$, A + B =		
		$A = 45^{0}$ and $B = 15^{0}$		
7	$1 - tan^2 45^0$	1-1 0		
	$\frac{1 \tan 45}{1 + \tan^2 45^0}$	$=\frac{1-1}{1+1} = \frac{0}{2} = 0$ $\alpha = 60^{0}$		
8	$\cos \alpha = \frac{1}{2}$	$\ldots \alpha = 60^{0}$		
	$\tan \beta =$	$\frac{1}{\sqrt{3}}$ $\beta = 30^{0}$		
		$(\beta^{0} + \beta^{0}) = \text{Sin} (60^{0} + \beta^{0})$		
9	$\cos \theta_1 + c$	$\cos\theta_2 + \cos\theta_3 = 0 +$	-0+0=0	
10	(1 + sin A	$(1 - \sin A) = \frac{3}{4}$		
		$n^2 A = \frac{3}{4}$		
		$A = \frac{3}{4}^{4}$		
		$\frac{4}{3}$		
	$\cos A = \sqrt{\frac{3}{4}}$			
	$\cos A = \frac{\sqrt{3}}{2}$			
	Sec A = $\frac{2}{\sqrt{3}}$			
		√3		
SHOR	T ANSWEI	R TYPE -SECTION	N - B	
Q NO		ANSWER	Q NO	ANSWER
1		31/25	11	1/√2
2		15°	12	2/5
3		10	13	1/7
4		30°	14	2
5		20 UNITS	15	24/5
6		4\sqrt{3}/5	16	3/23
7		1	17	$\alpha = 30^{\circ}, \beta = 15^{\circ}$
8		7/25	18	49/64
9		3	10	7/17
10		-	19	7/17
		$(a^2 + b^2)/(a^2 - b^2)$	20	7/17 30°
SHOR		-	20	
SHOR 1	1.4	$(a^2 + b^2)/(a^2 - b^2)$	20	
SHOR	1.4	$(a^2 + b^2)/(a^2 - b^2)$	20	
SHOR 1	1.4	$(a^2 + b^2)/(a^2 - b^2)$	20	
SHOR 1	$ \begin{array}{c} 1.4 \\ \overline{7} \\ \overline{13} \end{array} $	(a ² + b ²)/(a ² -b ²) R TYPE SECTION	20	
SHOR 1 2	1.4	$\frac{(a^2 + b^2)/(a^2 - b^2)}{R \text{ TYPE SECTION}}$	20	



	$\tan \Theta = \frac{5}{12} \qquad \cot \Theta = \frac{12}{5}$
4	$\sin P = \frac{12}{13}$ $\cos P = \frac{5}{13}$
	$\tan P = \frac{12}{5}$
5	$\sin A = \frac{1}{\sqrt{(\cot^2 A + 1)}}$ $\tan A = \frac{1}{\cot A}$
	$\sec A = \frac{\sqrt{(\cot^2 A + 1)}}{\cot A}$
6	Correct proof
7	Correct proof
8	Correct proof
9	Correct proof
10	2
11	Proof
12	1/8
13	10/3
14	$A = 30^{\circ}, B = 15^{\circ}$
15	Proof
LONG	ANSWER TYPE SECTION - D
1.	1. $\sin(A+B) = 1$
	$\sin(A+B) = \sin 90^{\circ}$
	$A+B = 90^{\circ} \qquad \dots $
	$\tan (A - B) = \frac{1}{\sqrt{3}}$
	1-
	$\tan (A - B) = \tan 30^{\circ}$
	$A - B = 30^{\circ}$ (2)
	Solving equation (1) and (2) for A and B W
	We get $A = 60^{\circ}$ and $B = 30^{\circ}$
	(i) $\tan A + \cot B$ = $\tan 60^\circ + \cot 30^\circ$
	$= \tan 30^\circ + \cot 30^\circ$ $= \sqrt{3} + \sqrt{3}$
	$= 2\sqrt{3}$
	(ii) $\sec A - \csc B$ = $\sec 60^\circ - \csc 30^\circ$
	$= \sec 60^{\circ} - \csc 50^{\circ}$ $= 2 - 2^{\circ}$
	= 2 - 2 $= 0$
2	
2	$1. \ \frac{\tan^3\theta}{1+\tan^2\theta} + \frac{\cot^3\theta}{1+\cot^2\theta}$
l	



	$= \frac{\tan^{3}\theta}{\sec^{2}\theta} + \frac{\cot^{3}\theta}{\csc^{2}\theta}$ $= \frac{\sin^{3}\theta}{\cos^{3}\theta} \cos^{2}\theta + \frac{\cos^{3}\theta}{\sin^{3}\theta} \sin^{2}\theta$ $= \frac{\sin^{3}\theta}{\cos^{3}\theta} + \frac{\cos^{3}\theta}{\sin^{9}\theta}$ $= \frac{\sin^{4}\theta + \cos^{4}\theta}{\sin^{9}\theta \cos^{9}\theta}$ $= \frac{(\sin^{2}\theta)^{2} + (\cos^{2}\theta)^{2}}{\sin^{9}\theta \cos^{9}\theta}$ (using $a^{2} + b^{2} = (a+b)^{2} - 2ab$) $= \frac{(\sin^{2}\theta + \cos^{2}\theta)}{\sin^{9}\theta \cos^{9}\theta}$ $= \frac{1 - 2\sin^{2}\theta \cos^{2}\theta}{\sin^{9}\theta \cos^{9}\theta}$ $= \frac{1}{\sin^{9}\theta \cos^{9}\theta} - \frac{2\sin^{2}\theta \cos^{2}\theta}{\sin^{9}\theta \cos^{9}\theta}$
3	$= \sec\theta \csc\theta - 2 \sin\theta \cos\theta$ $LHS = \frac{m^2 - 1}{m^2 + 1}$ $= \frac{(\csc A + \cot A)^2 - 1}{(\csc c A + \cot A)^2 + 1}$ $= \frac{\csc^2 A + \cot^2 A + 2 \csc c A \cot A - 1}{\csc^2 A + \cot^2 A + 2 \csc c A \cot A + 1}$ $= \frac{(\csc^2 A - 1) + \cot^2 A + 2 \csc c A \cot A}{\csc^2 A + (1 + \cot^2 A) + 2 \csc c A \cot A}$ $= \frac{\cot^2 A + \cot^2 A + 2 \csc c A \cot A}{\csc^2 A + \csc^2 A + 2 \csc c A \cot A}$ $= \frac{2 \cot^2 A + 2 \csc^2 A + 2 \csc c A \cot A}{2 \csc^2 A + 2 \csc^2 A + 2 \csc c A \cot A}$ $= \frac{2 \cot^2 A + 2 \csc c A \cot A}{2 \csc^2 A + 2 \csc c A \cot A}$ $= \frac{2 \cot^2 A + 2 \csc c A \cot A}{2 \csc^2 A + 2 \csc c A \cot A}$ $= \frac{2 \cot^2 A + 2 \csc c A \cot A}{2 \csc^2 A + 2 \csc c A \cot A}$ $= \frac{2 \cot A (\cot A + \csc A)}{2 \csc c A (\cot A + \csc A)}$ $= \frac{\cot A}{\csc c A}$ $= \frac{\cot A}{\csc c A} = \cos A = RHS$
4	$\frac{\sin 4 \csc 2 x}{1. 4 (\sin^4 30^\circ + \cos^4 60^\circ) - 3 (\cos^4 45^\circ - \sin^4 90^\circ)} = 4 \left[\left(\frac{1}{2}\right)^4 + \left(\frac{1}{2}\right)^4 \right] - 3 \left[\left(\frac{1}{\sqrt{2}}\right)^2 - 1^2 \right] = 4 \left[\frac{1}{16} + \frac{1}{16} \right] - 3 \left[\frac{1}{2} - 1 \right] = 4 x \frac{2}{16} - 3 x - \frac{1}{2} = \frac{1}{2} + \frac{3}{2} = 2$
5	2. In right angled triangle RPQ , $\langle Q = 90^{\circ}$ PR ² = 10 ² + 5 ²



	$PR^2 = 125$
	$PR = 5\sqrt{5} \text{ cm}$
	(i) $\sin^2 P = (\frac{10}{5\sqrt{5}})^2 = \frac{4}{5}$
	5 1 5
	(ii) $\cos^2 R = = \left(\frac{10}{5\sqrt{5}}\right)^2 = \frac{4}{5}$ and $\tan R = \frac{1}{2}$
	(iii) $\sin P x \cos P = \frac{2}{5}$
	(iv) $\sin^2 P - \cos^2 P = \frac{4}{5} - \frac{1}{5} = \frac{3}{5}$ $\sec \theta + \tan \theta = p$ (1)
6	$\sec\theta + \tan\theta = p$ (1)
	$sec^2\theta - tan^2\theta = 1$
	$(\sec\theta + \tan\theta) (\sec\theta - \tan\theta) = 1$
	$P(\sec\theta - \tan\theta) = 1$
	$\sec\theta + \tan\theta = \frac{1}{p}$ (2)
	adding (1) and (2) we get,
	$2 \sec \theta = p + \frac{1}{p}$
	$\sec \theta = \frac{P^2 + 1}{2P}$
	on subtracting (2) from (1), we get
	$2 \tan \theta = p - \frac{1}{p}$
	$\tan\theta = \frac{P^2 - 1}{2P}$
	$\frac{\sec\theta}{\tan\theta} = \frac{\frac{P^2+1}{P^2-1}}{\frac{P^2-1}{P^2-1}}$
	$\frac{\frac{1}{\cos\theta}}{\frac{\sin\theta}{2}} = \frac{P^2 + 1}{P^2 - 1}$
	$\frac{\cos\theta}{1} \qquad P^2 + 1$
	$\frac{1}{\sin\theta} = \frac{P^2 + 1}{P^2 - 1}$
	$\operatorname{Cosec} \theta = \frac{P^2 + 1}{P^2 - 1}$
7	$2 \operatorname{cosec}^2 30^\circ + Y \sin^2 60^\circ - \frac{3}{4} \tan^2 30^\circ = 10$
	$2 \ge 2^2 + Y \left(\frac{\sqrt{3}}{2}\right)^2 - \frac{3}{4} \left(\frac{1}{\sqrt{3}}\right)^2 = 10$
	$8 + Y \frac{3}{4} - \frac{1}{4} = 10$
	$\frac{3Y}{10} - \frac{4}{10} \frac{4}{8} + \frac{1}{10}$
	$\frac{\frac{3Y}{4}}{\frac{3Y}{4}} = \frac{10}{4} - 8 + \frac{1}{4}$ $\frac{\frac{3Y}{4}}{\frac{9}{4}} = \frac{9}{4}$
	$\frac{1}{4} = \frac{1}{4}$
8	Y = 3 1. dividing equation a sin ² x+b cos ² x = c
	by $\cos^2 x$



	$a \tan^2 x + b = c \sec^2 x$
	\Rightarrow a tan ² x +b =c(1+tan ² x)
	\Rightarrow a tan ² x + b = c + c tan ² x
	$=\tan^2 x(a-c) = c - b$
	$\tan^2 x = \frac{c-b}{a-c}$
	Similarly, dividing equation $b \sin^2 y + a \cos^2 y = d$
	by $\cos^2 y$
	$b \tan^2 y + a = d \sec^2 y$
	$\Rightarrow b \tan^2 y + a = d(1 + \tan^2 y)$
	\Rightarrow b tan ² y + a = d + d tan ² y
	\Rightarrow tan ² y (b - d) =d-a
	$=\tan^2 y = \frac{d-a}{b-d}$
	Now, a tanx=b tany
	$\Rightarrow a^2 \tan^2 x = b^2 \tan^2 y$
	$\Rightarrow \frac{a^2}{b^2} = \frac{\tan^2 y}{\tan^2 x}$
	$\Rightarrow \frac{a^2}{b^2} = \frac{\frac{d-a}{b-d}}{\frac{c-b}{c-b}}$
	a – c
	$\Rightarrow \frac{a^2}{b^2} = \frac{(d-a)(a-c)}{(b-d)(c-b)}$
9	$\sqrt{1+\sin\theta}$ $\sqrt{1-\sin\theta}$
	$\sqrt{\frac{1}{1-\sin\theta}} + \sqrt{\frac{1}{1+\sin\theta}}$
	$\sqrt{1+\sin\theta}$ $1+\sin\theta$ $\sqrt{1-\sin\theta}$ $1-\sin\theta$
	$=\sqrt{\frac{1+\sin\theta}{1-\sin\theta}}\times\frac{1+\sin\theta}{1+\sin\theta}+\sqrt{\frac{1-\sin\theta}{1+\sin\theta}}\times\frac{1-\sin\theta}{1-\sin\theta}$
	$\sqrt{(1+\sin\theta)^2}$ $\sqrt{(1-\sin\theta)^2}$
	$= \sqrt{\frac{(1+\sin\theta)^2}{1^2-\sin^2\theta}} + \sqrt{\frac{(1-\sin\theta)^2}{1^2-\sin^2\theta}}$
	As we know $\sin^2 A + \cos^2 A = 1$
	As we know $stat A + \cos A = 1$



Case	based o	question
Sl.no		Answers
		$\sqrt{\frac{(1+\sin\theta)^2}{\cos^2\theta}} + \sqrt{\frac{(1-\sin\theta)^2}{\cos^2\theta}}$
		$=\sqrt{(\frac{(1+\sin\theta)}{\cos\theta})^2} + \sqrt{(\frac{(1-\sin\theta)}{\cos\theta})^2} = \frac{1+\sin\theta}{\cos\theta} + \frac{1-\sin\theta}{\cos\theta}$
		$=\frac{1}{\cos\theta} + \frac{\sin\theta}{\cos\theta} + \frac{1}{\cos\theta} - \frac{\sin\theta}{\cos\theta} = \frac{2}{\cos\theta} = 2\sec\theta$ $= RHS$
	10	$\angle A + \angle B + \angle C = 180^{\circ}$
		$\angle A + \angle B = 180^{\circ} - \angle C$
		$\angle B + \angle C = 180^{\circ} - \angle A$
		$\sin (A+B-C) = \frac{1}{2}$
		A+B-C =30°
		$180^{\circ} - C - C = 30^{\circ}$
		CASE BASED QUESTIONS

Q.no 1 (1)	c
	a
(2) (3) (4) (5)	b
(4)	d
(5)	d
Q.no 2(1)	c
(2)	b
(2) (3) (4)	b
(4)	b
(5)	d
Q.no 3(1)	d
(2)	a
(3)	b
(4)	b
(2) (3) (4) (5)	b
Q.no 4(1)	a
(2)	c
(2) (3)	b

(4)	b
(5)	b
Q.no 5 (1)	a
(2)	d
(3)	b
(4)	b
(2) (3) (4) (5)	a
Q.no 6 (1)	a
(2)	b
(3) (4) (5)	a
(4)	d
(5)	b
Q.no 7 (1)	c
(2)	b
(2) (3)	с
(4) (5)	b
(5)	b

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SOME APPLICATIONS OF TRIGONOMETRY

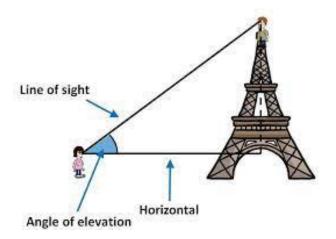
HEIGHTS AND DISTANCES: Trigonometry is used for finding the heights and distances of various objects, without measuring them.

Line of sight is the line drawn from the eye of the observer to the point on the object viewed by the observer.

Horizontal level is the horizontal line through the eye of the observer.

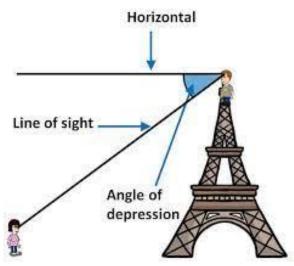
ANGLE OF ELEVATION

The angle of elevation is relevant for objects above horizontal level. It is the angle formed by the line of sight with the horizontal level.



ANGLE OF DEPRESSION

The angle of depression is relevant for objects below horizontal level. It is the angle formed by the line of sight with the horizontal level.



IMPORTANT POINTS TO REMEMBER:

In this right triangle $\angle B = 90^\circ$. If we take $\angle A$ as acute angle, then -

AB is the base, as the side adjacent to the acute angle. BC is the perpendicular, as the side opposite to the acute angle. AC is the hypotenuse, as the side opposite to the right angle.

Trigonometric ratios with respect to $\angle A$

	1			
RATIO	FORMULA	VALUE	ALTERNATIVE	SHORT FORM
			FORMULA	
sin A	opposite	BC	perpendicular	Р
	hypotenuse	\overline{AC}	hypotenuse	\overline{H}
	, p		ny povontaso	
cos A	adjacent	AB	base	В
	hypotenuse	\overline{AC}	hypotenuse	\overline{H}
tan A	opposite	BC	perpendicular	Р
	adjacent	\overline{AB}	base	\overline{B}
	,			
cosec A	hypotenuse	AC	hypotenuse	Н
	opposite	BC	perpendicular	\overline{P}
	L L		L L	
sec A	hypotenuse	AC	hypotenuse	Н
	adjacent	\overline{AB}	base	\overline{B}
cot A	adjacent	AB	base	В
	opposite	BC	perpendicular	\overline{P}
	000000	20	perpendiculu	-

Hypotenuse

Adjacent

Opposite

RECIPROCAL RELATION BETWEEN TRIOGONOMETRIC RATIOS

$\sin A = \frac{1}{\operatorname{Cosec} A}$	$\operatorname{cosec} A = \frac{1}{\sin A}$	$\sin A. \cos A = 1$
$\cos A = \frac{1}{\sec A}$	$\sec A = \frac{1}{\cos A}$	cos A. sec A=1
$\tan A = \frac{1}{\cot A}$	$\cot A = \frac{1}{\tan A}$	tan A. cot A= 1

QUOTIENT RELATION

tan A	sin A	
tall A	Cos A	
cot A	_cos A	
COL A		

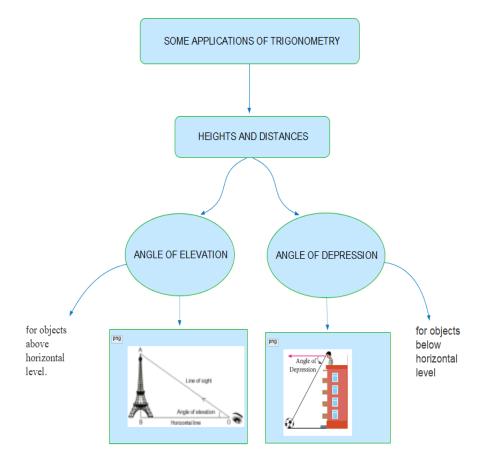
TRIGONOMETRIC RATIOS OF SOME SPECIFIC ANGLES



Trigonometry Table

				1	
	0°	30°	45°	60°	90°
sin $ heta$	0	$\frac{1}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{\sqrt{3}}{2}$	1
cos θ	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	0
tan θ	0	$\frac{1}{\sqrt{3}}$	1	$\sqrt{3}$	Not defined
cosec $ heta$	Not defined	2	$\sqrt{2}$	$\frac{2}{\sqrt{3}}$	1
sec $ heta$	1	$\frac{2}{\sqrt{3}}$	$\sqrt{2}$	2	Not defined
cot $ heta$	Not defined	$\sqrt{3}$	1	$\frac{1}{\sqrt{3}}$	0

MIND MAP



Choose the correct answer:(MCQ)

 The angle of elevation of the top of a tower from a point on the ground, which is 20m away from the foot of the tower is 60⁰. Find the height of the tower.

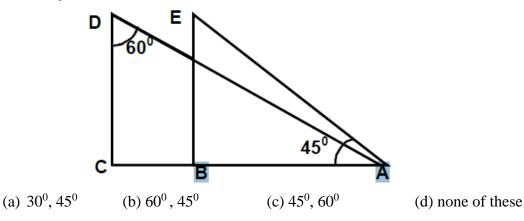
(a) $10\sqrt{3}$ m (b) $30\sqrt{3}$ m (c) $20\sqrt{3}$ m (d) none of these.



2. The angle of elevation of a ladder leaning against a wall is 60^0 and the foot of the ladder is 9.5 m away from the wall. Find the length of the ladder.

(a) 10 m (b) 19 m (c) 20 m (d) none of these

- 3. If the ratio of the height of a tower and the length of its shadow is $\sqrt{3:1}$, what is the angle of elevation of the Sun?
 - (a) 30^{0} (b) 60^{0} (c) 45^{0} (d) none of these
- 4. In the figure given below, what are the angles of depression from the observing positions D and E of the object A?



5. If the angle of elevation of a tower from a distance of 100m from its foot is 600, then the height of the tower is

(a) $100\sqrt{3}$ m (b) $200/\sqrt{3}$ m (c) $50\sqrt{3}$ m (d) $100/\sqrt{3}$ m

A tower is 50m high, its shadow ix 'x' metres shorter when the sun's altitude is 45⁰ than when it is 30⁰. Find the value of 'x'

(a) $100\sqrt{3}$ m (b) $200/\sqrt{3}$ m (c) $50\sqrt{3}$ m (d) $50(\sqrt{3}-1)$ m

7. A 1.5m tall boy stands at a distance of 2m from lamp post and casts a shadow of 4.5m on the ground. Find the height of the lamp post.

(a) 3 m (b) 2.5 m (c) 5 m (d) none of these

8. The tops of two poles of height 20m and 14m are connected by a wire. If the wire makes an angle of 30^{0} with horizontal, then the length of the wire is

(a) 12 m (b) 10 m (c) 8 m (d) 6 m

9. If the angles of elevation of a tower from two points distant a and b (a > b) from its foot and in the same straight line from it are 30⁰ and 60⁰, then the height of the tower is

(a) $\sqrt{a} + b$ m (b) $\sqrt{a} - b$ m (c) \sqrt{ab} m (d) \sqrt{a}/b m



10. At some time of the day, the length of the shadow of a tower is equal to its height. Then, the sun's altitude at that time is:

(a) 30° (b) 60° (c) 90° (d) 45^{0}

II State whether True or False

- 1. If the length of the shadow of a tower is increasing, then the angle of elevation of the sun is also increasing.
- 2. If a man standing on a platform 3 metres above the surface of a lake observes a cloud and its reflection in the lake, then the angle of elevation of the cloud is equal to the angle of depression of its reflection.
- 3. The angle of elevation of the top of a tower is 30°. If the height of the tower is doubled, then the angle of elevation of its top will also be doubled.
- 4. If the height of a tower and the distance of the point of observation from its foot, both, are increased by 10%, then the angle of elevation of its top remains unchanged.

III Fill in the blanks

- 1. The is the line drawn from the eye of an observer to the point in the object viewed by the observer.
- 2. The of the point viewed is the angle formed by the line of sight with the horizontal when the point being viewed is above the horizontal level.
- 3. The of a point on the object being viewed is the angle formed by the line of sight with the horizontal when the point is below the horizontal level.
- 4. The of an object or the distance between two distant objects can be determined with the help of trigonometric ratios.

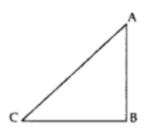
IV Very short answer questions

- The angles of elevation of the top of a tower from two points at a distance of 4 m and 9m from the base of the tower and in the same straight line with it are 60° and 30° respectively. Find the height of the tower.
- The tops of two towers of height x and y, standing on level ground, subtend angles of 30° and 60° respectively at the centre of the line joining their feet, then find x:y.

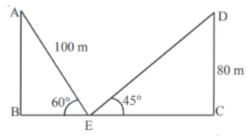
V SHORT ANSWER QUESTIONS (TWO MARKS)

- A ladder 15 m long just reaches the top of a vertical wall. If the ladder makes an angle of 60° with the wall, then calculate the height of the wall.
- In the given figure, a tower AB is 20 m high and BC, its shadow on the ground, is 20√3 m long. Find the Sun's altitude.

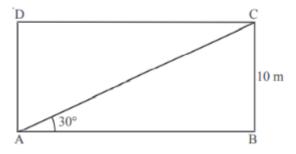




- 3. The string of a kite is 100 m long and it makes an angle of 60° with the horizontal. Find the height of the kite, assuming that there is no slack in the string.
- 4. A tree 12 m high, is broken by the storm. The top of the tree touches the ground making an angle 30°. At what height from the bottom the tree is broken by the storm?
- 5. In the figure, find the value of BC.

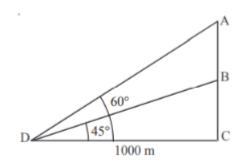


- Find the angle of elevation of a point which is at a distance of 10√3 m from the base of a tower 30m high.
- 7. The height of the tower is 15 m. What is the length of its shadow when sun's altitude is 45° ?
- 8. A 1.5 m tall boy stands at a distance of 2m from lamp post and casts a shadow of 4.5 m on the ground. Find the height of the lamp post?
- 9. The tops of two poles of height 20m and 14 m are connected by a wire. Find the length of the wire if it makes an angle of 30° with horizontal?
- 10. In the given figure, find the perimeter of rectangle ABCD.

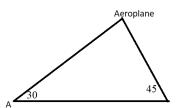


11. In the figure, find the value of AB.





- 12. If the shadow of a tower 30 m long, when the Sun's elevation is 30°. What is the length of the shadow, when Sun's elevation is 60°?
- 13. From a point on the ground, which is 21 m from the foot of a tower, the angle of elevation of the top of the tower is 30°. Find the height of the tower.
- 14. In figure, AB is a 6m pole and CD is a ladder inclined at an angle of 60° to the horizontal and reaches up to a point D of pole. If AD=2.54 m, find the length of the ladder. (Use $\sqrt{3}=1.73$)
- 15. An observer, 1.7 m tall, is $20\sqrt{3}$ m away from a tower. The angle of elevation from the eye of observer to the top of tower is 30° . Find the height of tower.
- 16. The angle of depression from the top of a tower 12 m high, at a point on the ground is 30°. Then find the distance of the point from the top of the tower.
- 17. The top of two towers of height x and y, standing on level ground, subtend angles of 30° and 60° respectively at the centre of line joining their feet, then find x : y.
- 18. A vertical stick 10 cm long casts a shadow 8 cm long. At the same time, a tower casts a shadow28 m long. Determine the height of the tower.
- 19. Stations A and B are $3(1+\sqrt{3})$ km apart. Each station sights an aeroplane at an angle of 30° and 45° as shown in figure. Find the altitude of the aeroplane.



20. From the vertex of a tower the angle of depression of a point 120 m away from the foot of the tower is 60°. Find the height of the tower.

VI SHORT ANSWER TYPE QUESTIONS (THREE MARKS)

- 1. Find the angle of elevation of the sun when the shadow of a pole h metres high is $\sqrt{3}$ h metres long.
- A ladder 15 metres long just reaches the top of a vertical wall. If the ladder makes an angle of 60° with the wall, find the height of the wall.



- 3. Two pillars of equal heights are on either side of a road, which is hundred metres wide. The angles of elevation of the tops of the pillars are 60° and 30° at a point on the road between the pillars. Find the position of the point between the pillars?
- 4. From a point on the ground, the angles of elevation of the bottom and top of a water tank kept on the top of the 30 m high building are 30° and 45° respectively. Find the height of the water tank?
- 5. From the top of a multi-storeyed building, 90m high, the angles of depression of the top and the bottom of a tower are observed to be 30° and 60° respectively. Find the height of the tower?
- 6. Two ships are there in the sea on either side of a lighthouse in such a way that the ships and the base of the lighthouse are in the same straight line. The angles of depression of two ships as observed from the top of the lighthouse are 60° and 45°. If the height of the lighthouse is 200m, find the distance between the two ships.
- 7. From the top of a 300 metre high light-house, the angles of depression of two ships, which are due south of the observer and in a straight line with its base, are 60° and 30°. Find their distance apart?
- 8. A Statue, 1.6 m tall, stands on the top of a pedestal. From a point on the ground, the angle of elevation of the top of the statue is 60° and from the same point, the angle of elevation of the top of the pedestal is 45°. Find the height of the pedestal? (Use $\sqrt{3} = 1.73$)
- 9. A peacock is sitting on the top of a tree. It observes a serpent on the ground making an angle of depression of 30°. The peacock with the speed of 300 metre/ minute catches the serpent in 12 seconds. What is the height of the tree?
- 10. An aero plane, at an altitude of 1200 m, finds that two ships are sailing towards it in the same direction. The angles of depression of the ships as observed from the aeroplane are 60° and 30° respectively. Find the distance between the two ships?
- 11. A spherical balloon of radius r subtends an angle θ at the eye of an observer. If the angle of elevation of its centre is φ , find the height of the centre of the balloon.
- 12. From a balloon vertically above a straight road, the angles of depression of two cars at an instant are found to be 45° and 60°. If the cars are 100 m apart, find the height of the balloon.
- 13. The angle of elevation of a cloud from a point h metres above the surface of a lake is θ and the angle of depression of its reflection in the lake is φ . Find the height of the cloud above the lake.
- 14. The angle of elevation of the top of a tower from certain point is 30°. If the observer moves 20 metres towards the tower, the angle of elevation of the top increases by 15°. Find the height of the tower.
- 15. The angle of elevation of the top of a tower from two points distant s and t from its foot are complementary. Find the height of the tower.



- 16. The shadow of a tower standing on a level plane is found to be 50 m longer when Sun's elevation is 30° than when it is 60°. Find the height of the tower.
- 17. A vertical tower stands on a horizontal plane and is surmounted by a vertical flag staff of height h. At a point on the plane, the angles of elevation of the bottom and the top of the flag staff are α and β , respectively. Find the height of the tower.
- 18. The angle of elevation of the top of a tower 30 m high from the foot of another tower in the same plane is 60° and the angle of elevation of the top of the second tower from the foot of the first tower is 30° . Find the distance between the two towers and also the height of the other tower.
- 19. From the top of a tower h m high, the angles of depression of two objects, which are in line with the foot of the tower are α and β ($\beta > \alpha$). Find the distance between the two objects.
- 20. The angle of elevation of the top of a vertical tower from a point on the ground is 60°. From another point 10 m vertically above the first, its angle of elevation is 45°. Find the height of the tower.

Long Answer Type Questions

- A person standing on the bank of a river observes that angle of elevation of the top of a tree standing on the opposite bank is 60°. When he moves 30m away from the bank, he finds the angle of elevation to be 30°. Find the height of the tree and the width of the river.
- 2. At a point on a level ground, the angle of elevation α of a vertical tower is found to be such that tan $\alpha = 5/12$. On walking 192m towards the tower, the angle of elevation becomes β such that tan $\beta = 3/4$. Find the height of the tower.
- 3. A boy whose eye level is 1.3m from the ground, spots a balloon moving with wind in a horizontal line at some height from the ground. The angle of elevation of the balloon from the eyes of the boy at any instant is 60°. After 12 seconds, the angle off elevation reduces to 30°. If the speed of wind at that moment is $29\sqrt{3}$ m/s, then find the height of the balloon from the ground.
- 4. Two pillars of equal height stand on either side of the roadway which is 150m wide. From a point on the roadway between the pillars, the elevations of the top of the pillars are 60° and 30°. Find the height of the pillars and the position of the point.
- 5. The angle of elevation of the top of the building from the foot of the tower is 30° and the angle of elevation of the top of the tower from the foot of the building is 60°. If the tower is 60m high, find the height of the building.
- 6. From the top of the building, 100m high, the angles of depression of the top and bottom of a tower are observed to be 45° and 60° respectively. Find the height of the tower. Also find the distance between the foot of the building and the bottom of the tower.



- The angles of elevation and depression of the top and bottom of a lighthouse from the top a 60° high building are 30° and 60° respectively. Find
 - (i) The difference between the heights of the lighthouse and the building
 - (ii) The distance between the lighthouse and the building.
- 8. The angle of elevation of the top of the hill at the foot of the tower is 60° and the angle of depression from the tower of the foot of the hill is 30°. If the tower is 50m high, find the height of the hill.
- 9. A man standing on the deck of the ship, which is 16m above the water level, observes the angle of elevation of the top of the clip as 60° and the angle of depression of the base of the cliff as 30°. Calculate the distance of the cliff from the ship and height of the cliff.
- 10. If the angle of elevation of a cloud from a point 'h' meters above a lake is α and angle of depression of its reflection in the lake is β , prove that distance of the cloud from the point of

observation is $\frac{2h \sec \alpha}{\tan \beta - \tan \alpha}$

Case Study 1



A group of students of class x visited India Gate on an education trip. The teacher and students had interest in History as well. The teacher narrated that India Gate, official name Delhi Memorial, originally called All-India War Memorial, monumental sandstone arch in New Delhi, dedicated to the troops of British India who died in wars fought between 1914 and 1919. The teacher also said that India Gate, which is located at the eastern end of the Rajpath (formerly called the Kingsway), is about 138 feet (42 meters) in height.

1. What is the angle of elevation if they are standing at a distance of 42 m away from the monument?

(a) 30°	(c) 60^0
(b) 45^0	(d) 0^0



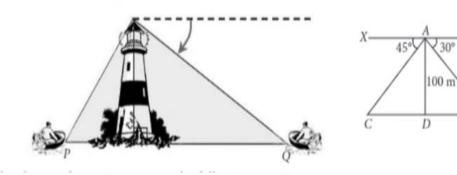
- 2. They want to see the tower at an angle of 60° . So they want to know the distance where they should stand and hence find the distance.
 - (a) $40\sqrt{3}$ (c) $14\sqrt{3}$ (d) $16\sqrt{3}$
 - (b) $42\sqrt{3}$
- 3. 3) If the altitude of the sun is at 60° , then the height of the vertical tower that will cast a shadow of length 20m is
 - $20\sqrt{3}m$ $15 / \sqrt{3m}$ a. c. $20 / \sqrt{3}m$ $15\sqrt{3m}$ b. d.
- 4. The ratio of the height of the vertical tower and its shadow is 1:1. The angle of the elevation of the sun is (c) 60°
 - (a) 30°
 - (b) 45⁰

(d) 90°

- 5. The angle formed by the line of sight with the horizontal when the object viewed is below the horizontal level is
 - (a) corresponding angle
 - (b) angle of elevation
 - (c) angle of depression
 - (d) complete angle

CASE STUDY 2: LIGHT HOUSE

A boy is standing on the top of light house. He observed that boat P and boat Q are approaching to light house from opposite directions. He finds that angle of depression of boat P is 45^0 and angle of depression of boat Q is 30° . He also knows that height of the light house is 100m.



Based on the above information, answer the following questions.

- Measure of $\angle ACD$ is equal to 1.
 - (a) 30°

(b) 45°

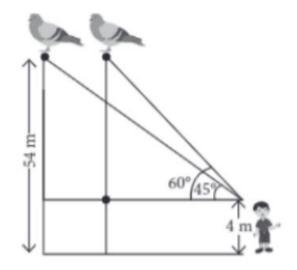
- 2. If \angle YAB = 30⁰, then \angle ABD is also 30⁰, why?
 - (a) vertically opposite angles
 - (b) alternate interior angles
- 3. Length of CD is equal to
 - (a) 90m
 - (b) 60m
- 4. (iv)Length of BD is equal to
 - (a) 50m

- (c) 60°
- (d) 90°
- (c) alternate exterior angles
- (d) corresponding angles
- (c) 100m
- (d) 80m
- (b) 100m



	(c) $100\sqrt{2}$ m	(d) $100\sqrt{3}m$
5.	Length of AC is equal to	
	(a) $100\sqrt{2} m$	(c) 50m
	(b) $100\sqrt{3}m$	(d) 100m

CASE STUDY 3:



A boy 4 m tall spots a pigeon sitting on the top of a pole of height 54m from the ground. The angle of elevation of the pigeon from the eyes of boy at any instant is 60° . The pigeon flies away horizontally in such a way that it remained at a constant height from the ground. After 8 seconds, the angle of evaluation of the pigeon from the same point is 45° . Based on the above information answer the following questions (take $\sqrt{3} = 1.73$)

1. Find the distance of first position of the pigeon from the eyes of the boy

(a) 54m	(c) $\frac{100}{\sqrt{3}}m$
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(b) 100m (d) $100\sqrt{3}m$

2. If the distance between the positions of pigeon increases, then the angle of elevation

(c) $50\sqrt{3}m$

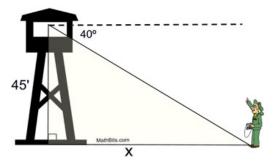
- (a) Increases (c) Remains unchanged
- (b) Decreases (d) can't say
- 3. Find the distance between the boy and the pole.
 - (a) 50m
 - (b) $\frac{50}{\sqrt{3}}m$ (d) $60\sqrt{3m}$
- 4. How much distance the pigeon covers in 8 seconds?
 - (a) 12.13m (c) 21.09m
 - (b) 19.60m (d) 26.32m
- 5. Find the speed of the pigeon?



- 1. 2.63m/sec
- 2. 3.88 m/sec

- 3. 6.7 m/sec
- 4. 9.3m/sec

Case Study 4



A hunter found a tall tower inside a dense forest. He was planning to climb the tower and noticed that the angle of depression was 40° and the height of the tower was 45 cm. His fellow colleague however, said that the angle of depression is actually 10° less than what the hunter has measured. Keeping into account the new angle of depression, answer the following questions.

- 1. What is the new angle of elevation to the top of the tower?
 - (a) 30° (c) 45°
 - (b) 60° (d) 90°
- 2. What is the new angle of depression to the top of the tower?
 - (a) 30° (c) 45°
 - (b) 60° (d) 90°
- 3. What is the new distance of the hunter from the base of the tower?
 - (a) 45 cm (c) 25 cm
 - (b) $45\sqrt{3}$ cm (d) $25\sqrt{3}$ cm

4. Did the distance of the hunter increase or decrease due to change of angle of depression?

- (a) Increase (b) Decrease
- 5. If the height of the tower decreases, will the angle of depression increase or decrease?
 - (a) Increase (b) Decrease



Case Study 5



Boojho went to a park. He went up the slide to play. The angle of elevation θ of the slide is 30^{θ} . But the base from which the angle of elevation is measured is 5 cm above the ground level and the distance from the staircase is 10 cm. (Use $\sqrt{3} = 1.732$)

Q1.What is the distance of the staircase from the point from which the angle of elevation of the slide is measured?

(a) 5 cm	(c) 15cm
(b) 10 cm	(d) 20 cm

Q2. What is the angle of depression from the top of the slide to its base?

(a) 30°	(c) 90°	
(b) 60°	(d) 120°	
Q3. What is the height of the staircase?		
(a) 5.77 cm	(c) 15.77 cm	
(b) 10.77 cm	(d) None of the above	
Q4. What is the length of the slide?		
(a) 9.874 cm	(c) 11.547 cm	
(b) 8.46 cm	(d) None of the above	
Q5. Will the angle of elevation increase or decrease if the staircase was made taller?		

(a) Increase

(b) Decrease



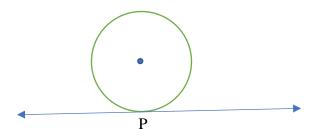
CHAPTER 10

Circles

Important Concepts

Tangent to a circle

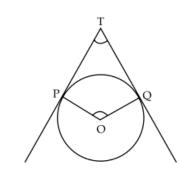
A tangent to a circle is a line that intersects the circle at only one point



- * There is only one tangent at a point on a circle
- * There are exactly two tangents to a circle through a point lying outside the circle.
- * The tangent at any point of a circle is perpendicular to the radius through the point of contact.
- * The length of tangents drawn from an external point to a circle are equal.

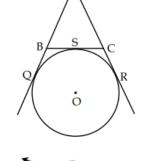
Multiple Choice Questions

- 1. In Fig. if from an external point T, TP and TQ are two tangents to a circle with centre O so that $< POQ = 110^{\circ}$, then < PTQ is:
 - A. 60⁰
 - **B**. 70⁰
 - C. 80°
 - D. 90°



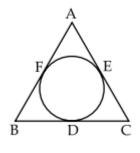
- 2. From a point P which is at a distance of 13cm from the centre O of a circle of radius 5cm, the pair of tangents PQ and PR to the circle are drawn. What are the lengths (in cm) of tangents PQ and PR?
 - A. 13,12
 - B. 13, 13
 - C. 12,12
 - D. 12,18

- 3. In the fig. if the semi perimeter of $\triangle ABC = 23$ cm, then AF + BD + CE is:
 - A. 46cm
 - B. 11.5cm
 - C. 23cm
 - D. 34.5cm
- 4. In the fig. PT is a tangent to a circle with centre O. If PT = 30cm and diameter of circle is 32cm, then the length of the line segment OP will be:
 - A. 68cm
 - B. 34cm
 - C. 17cm
 - D. 34.8cm
- 5. In fig. AQ, AR and BC are tangents to a circle with centre O, If AB = 7cm, BC = 5cm
 - AC = 5cm, then the length of tangent AQ is:
 - A. 5cm
 - B. 7cm
 - C. 8.5cm
 - D. 17cm
- 6. In Fig. if OC =9cm, and OB = 15cm, then BC+BD
 - A. 18cm
 - B. 12cm
 - C. 24cm
 - D. 36cm



O D B

find









О

5 cm

 \cap

В

12 cm

R

7. APB is a tangent to a circle with centre O, at point P. If $\langle QPB = 50^{\circ}$, then the measure of $\langle POQ$ is:

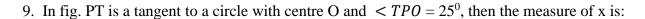
4 cm

Α

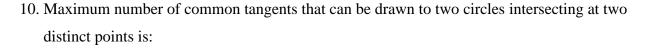
3 cm

O'

- A. 120°
- B. 100°
- C. 140°
- 8. In fig. the length of PR is:
 - A. 20cm
 - B. 26cm
 - C. 24cm
 - D. 28cm



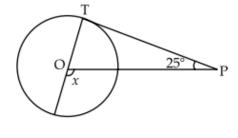
- A. 120⁰
- B. 125⁰
- C. 110^{0}
- D. 115⁰



- A. 1 C. 3 B. 2 D. 4
- 11. In the fig. O is the centre of the circle. If PA and PB are tangents to the circle, then $\langle AQB \rangle$ is equal to:
 - A. 100⁰
 - B. 80°
 - C. 70°
 - D. 50⁰

12. A line which is perpendicular to the radius of the circle through the point of contact is:

80°



O



A. Tangent	C. segment
B. Chord	D. normal

13. Number of tangents to a circle which are parallel to a secant is:

- A. 1 C. 3
- B. 2 D. Infinite

14. In the given quadrilateral, OQPR, <QOR is equal to:

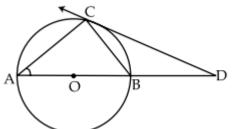
- A. 120°
- B. 130⁰
- C. 145⁰
- D. 110⁰

15. In fig. if OA = 5cm, OM = 3cm, the length of chord AB (in cm) is:

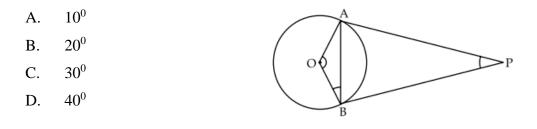
- A. 8
- **B**. 10
- C. 6
- D. 4

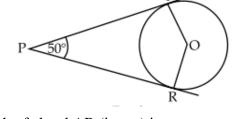
16. In the fig. AB is a diameter and AC is a chord of a circle such that $< BAC = 30^{\circ}$. If DC is a tangent, then Δ BCD is:

- A. Equilateral
- B. Isosceles
- C. Right angled triangle
- D. Acute angled



17. Two tangents are drawn from an external point P (as given in fig.) such that $\langle OBA = 10^{\circ}$. Then $\langle BPA$ is:







18. If two tangents inclined to each other at an angle 60^0 are drawn to a circle of radius 3cm, then the length of tangent is equal to:

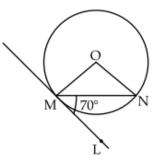
A.
$$\sqrt{3}$$
 cmC. $\frac{2}{\sqrt{3}}$ cmB. $2\sqrt{3}$ cmD. $3\sqrt{3}$ cm

19. In fig. O is the centre of the circle, MN is a chord and the tangent ML at the point M makes an angle 70° with MN then < MON is equal to:

A. 120⁰

B. 90°

- C. 140⁰
- D. 70°



20. The distance between two parallel tangents to a circle of radius 5cm is:

A.	10cm	C.	12cm
B.	11cm	D.	14cm

21. If the circumference of a circle increases from 4π to 8π , then its area will become

- A. half C. 4 times
- B. 2 times D. does not change

22. In Fig, PQ is a chord of a circle and PT is the tangent at P such that $\angle QPT = 60^{\circ}$. Then $\angle PRQ$ is equal to

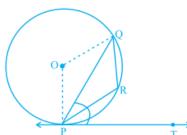
- A. 135⁰
- B. 150°
- C. 120⁰

D.
$$110^{\circ}$$

23. If two tangents inclined at an angle 60° are drawn to a circle of radius 3 cm, then length of each tangent is equal to

A. $\frac{3}{2}\sqrt{3}$ cm

- B. 6 cm
- C. 3 cm
- D. $3\sqrt{3}$ cm



0

1 2



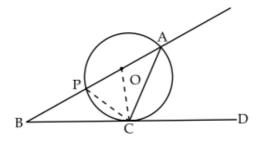
- 24. Here is a circle with centre O. Manu wants to draw a tangent RS to the circle. What is the number of points at which the line RS will meet the circle?
 - A.
 - В.
 - C.
 - D. 3

ONE MARK QUESTIONS (OTHER THAN MCQs)

- 25. Tangent to a circle intersects the circle at point(s)?
- 26. The tangent at any point of circle is perpendicular to thethrough the point of contact.
- 27. The lengths of tangents drawn from an external point to a circle are not equal. (true/false)
- 28. The common point of a tangent to a circle with the circle is called------.
- 29. If diagonal of a cyclic quadrilateral are the diameters of a circle through the vertices of a quadrilateral, then quadrilateral is a-----.
- 30. Given three non collinear points, then the number of circles which can be drawn through these three points are?
- 31. PQ is a tangent drawn from an external point P to a circle with centre O and QOR is the diameter of the circle. If $\angle POR = 120^{\circ}$, what is the measure of $\angle OPQ$?

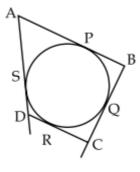
Very Short Answer Questions

- 1. Prove that the line segments joining the points of contact of two parallel tangents is a diameter of the circle.
- 2. O is the centre of the circle and BCD is a tangent to it at C. Prove that $\langle BAC + \langle ACD = 90^{\circ} \rangle$



3. In the figure quadrilateral ABCD is drawn to circumscribe a circle.

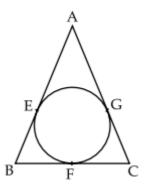
Prove that AD + BC = AB + CD



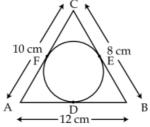




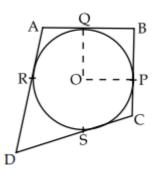
- 4. Prove that the tangents drawn at the end- points of the diameter of a circle are parallel.
- 5. Two concentric circles have centre O, OP= 4cm, OB = 5cm. AB is a chord of the outer circle and tangent to the inner circle at P. Find the length of AB.
- 6. Two tangents PA and PB are drawn to a circle with centre O such that $\langle APB = 120^{0}$. Prove that OP=2AP
- 7. In the isosceles triangle ABC in fig. AB = AC, show that BF = FC



8. In the fig. a circle is inscribed in a $\triangle ABC$ with sides AB = 12cm, BC = 8 cm and AC = 10cm. Find the lengths of AD, BE and CF

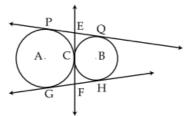


9. In fig. circle is inscribed in a quadrilateral ABCD in which $\langle B = 90^{\circ}$. If AD = 23cm, AB = 29cm, and DS = 5cm, find the radius 'r' of the circle

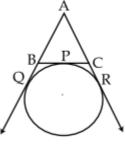




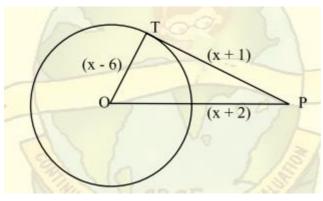
9. In fig. two circles touch each other externally at C. Prove that the common tangent at C bisects the other two tangents



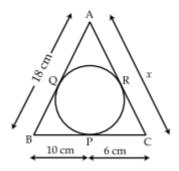
11. In fig. circle touches the side BC of a triangle ABC at the point P and AB and AC produced at Q and R. Show that $AQ = \frac{1}{2}$ (*perimeter of* ΔABC)



12. Find the actual length of sides of ΔOTP



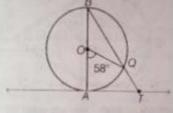
13. In fig. all three sides of the triangle touch the circle. Find the value of x.



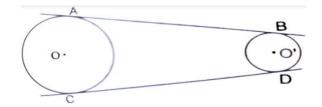
- 14. Two tangents PR and PQ are drawn from external point P to a circle with centre O. Prove that PROQ is a cyclic quadrilateral.
- 15. Prove that tangents drawn at the ends of a chord make equal angles with the chord



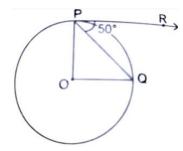
16. In the given fig. AB is diameter of the circle with centre O and AT is tangent. If $\angle AOQ=58^{\circ}$, Find $\angle ATQ$.



- 17. Two concentric circles are of radii 7 cm and r cm respectively, where r > 7. A chord of the larger circle, of length 48 cm, touches the smaller circle. Find the value of r
- 18. In the given figure, AP and BP are tangents to a circle with centre O, such that AP = 5cm, \angle APB = 60⁰. Find the length of chord AB
- 19. In the fig. AB and CD are common tangents to two circles of unequal radii. Prove AB = CD



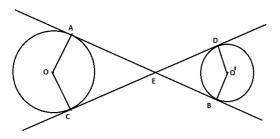
20. If O is the centre of circle, PQ is chord and the tangent PR at P makes an angle 50° with PQ. Find \angle POQ



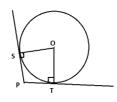
Short Answer Questions

- 1. If an angle between two tangents drawn from a point P to a circle of radius 'a' and centre O is 60°, then prove that $AP = a\sqrt{3}$.
- In the figure common tangents AB and CD to two circles with centre O and 'O^I intersects at E.
 Prove that AB = CD.

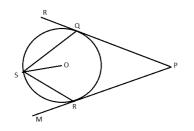




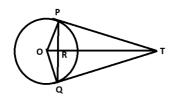
- 3. If all the sides of a parallelogram touch a circle, then prove that the parallelogram is a rhombus.
- 4. XY and X^IY^I are two parallel tangents to a circle with centre O and another tangent AB with point of contact C, intersecting XY at A and X^IY^I at B, is drawn. Prove that $\angle AOB = 90^{\circ}$.
- 5. In figure tangent segments PS and PT are drawn to a circle with centre O such that $\angle SPT = 120^{\circ}$. Prove that OP = 2PS.



6. In fig. 3, PQ and PR are tangents to the circle with centre O and S is a point on the circle such that \angle SQR= 50° and \angle SRM = 60°. Find \angle QSR.

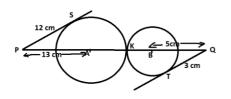


- 7. Two tangents TP and TQ are drawn to a circle with centre O from an external point T. Prove that $\angle PTQ=2\angle OPQ$.
- 8. In fig, PQ is a chord of length 8 cm of a circle of radius 5 cm, the tangents at P and Q intersect at a point T. Find the length TP.

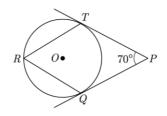


 In fig, two circles with centres A and B touch each other externally at K. find the length of segment PQ. (Given PA=13 cm, BQ=5 cm, PS=12 cm AND QT=3 cm)

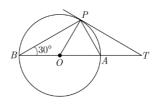




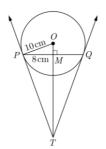
10. In figure, O is the centre of a circle. PT and PQ are tangents to the circle from an external point P. If \angle TPQ = 70°, find \angle TRQ.



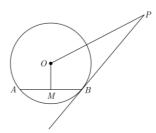
11. In the given figure, BOA is a diameter of a circle and the tangent at a point P meets BA when produced at T. If $\angle PBO = 30^\circ$, what is the measure of $\angle PTA$?



12. In figure, PQ, is a chord of length 16 cm, of a circle of radius 10 cm. the tangents at P and Q intersect at a point T. Find the length of TP.

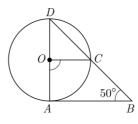


13. PB is a tangent to the circle with centre O to B. AB is a chord of length 24 cm at a distance of 5 cm from the centre. It the tangent is of length 20 cm, find the length of PO.





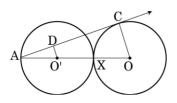
14. In the given figure, AD is a diameter of a circle with centre O and AB is a tangent at A. C is a point on the circle such that DC produced intersects the tangent at B and $\angle ABC = 50^{\circ}$. Find $\angle AOC$.



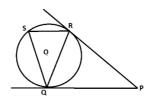
15. Prove that the parallelogram circumscribing a circle is a rhombus.

Long Answer Questions

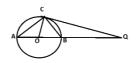
- 1. Prove that the lengths of tangents drawn from an external point to a circle are equal.
- 2. In fig, two equal circles with centres O and O^I, touch each other at X. OO^I produced meet the circle with centre O^I at A. AC is tangent to the circle with centre O, at the point C. O^ID is perpendicular to AC. Find the value of $\frac{DO^{i}}{CO}$.



- 3. The radius of the in-circle of a triangle is 4 cm and the segments into which one side is divided by the point of contact are 6 cm and 8 cm. Determine the other two sides of the triangle.
- 4. In fig, tangents PQ and PR are drawn from an external point P to a circle with centre O, such that $\angle RPQ = 30^{\circ}$. A chord RS is drawn parallel to the tangent PQ. Find $\angle RQS$.

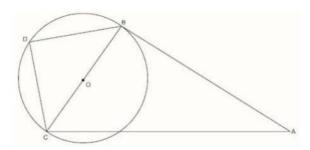


- 5. Prove that opposites sides of a quadrilateral circumscribing a circle subtend supplementary angles at the centre of the circle.
- In fig AB is diameter of a circle with centre O and QC is a tangent to the circle at C. If ∠CAB=30°, find ∠CQA and ∠CBA.





- In fig, O is the centre of a circle of radius 5 cm. T is a point such that OT = 13cm and OT intersect circle at E. If AB is a tangent to the circle at E, find the length of AB, where TP and TQ are two tangents to the circle.
- 8. The figure below represents a circle with centre O and diameter 12cm



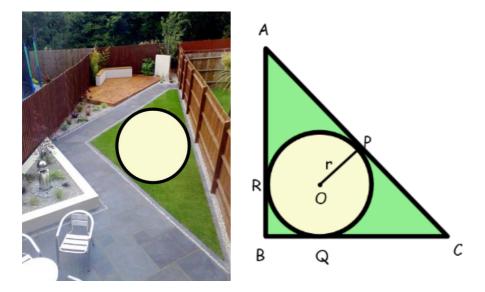
In triangle DBA, \angle DBC = \angle BCD and \angle A = 50°.

- (i) What is the measure of $\angle DCA$?
- (ii) Dhruv said that, "The quadrilateral DBAC is a cyclic quadrilateral." Is Dhruv correct?Give a reason to support your answer.
- (iii) In triangle BAC, the length of side CA = 2.5 times OB. What is the length of side BA?

CASE STUDY BASED QUESTIONS

CASE STUDY-1(PLAYGROUND)

A playground is in the shape of a triangle with right angle at **B**, AB = 3m and BC = 4m. A pit was dig inside it such that it touches the walls AC, BC and AB at P, Q and R, respectively such that AP = x m.



Based on the above information, answer the following questions.

(i) The value of AR =

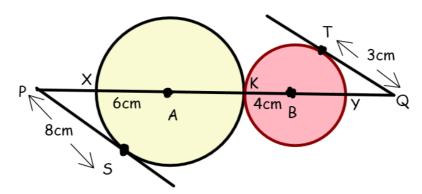
(a) 2x m (b) x / 2 m (c) x m (d) 3x m (ii) The value of BQ=



(a) 2x m ((b) (3 – x) m	(c) $(2 - x) m$	(d) 4x m
(iii) The value of CQ)=		
(a) $(4 + x) m$ ((b) $(5 - x) m$	(c) $(1 + x) m$	(d) Both (b) and (c)
(iv) Which of the foll	lowing is correct?		
(a) Quadrilateral	AROP is a square		(b) Quadrilateral BROQ is a square
(c) Quadrilateral	CQOP is a square		(d) None of the above
(v) Radius of the pit	is		
(a) 1 m (l	b) 3 m	(c) 4 m	(d) 5 m

CASE STUDY – 2 (CIRCLE DRAWING)

A student draws two circles that touch each other externally at point **K** with centres **A** and **B** and radii 6 cm and 4cm, respectively as shown in the figure



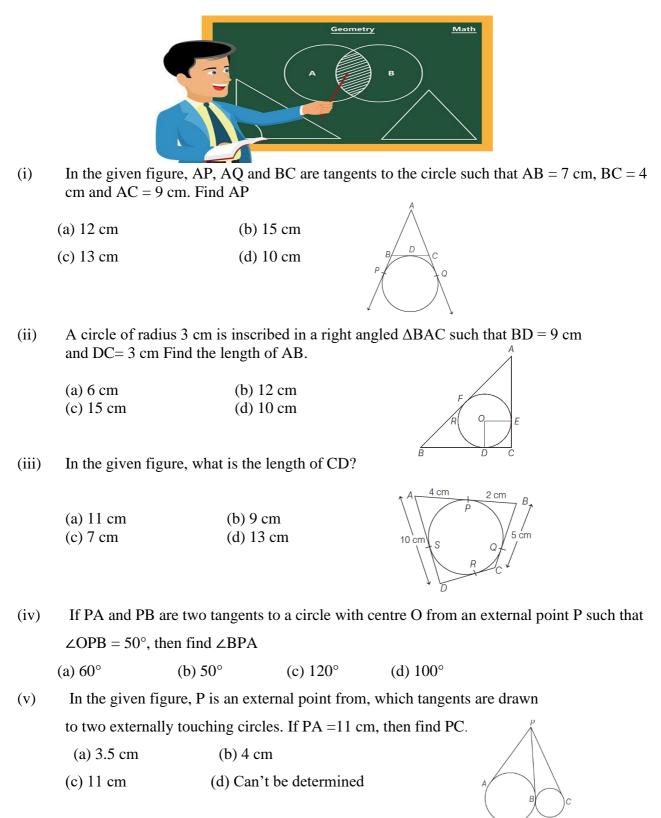
Based on the above information, answer the following questions.

(i) The value of $PA =$			
(a) 10 cm	(b) 5 cm	(c) 13 cm	(d) Can't be determined
(ii) The value of BQ=			
(a) 4 cm	(b) 5 cm	(c) 6 cm	(d) 18 cm
(iii) The value of PK =			
(a) 13 cm	(b) 15 cm	(c) 16 cm	(d) 18 cm
(iv) The value of QY =			
(a) 2 cm	(b) 5 cm	(c) 1 cm	(d) 3 cm
(v) If two circles touch ex	ternally, then the num	ber of common tai	ngents can be drawn is
(a) 1	(b) 2	(c) 3	(d) None of these
CASE STUDY – 3			

Kuldeep loves geometry. So, he was curious to know more about the concepts of circles. His grandfather is a mathematician. So, he reached to his grandfather to learn something interesting about



tangents and circles. His grandfather gave him knowledge on circles and tangents and ask him to solve the following questions





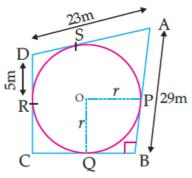
CASE STUDY-4

A Ferris wheel (or a big wheel in the United Kingdom) is an amusement ride consisting of a rotating upright wheel with multiple passengers carrying components (commonly referred to as passenger cars, cabins, tubs, capsules, gondolas, or pods) attached to the rim in such a way that as the wheel turns, they are kept upright, usually by gravity. After taking a ride in Ferris wheel, Aarti came out from the crowd and was observing her friends who were enjoying the ride. She was curious about the different angles and measures that the wheel will form. She forms the figure as given below.

S C C C C C C C C C C C C C C C C C C C	30° P	S O R	30° P
(i) In the given figure find $\angle R0$ (A) 60°	OQ. (B) 100°	(C) 150°	(D) 90°
 (ii) Find ∠RQP. (A) 75° 	(B) 60°	(C) 30°	(D) 90°
(iii) Find \angle RSQ. (A) 60°	(B) 75°	(C) 100°	(D) 30°
 (iv) Find ∠ORP. (A) 90° 	(B) 70°	(C) 100°	(D) 60°
(v) If PQ=40m and OQ=30m t (A) 50m	hen PO= (B) 60m	(C) 70m	(D) 80m

CASE STUDY-5

ABCD is a playground. Inside the playground a circular track is present such that it touches AB at point P, BC at Q, CD at R and DA at S.



1. If DR = 5 m, then DS is equal to:

(A) 6 m	(B) 11 m	(C) 5 m	(D) 18 m
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2. The length of AS is:			
(A) 18 m	(B) 13	(C) 14 m	(D) 12 m
3. The length of PB is:			
(A) 12 m	(B) 11 m	(C) 13 m	(D) 20 m
4. What is the angle of OQ	QB?		
(A) 60°	(B) 30°	(C) 45°	(D) 90°
5. What is the diameter of	given circle?		
(A) 22 m	(B) 33 m	(C) 20 m	(D) 30 m
CASE STUDY- 6			

ASE STUDY- 6

Varun has been selected by his School to design logo for Sports Day T-shirts for students and staff. The logo design is as given in the figure and he is working on the fonts and different colours according to the theme. In given figure, a circle with centre O is inscribed in a $\triangle ABC$, such that it touches the sides AB, BC and CA at points D, E and F respectively. The lengths of sides AB, BC and CA are 12 cm, 8 cm and 10 cm respectively.

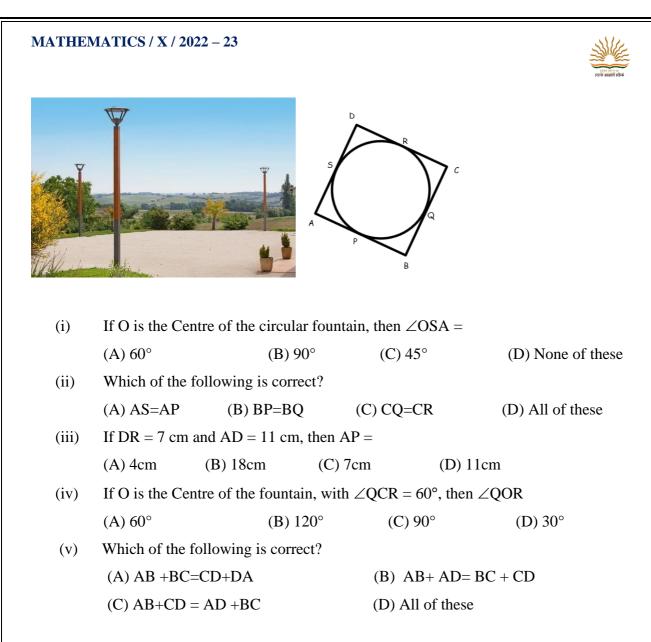


1. Find the length of AD

a) 7	b) 8	c) 5	d) 9
2. Find t	he Length of	BE	
a) 8	b) 5	c) 2	d) 9
3. Find t	he length of	CF	
a) 9	b) 5	c) 2	d) 3
4. If radi	ius of the circ	cle is 4cm, Find th	he area of ΔOAB
a) 20	b) 36	c) 24	d) 48
5. Find a	area of ΔABC	C	
a) 50	b) 60	c) 100	d) 90
CASE	STUDY 7	7	

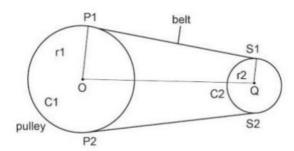
CASE STUDY-7

In a park, four poles are standing at positions A, B, C and D around the fountain such that the cloth joining the poles AB, BC, CD and DA touches the fountain at P, Q, Rand S respectively as shown in the figure. Based on the above information, answer the following questions.



CASE STUDY-8

Given below is the diagram of a pair of pulleys

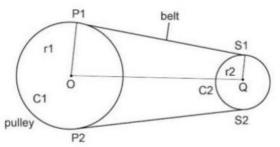


C1 and C2 are two pulleys attached with a belt. O and Q are the centres of C1 and C2, respectively. P1 and P2 are points of contact, where the belt meets C1.S1 and S2 are points of contact, where belt meets C2

i) Identify the common tangents to the two circles (pulleys)?

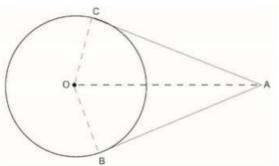
Ankit joins the centre of the two pulleys and observes line segments P1S1 and P2S2 when extended meet at a point X.





- ii) What is the length OX when the diameter of C1 is 30cm, diameter of C2 is 10cm and length of OQ is 100cm?
- iii) Which line segment is equal to the length P1S1?a) OQb) P1S1c) QXd) XS2

Given below is the diagram of a pair of pulleys.

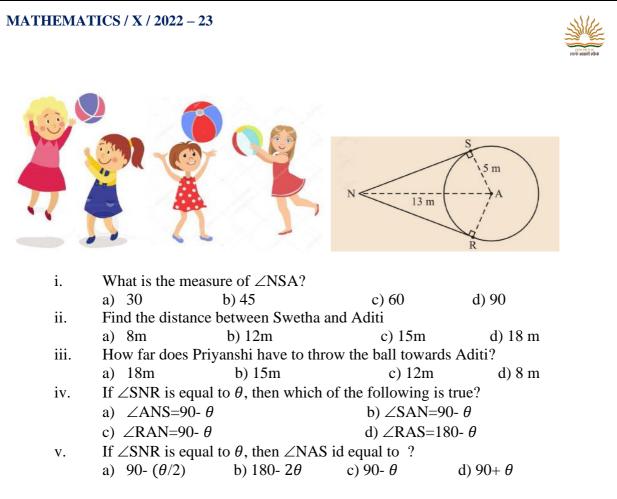


The length of AC is 12 cm and radius is 5cm

- iv) What is the perimeter of the triangle ABO?
- v) If in the given fig. $\angle CAB = 20^\circ$, what is the measure of $\angle AOC$?

CASE STUDY -9

In an international school in Hyderabad organized an Interschool Throwball Tournament for girls just after the pre-board exam. The throw ball team was very excited. The team captains Anjali directed the team to assemble in the ground for practices. Only three girls Priyanshi, Swetha and Aditi showed up. The rest did not come on the pretext of preparing for pre-board exam. Anjali drew a circle of radius 5 m on the ground. The centre A was the position of Priyanshi. She marked a point N, 13 m away from centre A as her own position. From the point N, she drew two tangential lines NS and NR and gave positions S and R to Swetha and Aditi. Anjali throws the ball to Priyanshi, Priyanshi throws it to Swetha, Swetha throws it to Anjali, Anjali throws it to Aditi, Aditi throws it to Priyanshi, Priyanshi throws it to Swetha and so on.



CASE STUDY-10

People of village want to construct a road nearest to the circular village Parli. The road cannot pass through the village. But the people want the road should be at the shortest distance from the center of the village. Suppose the road start from point O which is outside the circular village and touch the boundary of the circular village at point A such that OA = 20 m. And also, the straight distance of the point O from the center C of the village is 25 m.



- i. Find the shortest distance of the road from the centre of the village
 - a) 15m b) 14m c) 13m d) 12m
- ii. Which method should be applied to find the shortest distance?
 - a) Concept of tangent to a circle b) Pythagoras theorem
 - c)Both a and b d) None of these
- iii. If a point is inside the circle, how many tangents can be drawn from that point
 - a) 0 b) 1 c) 2 d) 3
- iv. Number of common tangents can be drawn to two circles which do not intersect



a) 2 b) 3 c) 4 d) 1 v. If we draw two tangents at the end of the diameter, these tangents are always Parallel b) perpendicular c) coincident d) None of these

ANSWERS

MULTITLE CHOICE QUESTIONS					
QN. NO	CORRECT	QN. NO	CORRECT	QN. NO	CORRECT
	OPTION		OPTION		OPTION
1	В	11	D	21	С
2	С	12	А	22	С
3	С	13	В	23	D
4	В	14	В	24	С
5	С	15	А		
6	С	16	В		
7	В	17	В		
8	В	18	D		
9	D	19	С		
10	В	20	А		

MULTIPLE CHOICE QUESTIONS

ONE MARK QUESTIONS (OTHER THAN MCQs

QUES	ANSWEER	QUES	ANSWER
24	One Point	29	150°
25	Radius	30	Parallelogram
26	False	31	Only one
27	7cm	32.	30°
28	Point of contact	33	10cm

Very Short answer Questions

1. Consider the circle with centre at O

PQ & RS are two parallel tangents to it touching at A and B respectively.

Join OA and OB

Now OA perpendicular to PQ (.: radius is perpendicular to tangent)

and OB perpendicular to RS

∴OA∥OB

But OA and OB pass through O

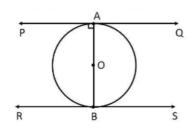
∴AB is straight line through centre

 \therefore AB is a diameter



- 2. $<OCD=90^{0}$ (: radius is perpendicular to tangent at the point of contact) $<OCA + <ACD = 90^{0}$ $<OAC + <ACD = 90^{0}$ (: OC = OA, <OCA=<OAC) $<BAC + <ACD = 90^{0}$

4.



Let AB be a diameter of the circle. Two tangents PQ and RS are drawn at points A and B respectively.

Radius drawn to these tangents will be perpendicular to the tangents.

Thus, $OA \perp PQ$ and $OB \perp RS$

 $\angle OAP = 90^{\circ}$

 $\angle OAQ = 90^{\circ}$

 $\angle OBR = 90^{\circ}$

 $\angle OBS = 90^{\circ}$

It can be observed that

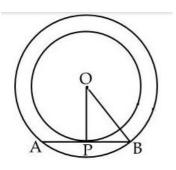
 $\angle OAP = \angle OBS$ (Alternate interior angles)

 $\angle OAQ = \angle OBR$ (Alternate interior angles)

Since alternate interior angles are equal, lines PQ and RS will be parallel.



5.



OP = 4 cm, OB = 5 cm

We know that the radius is perpendicular to the tangent at the point of contact.

 $\therefore \angle OPB = 90^{\circ}$ In right triangle OPB, $OB^{2} = OP^{2} + PB^{2}$ $(5)^{2} = (4)^{2} + PB^{2}$

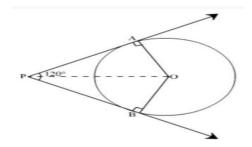
 $PB^2 = 25 - 16 = 9$

PB = 3 cm

We know that perpendicular from the centre to the chord bisect the chord.

 \therefore AB = 2PB = 6 cm

6



In $\triangle OAP$ and $\triangle OBP$,

OP = OP (Common)

 $\angle OAP = \angle OBP$ (90°) (Radius is perpendicular to the tangent at the point of contact)

OA = OB (Radius of the circle)

 $\therefore \Delta OAP$ is congruent to ΔOBP (RHS criterion)

 $\angle OPA = \angle OPB = 120^{\circ}/2 = 60^{\circ} (CPCT)$

In $\triangle OAP$,

 $\cos \angle OPA = \cos 60^\circ = AP/OP$

Therefore, 1/2 = AP/OP



Thus, OP = 2AP

Hence, proved.

- 7. AB = AC (given)
 - ie AE + BE = AG + GC

BE = GC (Length of tangents drawn from an external point to a circle are equal)

BF = CF (: BE = BF and GC = CF)

- 8. Let AD = x cm
- BD = 12 xBE = 12 - xCE = 8 - (12 - x)CE = x - 4 (i) AF = xCF = 10 - x -----(ii) From (i) and (ii), we get x - 4 = 10 - x x = 7 cm AD = 7 cm BE = 5cm CF = 3cm 9. OPBQ is a square Let AQ = xSo BQ = 29 - x, BP = 29 - x

AQ = AR = x, DR = DS = 23-x

i.e. 23-x = 5 gives x = 18 units

Radius of the circle = 29-x = 29-18 = 11cm

10. PE = CE = EQ (lengths of tangents from an external point to a circle are equal)



GF = CF = FH

Therefore, CF bisects PQ and GH

11. AQ = AB + BQ = AB + BP

AR = C R + AC = CP + AC

AQ + AR = AB + BP + CP + AC

2AQ = AB + BC + AC

 $AQ = \frac{1}{2}$ (perimeter of triangle ABC)

12.
$$(x+2)^2 = (x + 1)^2 + (x - 6)^2$$

 $x^2 - 14x + 33 = 0$
 $(x - 11) (x - 3) = 0$

so OT = 5 units, TP = 12 units, OP = 13 units

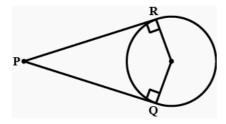
13. BP=BQ=10cm

$$AQ = AQ = 8cm$$

 $CR = CP = x - 8 cm$

x-8 = 6cm

there fore x = 14cm



14.

Given : Tangents PR and PQ from an external point P to a circle with centre O.

To prove : Quadrilateral QORP is cyclic.

Proof: RO and RP are the radius and tangent respectively at contact point R.

∴∠PRO=90°

Similarly ∠PQO=90°

In quadrilateral OQPR, we have

$$\angle P + \angle R + \angle O + \angle Q = 360^{\circ}$$

 $\Rightarrow \angle P + \angle 90^{\circ} + \angle O + \angle 90^{\circ} = 360^{\circ}$

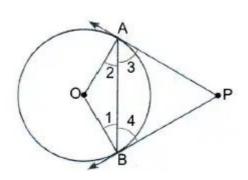
 $\Rightarrow \angle P + \angle O = 360^{\circ} - 180^{\circ} = 180^{\circ}$



These are opposite angles of quadrilateral QORP and are supplementary.

: Quadrilateral QORP is cyclic, hence, proved.

15.



Given: - A circle with centre O, PA and PB are tangents drawn at ends A and B on chord AB.

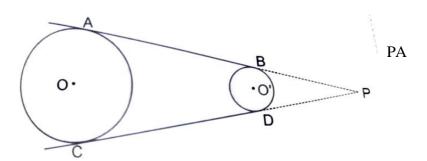
To prove: - ∠**PAB**=∠**PBA** Construction: - Join OA and OB Proof: - In $\triangle AOB$, we have OA=OB (Radii of the same circle) (Angles opposite to equal sides) ∠OAB=∠OBA $\angle OAP = \angle OBP = 90$ (∵Radius ⊥Tangent) ⇒∠PAB=∠PBA Hence proved. 16. ∠AOQ=2 ∠ABQ So ∠ABQ=58 /2 =29⁰ $\angle ATQ = 180^{\circ} - \angle TAB - \angle ABT$ $=180^{0}-90^{0}-29^{0}$ $=61^{0}$ $R = \sqrt{(72+242)}$ 17. $=\sqrt{(49+576)}$ $=\sqrt{625}=25$ cm PA = PB18. $\angle PAB = \angle PBA$



 $\therefore \Delta PAB$ is an equilateral triangle.

Hence AB = PA = 5cm

19. Extend AB and CD to meet at P = PC, PB = PD PA - PB = PC - PDAB = CD

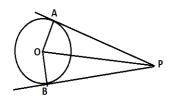


20. $\angle RPQ = 50^{\circ}$ $\angle OPQ = 40^{\circ}$ OP = OQ $\therefore \angle OPQ = \angle OQP = 40^{\circ}$

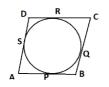
$$\angle POQ = 100^{\circ}$$

Short Answer Questions

1. $\triangle AOP \cong \triangle BOP$, $\angle APO = 30^{\circ}$, use tan 30 in $\triangle AOP$



- AE=EC and DE=BE (lengths of tangents are equal)AB=AE+EB = EC+DE=CD
- 3. AP=AS, BP=BQ, RC=CQ, DR=DS



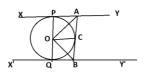
AB+DC=AP+PB+DR+RC=AS+BQ+DS+CQ=(AS+DS)+(BQ+CQ)=AD+BC

AB + AB = AD + AD

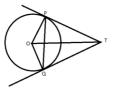
 $2AB=2AD \Rightarrow AB=AD \Rightarrow ABCD$ is a rhombus

4. $\triangle APO \cong \triangle ACO \text{ and } \triangle OBC \cong \triangle OBQ$ $\angle AOP = \angle AOC \text{ and } \angle BOC = \angle BOQ$, use POQ as straight angle.





- 5. $\triangle PSO \cong \triangle PTO \Rightarrow \angle OPS = \angle OPT = 60^{\circ}$ Use cos 60° in $\triangle PSO$
- 6. $\angle QSR=70^{\circ}$
- 7. $\angle PTQ = 180 \angle POQ = 180 (180 2 \angle OPQ) = 2 \angle OPQ$



- 8. TP= $\frac{20}{3}$ (PR=4cm, OR=3cm, Δ POR~ Δ TOP by AA criteria, use side proportionality)
- 9. PQ= 27 cm
- 10. Here, O is the centre of circle.

PQ and PT are tangents to the circle from a point P

R is any point on the circle. RT and RQ are joined.

∠TPQ=70∘

Now,

Join TO and QO

∠TOQ=180∘-70∘=110∘

Here, OQ and OT are perpendicular on QP and TP.

 \angle TOQ is on the centre and \angle TRQ is on the rest part.

 \angle TRQ=1/2 \angle TOQ=1/2(110 \circ)=55 $^{\circ}$

Therefore, ∠TRQ=55°

^{11.} Given, BOA is a <u>diameter of a circle</u>

 $\angle OPT = 90^{\circ}, \angle BPA = 90^{\circ}$

 $\angle PBA + \angle PAB + \angle BPA = 180^{\circ}$

From the figure,

 $\angle PBA = 30^{\circ}$



 $30^\circ + \angle PAB + 90^\circ = 180^\circ$

 $120^{\circ} + \angle PAB = 180^{\circ}$

 $\angle PAB = 180^{\circ} - 120^{\circ}$

 $\angle PAB = 60^{\circ}$

We know that $\angle PAB = \angle OAP = 60^{\circ}$

From the figure,

OP = OA = OB = radius

In triangle OPA,

 $\angle OPA = \angle OAP$

Also, $\angle OPT = \angle OPA + \angle APT$

 $90^\circ = 60^\circ + \angle APT$

 $\angle APT = 90^{\circ} - 60^{\circ}$

```
\angle APT = 30^{\circ}
```

Therefore, the measure of angle APT is equal to 30°

```
12. Joint OT.
```

Let it meet PQ at the point R. Then Δ TPQ is isosceles and TO is the angle bisector of \angle PTO. [:'TP=TQ= Tangents from T upon the circle] :'OT \perp PQ :'OT bisects PQ. PR=RQ=4 cm Now, OR²=OP²-PR²=5²-4² OR=3 cm Now, \angle TPR+ \angle RPO=90°(:'TPO=90°) = \angle TPR+ \angle PTR(:'TRP=90°)



∴∠RPO=∠PTR

: Right triangle TRP is similar to the right triangle

PRO. [By A-A Rule of similar triangles]

 $\therefore \Rightarrow$ TP=20/3 cm.

13.Now join OB.

In right angle triangle OMB $OB^2 = OM^2 + MB^2$ (i) (by pythagoras theorem) we have, OM = 5cm and MB = 12cm Put the given value in equation (i) $\therefore OB^2 = (5)^2 + (12)^2$ = 25 + 144 = 169 $OB = \sqrt{169} = 13c$ we have, $OP^2 = OB^2 + PB^2$ $\therefore OP^2 = (13)^2 + (20)^2$ (length of tangent = 20 cm given) = 169 + 400 = 509

= 169 + 400 = 509 $OP = \sqrt{509} = 22.5 \text{ cm}$

Hence, the length of PO is 22.5 cm.

14.Given AB is tangent to the circle at A and OA is radius, $OA \perp AB$

In $\triangle ABD$

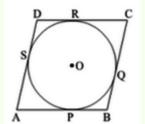
<DAB+<ABD+<ADB=180

90+50+<ADB=180

<ADB=40

<AOC=<OCD+<ODC=40+40=80

15.Given ABCD be a parallelogram circumscribing a circle with centre O. To Prove : ABCD is a rhombus.



We know that the tangents drawn to a circle from an exterior point are equal is length. \therefore AP = AS, BP = BQ, CR = CQ and DR = DS. AP+BP+CR+DR = AS+BQ+CQ+DS (AP+BP) + (CR+DR) = (AS+DS) + (BQ+CQ) \therefore AB+CD=AD+BC



or 2AB=2AD (since AB=DC and AD=BC of parallelogram ABCD) ∴ AB=BC=DC=AD Therefore, ABCD is a rhombus. Long Answer Questions

- 1. Proof of theorem 10.2
- 2. $\Delta ADO^{I} \sim \Delta ACO \Rightarrow \frac{AO^{i}}{AO} = \frac{DO^{i}}{CO} \Rightarrow \frac{r}{3r} = \frac{DO^{i}}{CO}$
- 3. The other two sides are 13 cm and 15 cm. (Hint: use area of triangle)
- 4. ∠RQS=30°
- 6. $\angle CQA=30^{\circ}, \angle CBA=60^{\circ}$
- 7. AB = 6.6 cm (PT=12 cm, x)²=64+x²)

 $\begin{array}{c} & & \\ & &$

8. i) 85°

ii) No, opposite angles of a cyclic quadrilateral are supplementary

iii) 1.5 times OB = 18cm

	CASE STUDY-1 (PLAYGROUND)						
QUESTION	Ι	II	III	IV	V		
ANSWER	(C) x m	(b)(3 – x) m	(d) Both b and c	(b) Quadrilateral BROQ is a square	(a) 1 m		
CASE STUDY-2 (CIRCLE DRAWING)	(a) 10 cm	(b) 5 cm	(c) 16 cm	(c) 1 cm	(c) 3		
ANSWER	(d) 10 cm	(c) 15 cm	(b) 9 cm	(d) 100°	(c) 11 cm		
CASE STUDY-4 (FERRIS WHEEL)	(C) 150°	(A) 75°	(B) 75°	(A) 90°	(A) 50m		
CASE STUDY-5 (PLAYGROUND)	(C) 5 m	(A) 18 m	(B) 11 m	(D) 90°	(A) 22 m		
CASE STUDY-6 (SPORTS DAY T-SHIRT)	a) 7	b) 5	d) 3	c) 24	b) 60		
CASE STUDY-7 (PARK)	(B) 90°	(D) All of these	(A) 4cm	(B) 120°	$\begin{array}{c} (C) AB+CD = \\ AD +BC \end{array}$		
CASE STUDY- 8	P1S1 and P2S2	150cm	(b) P2S2	30cm	140 ⁰		
CASE STUDY- 9	d) 90	b) 12m	c) 12m	d) $\angle RAS = 180 - \theta$	a) 90- (θ/2)		
CASE STUDY-10	a) 15m	c) both a and b	a) 0	c) 4	a) Parallel		



Areas related to Circles

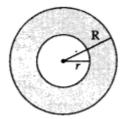
MCQ and CCT Questions

Summary

Circumference of a circle = $2\pi r$

Area of a circle = πr^2 [where r is the radius of a circle] Area of a semi-circle = $\pi r^2 / 2$

Area of a circular path or ring:



Let 'R' and 'r' be the radii of two circles

Then area of shaded part = $\pi R^2 - \pi r^2 = \pi (R^2 - r^2) = \pi (R + r)(R - r)$

Minor arc and Major Arc: An arc length is called a major arc if the arc length enclosed by the two radii is greater than a semi-circle.

If the arc subtends angle ' θ ' at the centre, then the

Length of minor arc $=\frac{\theta}{360} \times 2\pi r = \frac{\theta}{180} \times \pi r$

Length of major arc = $\left(\frac{360-\theta}{360}\right) \times 2\pi r$

Sector of a Circle and its Area

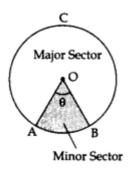
Sector is the region of the circle enclosed by the two radii and the arc between the two radiiA sector is called a minor sector if the minor arc of the circle is part of its boundary.

OAB is minor sector.

Area of minor sector = $\frac{\theta}{360} (\pi r^2)$

Perimeter of minor sector = $2r + \frac{\theta}{360} (2\pi r)$





(ii) A sector is called a major sector if the major arc of the circle is part of its boundary.

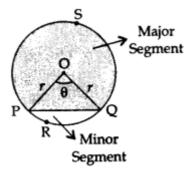
OACB is major sector

Area of major sector = $=(\frac{360-\theta}{360}) \times (2\pi r^2)$

Perimeter of major sector = $2r + (\frac{360-\theta}{360}) \times 2\pi r$

v. The sum of the arc lengths of major and minor sectors of a circle is equal to the circumference of the circle.

Minor Segment: The region enclosed by an arc and a chord is called a segment of the circle. The region enclosed by the chord PQ & minor arc PRQ is called the minor segment.



Area of Minor segment = Area of the corresponding sector – Area of the corresponding triangle

$$= \left[\frac{\theta}{360}\pi r^2 - \frac{1}{2}r^2\sin\theta\right]$$
$$= \frac{1}{2}r^2 \left[\frac{\theta}{180}\pi - \sin\theta\right] \text{ or } \frac{1}{2}r^2 \left[\frac{\theta}{180}\pi - 2\sin\frac{\theta}{2}\cos\frac{\theta}{2}\right]$$

Major Segment: The region enclosed by the chord PQ & major arc PSQ is called the major segment.

Area of major segment = Area of a circle – Area of the minor segment. [OR Area of major sector + Area of triangle]



$$= \pi r^2 - \frac{\theta}{360}\pi r^2 + \frac{1}{2}r^2\sin\theta = r^2 \left[\pi - \frac{\theta}{360}\pi + \frac{\sin\theta}{2}\right]$$

The sum of the areas of the major and minor sectors of a circle is equal to the area of the circle.

- Some useful results to remember;
- Angle described by minute hand in 60 minutes (1HOUR) = 360
- Angle decribed by minute hand in 1 minute = 6^0 (minute hand rotates through an angle of 6^0 in 1 minute)
- Angle described by the hour hand in 12 hours = 360
- Angle described by the hour hand in 1 hour $=\frac{360}{12}=30$

★ Angle described by the hour hand in 1 minute = $\frac{30}{60} = \frac{1}{2}$ (hour hand rotates through (1/2)⁰ in 1 minute.

SECTION A

MCQ QUESTIONS AND VSA (1 Mark)

Q1. If θ is the angle in degrees of a sector of a circle of radius r units, then the area of the sector is

(a.)	$\frac{\Pi r^2 \theta}{360}$	(c.)	$\frac{2\pi r\theta}{360}$
(b.)	$\frac{\pi r^2 \theta}{180}$	(d.)	<u>2πrθ</u> 180

Q2. Area of the largest triangle inscribed in a semi-circle of radius r units is

(a.) r^2 sq. units	(c.) $2r^2$ sq. units
(b.) $\frac{1}{2}$ r ² sq. units	(d.) $\sqrt{2} r^2$ sq. units

Q3. If the circumference of a circle and the perimeter of a square are equal, then the

(a.) Area of the circle = Area of the square

(b.) Area of the circle > Area of the square

(c.) Area of the circle < Area of the square

(d.) We cannot definitely say about the relation between area of the circle and the square

Q4. Radii of two circles are 4 cm and 3 cm respectively. There is another circle, which is having area equal to the sum of the areas of two circles whose radii are known. Find the diameter (in cm) of the third circle.

- (a.) 5 (c.) 0
- (b.) 7 (d.) 14



Q5. Which ratio is denoted by a constant known as π

(a) Diameter	(c) Circumference
(a.) $\overline{Circumference}$	(c.) <u>Diameter</u>
(b.) $\frac{Area}{Circumference}$	(d.) <u>Area</u> Diameter

Q6. The minute hand of a clock is 14 cm long. The area described by it on the face of the clock in 5 minutes is

- (a.) 51.33 cm^2 (c.) 21.15 cm^2
- (b.) 15.33 cm^2 (d.) 12.35 cm^2

Q7. Find area of the largest circle that can be drawn inside a rectangle with length a cm and breadth b cm. (a > b).

(a.) $\frac{a^2 \pi}{4} \text{ cm}^2$ (b.) $\frac{b^2 \pi}{2} \text{ cm}^2$ (c.) $\frac{b^2 \pi}{4} \text{ cm}^2$ (d.) $\frac{a^2 \pi}{2} \text{ cm}^2$

Q8. The ratio of areas of two circles whose ratio of circumferences is in the ratio of 3 : 1 will be

- (a.) 3:1 (c.) 1:9
- (b.) 1:3 (d.) 9:1

Q9. Area of a square is same as area of a circle. What will be the ratio of their perimeters?

- (a.) 1:1 (c.) $2:\sqrt{\pi}$
- (b.) $\pi : \sqrt{2}$ (d.) None of these

Q10. A display board is in the shape of a circle. While designing the board, if diameter of the board is increased by 40% from the previous design, then the area will be increased by

- (a.) 40% (c.) 96%
- (b.) 80% (d.) 45%
- Q11. Find circumference of a circle whose area is 314 cm2. (Given $\pi = 3.14$)

Q12. State the following statement is "True" or "False".

"If the perimeter and area of a circle are numerically equal, then the radius of the circle is 2 units".

Q13. Find the area of a sector of a circle of radius 28 cm and central angle 45°. (Take $\pi = \frac{22}{7}$)

Q14. If the perimeter of a semi-circular protractor is 66 cm, find the length of the straight-line part of the protractor. (Take $\pi = \frac{22}{7}$)

Q15. Area of a sector is one- twelfth that of the complete circle. Find the angle of the sector.

Q16. An arc of a circle of length 5π cm bounds a sector whose area is 20π cm². Find the radius of the circle.



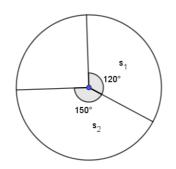
- Q17. A chord of a circle of radius 10 cm subtends right angle at the centre of the circle. What will be the area of the corresponding major sector. (Given $\pi = 3.14$)
- Q18. Rear wheel of a motor cycle is of radius 35 cm. It is assumed that the speed of the motor cycle is fully depend on the rpm of the rear wheel and no loss of energy. How many revolutions per minute (rpm) must the wheel make so as to keep a constant speed of 66 km/hr. (Take $\pi = \frac{22}{7}$)
- Q19. Find area of a sector of a circle of radius 5 cm, if the corresponding arc length is 3.5 cm.
- Q20. Say the following statement is "True" or "False". Write reason for your answer."Area of a segment of a circle is less than the area of its corresponding sector."

SECTION B

SHORT ANSWER QUESTIONS (2 MARKS)

- Q1. The circumference of a circle exceeds the diameter by 16.8 cm. Find the radius of the circle.
- Q2. Find the diameter of the circle whose area is equal to the sum of the areas of two circles of diameters 20cm and 48cm.
- Q3. All the vertices of a rhombus lie on a circle. Find the area of the rhombus, if area of the circle is $1256 \ cm^2$.
- Q4. A race track is in the form of a ring whose inner circumference is 352m and the outer circumference is 396m.Find the width of the track.
- Q5. A bicycle wheel makes 5000 revolutions in moving 11km.Find the diameter of the wheel.
- Q6. A wheel has diameter 84cm. Find how many complete revolutions must it take to cover 792m.
- Q7. A car travels 1 km distance in which each wheel makes 450 complete revolutions. Find the radius of its wheels.
- Q8. The perimeter of a sector of a circle of radius 5.2cm is 16.4cm. Find the area of the sector.
- Q9. An arc of a circle is of length 5π cm and the sector it bounds has an area of 20π cm². Find the radius of the circle.
- Q10. The minute hand of a clock is 10 cm long. Find the area of the face of the clock described by the minute hand 9 A.M and 9.35 A.M.
- Q11. The short and long hands of a clock are 4 cm and 6 cm long respectively. Find the sum of distances travelled by their tips in 2 days.
- Q12. If the perimeter of a sector of a circle of radius 6.5cm is 29cm, find its area.
- Q13. Find the ratio of the areas of two sectors S_1 and S_2 .





- Q14. Find the area of a sector whose perimeter is four times its radius r units.
- Q15. If the area of a circle inscribed in an equilateral triangle is given as 48π square units, then what is the perimeter of the triangle?
- Q16. It is given that area of a circle is equal to the sum of the areas of two circles of diameters 10cm and 24cm.then find the diameter of the larger circle.
- Q17. A piece of wire 20 cm long is bent into the form of an arc of a circle subtending an angle of 60° at its centre. Find the radius of the circle.
- Q18. Find the ratio of area of the circle circumscribing a square to the area of a circle inscribed in the square.
- Q19. A chord of circle of radius 10cm subtends a right angle at the centre. Find the area of the minor segment.
- Q20. A ceiling fan has 3 wings. Find the length of the arc described between two consecutive wings, where length of each wing is 0.98 m.

SECTION C

SHORT ANSWER QUESTIONS (3 MARKS)

- Q1. Calculate the perimeter of an equilateral triangle, if it is inscribed in a circle with area 154 cm².
- Q2. In a circle of radius 21 cm, an arc subtends an angle of 60° at the centre. Find the area of sector formed by the arc.
- Q3. A square is inscribed in a circle. Calculate the ratio of area of circle to that of square.
- Q4. The chord of a circle of radius 10 cm subtends a right angle at its centre. Find the length of the chord. (Given $\pi = 3.14$)
- Q5. The difference between circumference and radius of a circular field is 37 m. Find the area of the field. (Hint: $\pi = \frac{22}{7}$)
- Q6. Four poles are erected at four corners of a rectangular field of dimensions 80 m by 50 m. Vasanthi tethered a cow at one corner of the field with a rope. After tying the length of rope



from pole to cow is 7 m and Rajan tethered a buffalo at another pole of the same field and the length of rope from pole to animal is 6.3 m.

Answer the following questions.

- i. How much area of the rectangular field did the cow graze?
- ii. Find the ratio of grazing areas of the field by the cow and buffalo.
- Q7. Diameter of a garden roller is 1.4 m. Find the cost of painting both circular faces of the roller at the cost of ₹ 120 per sq. m. (Take $\pi = \frac{22}{7}$)
- Q8. Two circles touch externally. The sum of their areas is 130π cm². Distance between their centres is 14 cm, Find radius of each circle.
- Q9. A square of diagonal 18 cm is inscribed in a circular plate. The square portion is cut using a LASER cutter and taken out. Find the area of the remaining portion of the circular plate.
- Q10. A car has two wipers which do not overlap. Each wiper has a blade length of 25 cm and sweeping through an angle of 115°. What will be the total area of the glass wiped at each sweep of the wiper blades.
- Q11. The difference between the radii of the smaller circle and the larger circle is 7 cm and the difference between the areas of the two circles is 1078 sq.cm. Find the radius of the smaller circle.
- Q12. The central angles of two sectors of circles of radii 7cm and 21 cm are respectively 120^o and 40^o. Find the areas of the two sectors as well as the length of the corresponding arcs. What do you observe?
- Q13. In a circle with centre O and radius 5cm,AB is a chord of length $5\sqrt{3}$ cm. Find the area of sector AOB.
- Q14. A chord AB of a circle of radius 10 cm makes a right angle at the centre of the circle. Find the area of the minor and major segments.
- Q15. If the difference between the circumference and area of a circle is37 cm, find its area.

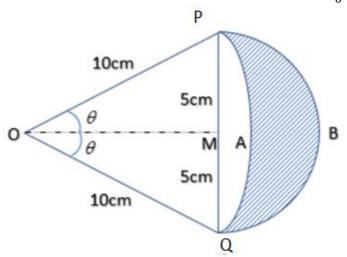
SECTION D

SHORT ANSWER QUESTIONS (4 MARKS)

- Q1. A boy is cycling such that the wheels of the cycle are making 140 revolutions per minute. If the diameter of the wheel is 60cm, calculate the speed per hour with which the boy is cycling.
- Q2. Two circles touch externally. The sum of their areas is 130π sq.cm and the distance between the centres is 14 cm. Find the radii of the circles.



- Q3. Two circles touch internally. The sum of their areas is $116 \pi cm^2$ and the distance between their centres is 6cm. Find the radii of the circles.
- Q4. Find the difference of the areas of a sector of angle 120⁰ and its corresponding major sector of a circle of radius 21 cm.
- Q5. A chord of a circle of radius 10cm subtends a right angle at the centre.find
 - (1) area of the minor sector (2) area of the minor segment
 - (2) area of the major sector (4) area of the major segment
- Q6. The figure given below shows two arcs A and B. Arc A is part of the circle with centre O and radius OP. Arc B is part of the circle with centre M and radius PM, where M is the midpoint of PQ. Show that the area enclosed by the two arcs is equal to $25 \left[\sqrt{3} \frac{\pi}{6}\right] cm^2$.



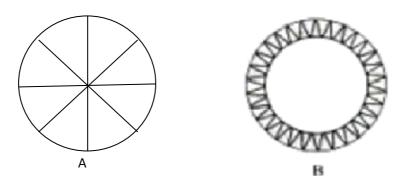
- Q7. Find the difference of the areas of two segments of a circle formed by a chord of length 5cm subtending an angle of 90^o at the centre.
- Q8. Find the area of the segment of a circle of radius 15 cm, when the angle of the corresponding sector is 120^o.
- Q9. Find the area of the minor segment of a circle of radius 42 cm, if length of the corresponding arc is 44 cm.
- Q10. The inner circumference of a circular track is 220m. The track is 7m wide everywhere. Calculate the cost of putting up a fence along the outer circle at the rate of Rs.2 per metre.

CASE STUDY BASED QUESTIONS

CASE STUDY 1

Q1. A brooch is a small piece of jewellery which has a pin at the back so it can be fastened on a dress, blouse or coat. Designs of some brooch are shown below. Ob serve them carefully.





Design A; Brooch A is made with silver wire in the form of a circle with diameter 28 mm. The wire is used for making 4 diameters which divide the circle into 8 equal parts.

Design B; Brooch B is made up of 2 colours.Gold and Silver.Outer part is made with gold.The circumference of silver part is 44 mm and the gold part is 3 mm wide everwhere.

Refer to Design A

- (i) Find the total length of silver wire required
- (ii) Find the area of each sector of the brooch
- (iii) REFER TO DESGN B; Find the circumference of the outer part (golden)
- (iv) A boy is playing with Brooch B; He makes revolutions with it along its edge. How many complete revolutions must it take to cover 80π mm?

CASE STUDY 2

In a Jewellery work shop, a brooch is made with silver wire in the form of a circle with diameter 35 mm. The wire is also used in making 5 diameters which divide the circle into 10 equal sectors as shown in Fig.



Q1. What is the radius of the circle?

- a) 35/2 mm
- b) 5/2 Mm
- c) 35mm
- d) 10mm
- Q2. What is the circumference of the brooch?
 - a) 100mm
 - b) 110 mm



- c) 50mm
- d) 10mm

Q3. What is the total length of silver wire required ?

- a) 528 mm
- b) 825mm
- c) 285mm
- d) 852mm

Q4. What is the area of each sector of the brooch?

- a) $385/2 \text{ mm}^2$
- ^{b)} 358/2 mm2
- c) $585/2 \text{ mm}^2$
- d) $385/4 \text{ mm}^2$

Short answe	er (1mark)							
1	А		11		62.8 cm			
2	А		12		True			
3	В		13		308 <i>cm</i> ²			
4	С		14		21cm			
5	С		15		30			
6	А		16		8cm			
7	В		17		$235.5 cm^{2}$			
8	D		18		500rpm			
9	С		19		8.7 <i>cm</i> ²			
10	С		20		false			
-	ISWER (2 MARK	(S)						
1	3.92 cm		11		1910.85 cr	n		
2	d = 52 cm		12		52 sq.cm			
3	800 sq.cm		13		4:5			
4	7 m		14		r^2 sq.units			
5	70 cm		15		$48\sqrt{3}$ units	5		
6	300		16		26cm.			
7	35.35 cm		17		$\frac{60}{\pi}$ cm			
8	15.6 sq.cm		18		2:1			
9	r = 8 cm		19		285.5			
10	183.3 sq.cm		20		2.05 m			
SHORT ANS	SWER (3 MARKS	5)						
1	423cm	6			5sq.cm,	11	r = 21 cm	
2	221 ag am	7		100	369.6	12	154/3,154,44/3,44/3arc	
2	231 sq.cm	/		KS	509.0	12	lengths of 2 circles of	
							diff. Radii may be	
							same but areas need	
							not be equal.	
		1		1		1	not of equilit	

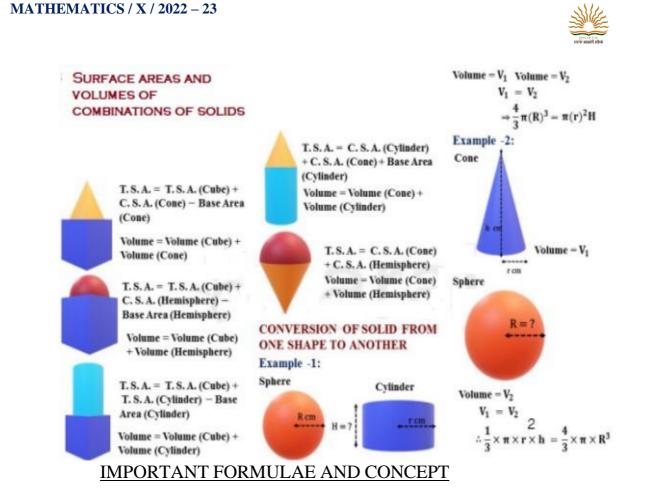


3	П :2	8		11cm and	3	13	25π m^2
				cm			$\frac{23\pi}{3}$ cm ²
4	102 cm	9		92.57 sq.c	m	14	$28.5 \ cm^2, 285.5 \ cm^2$
5	157 sq.cm	10		1254.96		15	154 <i>cm</i> ²
	-			sq.cm			
LONG ANSW	ER (4 MARKS)						
1	15.84 km/hr		6	$25\left[\sqrt{3}-\frac{\pi}{6}\right]cm^2$		cm ²	
2	11cm,3 cm 7			$\frac{25}{4}(\pi$	$\frac{25}{4}(\pi+2)$		
3	3 10 cm, 4cm 8				$75\pi - \frac{225}{4}\sqrt{3} \ cm^2$		
4	$462 cm^2$		9		160	sq.cm ap	prox.
5	78.5,28.5,235.	5,285.5	10		Rs.5	28	
	<u>C</u>	ASE ST	UDY BA	ASED QUE	STIC	NS	
CASE STUY 1 (1) 200M		(2) $77mm^2$		(3) 8	32.2 mm	(4) 2	
CASE STUDY 2 1.(a)		(2) b		(3) 0	2	(4) d	

MENSURATION - SURFACE AREA AND

VOLUMES

Name of the solid	Figure	Volume	Laterial/Curved Surface Area	Total Surface Area
Cuboid	h b	lbh	2lh + 2bh or 2h(l+b)	2lh+2bh+ <mark>2lb</mark> or 2(lh+bh+lb)
Cube	a aaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaa	a ³ 4a ²		4a ² +2a ² or 6a ²
Right circular cylinder	H H	πr²h	2πrh	$2\pi rh + 2\pi r^{2}$ or $2\pi r(h+r)$
Right circular cone	h	$\frac{1}{3}\pi r^{2}h$	$\frac{1}{3}\pi r^{3}h$ πr^{1}	
Sphere		$\frac{4}{3}\pi r^{3}$	$4\pi r^2$	$4\pi r^2$
Hemisphere	r	$\frac{2}{3}\pi r^{3}$	$2\pi r^2$	$2\pi r^2 + \pi r^2$ or $3\pi r^2$



Surface areas and volumes of combinations of solids

Surface areas and volumes of combinations of solids of any two of the following:

cubes, cuboids, spheres, hemispheres and right circular cylinders/cones.

Deleted Topics

• Conversion of Solid from One Shape to Another

Problems involving converting one type of metallic solid into another and other mixed problems. (Problems with combination of not more than two different solids).

Frustum of a cone (Total surface area and volume of Frustum of a cone)

SURFACE AREA AND VOLUMES

MULTIPLE CHOICE QUESTIONS(1 Mark each)

SECTION A

Q1. The ratio of the total surface area of a solid hemisphere to the square of its radius is

- a) $2\pi : 1$ c) $4\pi : 1$
- b) $3\pi:1$ d) $1:4\pi$

Q2. Two cubes each of volume $8cm^3$ are joined end to end, then the surface area of the resulting



cuboid is

a)	$80 cm^2$	c)	$40 cm^2$
b)	64 <i>cm</i> ²	d)	$8cm^2$

Q3. The radius of a sphere is r cm. The sphere is divided into two equal parts. The whole surface area of two parts will be:

a)	$8\pi r^2$	c)	$4\pi r^2$
b)	$6\pi r^2$	d)	$3\pi r^2$

Q4. If the radius of the base of a right circular cylinder is halved, keeping the height same, the ratio of the volume of the reduced cylinder to that of original cylinder is

a)	2:3	c)	1:4
b)	3:4	d)	4:1

Q5. The surface area of the two spheres are in the ratio 1 : 2. The ratio of their volumes is :

a)	$\sqrt{2:1}$	c)	1:8
b)	$1:2\sqrt{2}$	d)	1:4

Q6. If the areas of three adjacent faces of a cuboid are X, Y and Z respectively, then the volume of cuboid is :

a)	XYZ	c)	\sqrt{XYZ}
b)	2XYZ	d)	$\sqrt{2XYZ}$

Q7. The radii of two cylinders are in the ratio 2 : 3 and their heights are in the ratio 5 : 3. Ratio of their volumes is

a)	27:20	c)	9:4
b)	20:27	d)	4:9

Q8. The radius of a wire is decreased to one third. If the volume remains the same, the length will become

a)	3 times	c)	9 times
b)	6 times	d)	27 times

Q9. The ratio of the volumes of two spheres is 8:27. If r and R are the radii of spheres respectively then (R - r): r is :

- a) 1:2 c) 2:3
- b) 1:3 d) 4:9

Q10. The circumference of the edge of a hemispherical bowl is 132 cm. When π is taken as 22/7



the capacity of the bowl in cm^3 is :

a)	2772	c)	19404
• •		•	

b) 924

d) 9702

OBJECTIVE QUESTIONS (1 MARK)

- Q11. The surface area of a sphere is same as the curved surface area of a right circular cylinder whose height and diameter are 12 cm each. Find the radius of the sphere.
- Q12. Find the volume of the greatest sphere that can be cut from a cylindrical log of wood of base radius 1 cm and height 5 cm.
- Q13. Find the curved surface area of a right circular cone of height 15 cm and base diameter 16 cm.
- Q14. A cone and a hemisphere have equal bases and equal volumes. What is the ratio of their heights?
- Q15. Find the volume of a right circular cylinder of base radius 7 cm and height 10 cm .
- Q16. If h, c and V respectively are the height, curved surface area and volume of a cone then find $3\pi Vh^3 - c^2h^2 + 9V^2 = \dots$
- Q17. How many bags of grain can be stored in a cubic granary 12m x 6m x 5m, if each bag occupies a space of 0.48 m³?
- Q18. The volume of two cubes are in the ratio 8:64, then find the ratio of their surface areas.
- Q19. A cylinder and a cone are of same base radius and of same height. What is the ratio of their volumes?
- Q20. Find the Total Surface Area of a hemispherical solid having radius 7 cm.

SHORT ANSWER TYPE QUESTIONS – 2 MARKS

SECTION-B

- Q21. Two cubes each of volume27cm³ are joined end to end to form a solid. Find the surface area of the solid.
- Q22. 22.Two cubes each of side 4cm are joined end to end. Find the volume of the resulting solid.
- Q23. Volume and surface area of a solid hemisphere are numerically equal. What is the diameter of hemisphere?
- Q24. If the total surface area of a solid hemisphere is 462 cm^2 , find its radius.
- Q25. A wallpaper, 312m long and 25cm wide is required to cover the walls of a room. Length of the room is 7m and its breadth is twice its height. Determine the height of the room.
- Q26. The surface area of a sphere is 616 cm². Find its radius.



- Q27. The radii of 2 cylinders are in the ratio 3:5 and their heights are in the ratio 2:3. What is the ratio of their curved surface areas.
- Q28. 28.The base radii of 2 right circular cones of the same height are in the ratio 3:5. Find the ratio of their volumes.
- Q29. The circumference of the base of a 9m high wooden solid cone is 44m. Find its volume.
- Q30. Find the volume of the largest right circular cone that can be cut out of a cube whose edge is 9cm.
- Q31. A toy is in the form of a cone mounted on a hemi-sphere of same radius. The diameter of the base of the conical part is 7cm and the total height of the toy is 14.5cm. find the volume of the toy.
- Q32. The TSA of a solid cylinder is 231 cm^2 . If its CSA is $\frac{2}{2}$ of its TSA. Find its radius and height.
- Q33. The length of a hall is 20m and width is 16m. the sum of the areas of the floor and the flat roof is equal to the sum of the areas of the four walls. Find the height of the hall.
- Q34. A cone and a cylinder of same radius 3.5cm have same CSA. If height of the cylinder is 14cm then find the slant height of the cone.
- Q35. A circus tent is cylindrical up to a height of 3m and conical above it. If the diameter of the base is 105m and the slant height of the conical part is 53cm, find the total canvas required in making the tent.
- Q36. A bird-bath in a garden is in the shape of a cylinder with a hemi-spherical depression at one end. The height of the hollow cylinder is 1.45m and its radius is 30cm. find the TSA of the bird-bath.
- Q37. A tent is in the shape of a cylinder of diameter 20m and height 2.5cm, surmounted by a cone of equal base and height 7.5m. find the capacity of the tent.(take $\pi = 3.14$)
- Q38. A vessel in the shape of a hollow hemi-sphere mounted by a hollow cylinder. The diameter of the hemi-sphere is 14cm and the total height of the vessel is 13cm. find the inner surface area of the vessel.
- Q39. A conical vessel whose inner radius is 10cm and height 48cm is full of water. Find the volume of water in it.
- Q40. Fifty circular plates each of radius 7cm and thickness 0.5cm are placed one above another to form a solid right circular cylinder. Find its TSA.



SHORT ANSWER TYPE QUESTIONS – 3 MARKS

SECTION-C

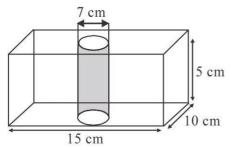
- Q41. A toy is in the form of a cone mounted on a hemisphere of same radius 7 cm. If the total height of the toy is 31 cm, find its total surface area.
- Q42. Two cones with same base radius 8 cm and height 15 cm are joined together along their bases. Find the surface area of the shape so formed.
- Q43. A solid is in the shape of a cone surmounted on a hemisphere. The radius of each of them is3.5 cm and the total height of the solid is 9.5 cm. Find the volume of the solid.
- Q44. A solid cylinder of radius r and height h is placed over another cylinder of same height and radius. Find the total surface area of the shape so formed
- Q45. An ice cream cone consists of a cone surmounted by a hemisphere. The radius of the hemisphere is 3.5 cm and height of the ice cream cone is 12.5 cm. Calculate the volume of the ice cream in the cone.
- Q46. The sum of the radius of base and height of a solid right circular cylinder is 37 cm. If the total surface area of the solid cylinder is 1628 sq. cm, find the volume of the cylinder
- Q47. The radius and height of a solid right circular cone are in the ratio of 5 : 12. If its volume is 314 cm³, find its total surface area. (Use $\pi = 3.14$)
- Q48. A cone of maximum size is carved out from a cube of edge 14 cm. Find the surface area of the solid left out after the cone is carved out.
- Q49. The largest possible cylinder is cut out from a wooden cube of edge 8 cm. Find the volume of wood remaining in the cube.
- Q50. A semi-circular sheet of paper of diameter 28 cm is bent into an open conical cup. Find the depth and capacity of the cup.
- Q51. A solid sphere of diameter 14 cm is cut into two halves by a plane passing through the centre. Find the combined surface area of the two hemispheres so formed.
- Q52. If the radius of the base of a right circular cylinder is halved, keeping the height same, find the ratio of the volume of the reduced cylinder to that of the original cylinder.
- Q53. From a solid cylinder of height 14 cm and base radius 7 cm, two identical conical holes from each end of radius 2.1 cm and height 4 cm are drilled out. Find the volume of the remaining solid.
- Q54. A petrol tank is a cylinder of base diameter 21 cm and length 18 cm fitted with a conical end of length 9 cm. Determine the capacity of the tank.



Q55. A rocket is in the form of a cylinder, closed at the lower end, has a cone attached to its top. If each one has a radius 20 cm and height 21 cm, find the surface area of the rocket.

LONG ANSWER OUESTIONS (4 MARKS)

- Q56. A solid is in the shape of a cone mounted on a hemisphere of same base radius. If the curved surface areas of the hemispherical part and the conical part are equal, then find the ratio of the radius and the height of the conical part.
- Q57. A tent is in the shape of a right circular cylinder up to a height of 300 cm and conical above it. The total height of the tent is 1350 cm and radius of its base is 1400cm. Find the cost of cloth required to make the tent at the rate of Rs.80 per square metre. (Take $\pi = 22/7$)
- Q58. From a cuboidal solid metallic block of dimensions 15cm x 10cm x 5cm a cylindrical hole of



diameter 0.07m is drilled out. Find the surface area of the remaining block. (π = 22/7)

- Q59. A hollow cylindrical pipe is made up of copper. It is 21 dm long. The outer and inner diameters of the pipe are 10cm and 6cm respectively. Find the volume of copper used in making the pipe (π = 22/7)
- Q60. A circus tent is in the form of a right circular cylinder with right circular cone above it. The
 - i. diameter and the height of the cylindrical part of the tent are 126m and 12m respectively. The total
 - ii. height of the tent is 28m. Find the total cost of the tent if the canvas used costs Rs.30 per sq.m.
- Q61. A right circular cylinder and a cone have equal bases and equal heights. If their curved surface areas are in the ratio 8:5, show that the ratio between the radius of their bases to their heights is 3:4
- Q62. A metallic cylinder has radius 3cm and height 5cm. To reduce its weight, a conical hole is drilled in the cylinder. The conical hole is drilled in the cylinder. The conical hole has a radius of 3/2 cm. and its depth is 8/9cm. Calculate the ratio of the volume of metal left in the cylinder to the volume of metal taken out in the conical shape.
- Q63. A rectangular sheet of paper 30cm x 18cm can be transformed into the curved surface of a right circular cylinder in two ways either by rolling the paper along its length or by rolling it



along its breadth. Find the ratio of the volume of the two cylinders thus formed.

- Q64. The internal and external diameters of a hollow hemispherical vessel are 12cm and 16cm respectively. If the cost of painting 1 sq.cm of the surface area is Rs. 5, find the total cost of painting the vessel all over. ($\pi = 3.14$)
- Q65. The sum of the radius of the base and height of a solid right circular cylinder is 37cm. if the total surface area of the solid cylinder is 1628 sq.cm, find the volume of the cylinder. (π = 22/7)

CASE STUDY BASED QUESTIONS

Case study question 1 An antique box and its dimensions excluding the stand is given





below.

- 1. What is the volume of the jewellery box?
 - a) $(l \times b \times h) + \pi r^2 h$ c) $2(lb \times bh \times lh) + \pi r^2 h$
 - b) $(l \times b \times h) + \frac{1}{2}\pi r^2 h$ d) $(l \times b \times h) + 2\pi r h$
- 2. How much brass will be needed to plate the curved surface of the dome as shown in figure?

a) 1320cm ²	c) 440 cm^2
b) 220 cm^2	d) 660 cm^2

- 3. How many sheets of dimensions 14cm x 30cm x 2cm can be placed in the box?
 - a) 10 c) 2
 - b) 5 d) 15

4. Considering the thickness of the box to be negligible, how much velvet cloth will be needed to cover the cuboidal inner area?

a) 1720 cm^2

b) 880 cm²



c) 1300 cm^2

Case study question- 2

During Covid times people prefer using homogenized milk, UHT Processed and aseptically packed in an exceptional six layer, tamper-proof Tetra Packaging with 0% bacteria and 100% pure health. This new six layer interfere proof, prevents air and freshness, light and bacteria from entering the pack. As an effect, the milk stays fresh and pure for a minimum of 180 days until opened, even without refrigeration. The 500ml milk is packed in cuboidal containers of dimensions $15 \times 8 \times 5$. These milk packets are then packed in cuboidal cartons of dimension $30x 32 \times 15$. (All dimensions are in **cm**)



Based on the above given information answer the following questions

1) Find the total surface area of a milk box.

a) 1890cm ²	c) 470cm ²
b) 400 cm^2	d) 600 cm^2

2) How many milk packets can be filled in a carton?

a) 12	c) 20
-------	-------

b) 24 d) 8

- 3) How much milk will the cup contain?
 - a) 1200 L c) 11 L 10 ml b) 1 L 100ml d) 100 L
- 4) How much cardboard is needed to make the carton if 10% of wastage is taken into account.

a) 3310 cm^2

d) 1580 cm²



^{d)} 3969 cm^2

b) 2100 cm^2

c) 4200 cm^2

Question	Answer	Question	Answer
1	b) 3π : 1	11	6 cm
2	c) 40 cm^2	12	$\frac{4}{3}\pi$
3	b) 6πr2	13	136π
4	c) 1:4	14	2:1
5	b) 1 : 2 √ 2	15	1540 cm^3
6	c) √ <i>XYZ</i>	16	0
7	b) 20:27	17	750
8	c) 9 times	18	4:9
9	a) 1:2	19	3:1
10	c) 19404	20	462

SECTION-A ANSWER KEY

SECTION-B

1.90cm^2	6) 7cm	11) 231cm ³	16) $3.3m^2$
2) 128cm^3	7) 2:5	12) 3.5cm, 7cm	17) 1570m ²
3) 9units	8) 9:25	13) 8.8m	18) 572cm^2
4) 7cm	9) 462cm^3	14) 28cm	19) 5024 cm ²
5) 3m	10) 190.93cm ³	15) 9735m ²	20) 1408cm^2

SECTION-C

1. 858 cm^2	6. 4620 cm ³	11. 924 cm^2
2. $854 \frac{6}{7} \text{ cm}^2$	7. 266.9 $\rm cm^2$	12. 1:4
3. 166.83 cm^3	8. 1365.2 cm ²	13. 2119.04 cm^3
4. $2\pi r^{2} + 4\pi rh$ sq. units	9. 109.8 cm^3	14. 29106 cm ³
5. 205.33 cm^3	10. $718\frac{2}{3}$ cm ³	15. 5720 cm^2



SECTION-D

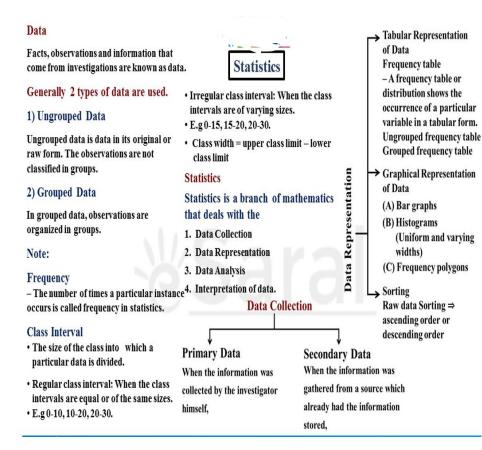
1. 1:√ 3	6) 3:4
2. Rs.82720	7) 133: 2
3. 583sq.cm	8) 5:3
4. 10560cub.cm	9) Rs. 3579.60
5.Rs.528660	10) 4620 cub.cm

CASE STUDY-1	CASE STUDY-2
1. (b) $(lxbxh) + \frac{1}{2}\pi r^{2}h$	1 b)470cm ²
2 (d) 660 cm ²	2. c) 24
3 (b) 5	3. c) 1 L 100ml
4 (c) 1300 cm^2	4. a) 3310 cm^2



STATISTICS

MIND MAP



ARITHMETIC MEAN

- > Direct Method $\bar{x} = \frac{\sum f_i x_i}{\sum f_i}$
- Assumed Mean Method
- Step Deviation Method

$$\bar{x} = a + \frac{\sum f_i d_i}{\sum f_i}$$
$$\bar{x} = a + \frac{\sum f_i u_i}{\sum f_i}$$

COMPUTATION OF MODE FOR A CONTINOUS FREQUENCY DISTRIBUTION

MODE

<u>Algorithm</u>

- 1. Obtain the continuous frequency distribution
- 2. Determine the class of maximum frequency either by inspection or by grouping method
- 3. This class is called the modal class
- 4. Obtain the values of the following from the frequency distribution table

l = lower limit of the modal class

$$f_1 = frequency of modal class$$



h = width(size) of the modal class $f_0 = frequency of the class preceding the modal class$ $f_2 = frequency of the class following the modal class$

Mode =
$$l + \left(\frac{f_1 - f_0}{2f_1 - f_0 - f_2}\right) h$$

MEDIAN OF GROUPED DATA

Algorithm

- 1. Obtain the frequency distribution
- 2. Prepare the cumulative frequency column
- 3. Obtain $n = (\sum f_i)$ and $\frac{n}{2}$
- 4. See the cumulative frequency just greater than (nearer to) $\frac{n}{2}$ and determine the corresponding class. This class is known as *median class*
- 5. Obtain the values of the following from the frequency distribution table
- l = lower limit of the median class
- f = frequency of median class
- h = width(size) of the median class
- cf = cumulative frequency of the class preceding the median class

Substitute the values in the following formula

Median =
$$l + \left(\frac{\frac{n}{2} - cf}{f}\right)h$$

THE EMPIRICAL RELATIONSHIP BETWEEN THE THREE MEASURES OF CENTRAL TENDENCY

3 median = mode + 2 m

MULTIPLE CHOICE QUESTIONS (1 MARK)

SECTION A

Choose the correct answer from the following:

Q1. The Arithmetic Mean of 1,2, 3, 4, n is

(a)	n+1		
(a)			
()	2		
	2		
	n		

(b)	$\frac{n}{2}$	(d)	$\frac{n}{2}$	+1

Q2. Which is the empirical relation between Mean, Median and Mode

- (a) 3Mean =Mode +2Median
- (b) 3Median=Mode +2Mean

- (c) 2Median= Mode +3Mean
- (d) 3Median=Mode -2Mean

(c)

Q3. Mean of the following distribution is 2.5. Find the value of 'y'



	Variable x	1	2	3	4	5			
	Frequency y	y 4	5	Y	1	2			
	(a) 3 (c) 5								
	(b) 4 (d) 2								
Q4.	If Arithmetic M	Aean of x, z	x+2, x+4 a	and x+6 is 5	5. Then find	the value of x is			
	(a) 3				(c) 1				
	(b) 2				(d) 5	5			
Q5.	If Median of da	ata 16,18, 2	20, 24-x, 2	0 + 2x, 28,	30, 32 is 24	then x is			
	(a) 4				(c) 1	6			
	(b) 18				(d) 2	20			
Q6.	If mean of first	n natural 1	number is	$\frac{5n}{2}$ then n	is				
	(a) 5			9	(c) 9)			
	(a) 5 (b) 4 (c) 5 (d) 10								
Q7.		five numbe	er is 15 If	we include		umber, the mean of			
V ¹	numbers becon					united, the mean of			
	(a) 24		menadea i		(c) 2	26			
	(b) 2				(d) $\frac{1}{2}$				
Q8.		sum of de	viation of	frequency a		from its mean is			
X 00	(a) 0		viacion or	nequency	(c) -				
	(b) 1				(d) 2				
Q9.	For the followi	ng distribu	tion.						
		8	7						
	Class	0-5	5-10	10-15	15-20	20-25			
	Interval								
	Frequency	10	15	12	20	9			
	The sum	of lower li	mits of M	edian class	and Modal	class is			
	(a) 15				(c) 3	80			
	(b) 25				(d) 3				
		<i>c c c c c c c c c c</i>			40.1				
Q10.	If Mode of data	a 64, 60, 48	3, x, 43, 48	3, 43, 34 is	43 then $x+3$	15			

- (b) 45
- (c) 46
- (d) 48



Answer the following (1 mark each)

- Q11. Find the median of first 9 prime numbers.
- Q12. The mean and median of the data are 14 and 15. Find the value of mode.
- Q13. Find the lower limit of the modal class:

Class	0-10	10-20	20-30	30-40	40-50
Frequency	5	8	13	7	6

Q14. If $u_i = \frac{xi-25}{10}$, $\sum f_i u_i = 20$ and $\sum f_i = 100$, then find mean.

Q15. Find the frequency of class 30-40.

More than or equal to	51
30	
More than or equal to	48
40	
More than or equal to	42
50	

- Q16. If the difference of mode and median of the data is 24, then find the difference of median and mean.
- Q17. If arithmetic mean of 7, 8, x, 11, 14, is x, find x.
- Q18. If mean of 6, 7, x, 8, y, 14 is 9, find x+y.
- Q19. Find the mean of first n odd natural numbers.
- Q20. Find the class mark of the class 10 25.

Short Answer Questions (2 Marks questions) SECTION B

Q1. Find the mode of the following data:

CI	1-3	3-5	5-7	7-9	9-11
F	7	8	2	2	1

Q2. From the following distribution, find the lower limit of the median Class:

CI	85-89	90-94	95-99	100-104	105-109
F	10	12	11	5	30

Q3. Find the value of p, if the arithmetic mean of the following distribution is 25:

CI	0-10	10-20	20-30	30-40	40-50
F	5	8	15	р	6



- Q4. Find the mean, if $d_i = x_i 25$; $\sum f_i d_i = 20$; $\sum f_i = 100$.
- Q5. Find the value of x, if the mode of following distribution is 45.

CI	0-20	20-40	40-60	60-80	80-100
F	5	10	Х	6	3

Q6. An inter house cricket match was organised by a school. Distribution of run made by the students is given below. Find the median runs scored.

Runs Scored	0-20	20-40	40-60	60-80	80-100
No. of Students	4	6	5	3	4

Q7. Find the mode of following frequency distribution:

Class	10-20	20-30	30-40	40-50	50-60
Frequency	15	10	12	17	4

- Q8. Find the mean of the data using an empirical formula when it is given that mode is 50.5 and median is 45.5.
- Q9. Find the mean of the Following distribution:

Class	3-5	5-7	7-9	9-11	11-13
frequency	5	10	10	7	8

- Q10. If the mean of first n natural numbers is 15, then find n.
- Q11. Given below is a cumulative frequency distribution showing the marks secured by 50 students:

Marks	Below 20	Below 40	Below 60	Below 80	Below 100
No. of Students	17	22	29	37	50

Form frequency distribution table for the data.

- Q12. The mean and median of 100 observations are 50 and 52 respectively. The value of the largest observation is 100. It was later found that it is 110 not 100. Find the true mean and median.
- Q13. If the median of a series exceeds the mean by 3, find by what number the mode exceeds its mean?
- Q14. Find the mean of first five odd multiples of five.
- Q15. Find the x and y from the following cumulative frequency distribution:

Class	0-8	8-16	16-24	24-32	32-40
frequency	15	Х	15	18	9
Cumulative	15	28	43	у	70
frequency					

Q16. Calculate the median from the following data:

CI	0-10	10-20	20-30	30-40	40-50
F	5	15	30	8	2



- Q17. In a frequency distribution, if a = assumed mean =55, $\sum f_i = 100$, h=10 and $\sum f_i u_i$ =-30 then find the mean of the distribution.
- Q18. Change the following distribution into a less than type distribution table:

CI	200-300	300-400-	400-500	500-600	600-700
F	12	18	35	20	15

Q19. Change the following distribution into a more than type distribution table.

Class	0-10	10-20	20-30	30-40	40-50	50-60	60-70
Frequency	5	15	20	23	17	11	9

Q20. For the following distribution, find the modal class:

Marks	Below10	Below20	Below30	Below40	Below50	Below60
No. of	3	12	27	57	75	80
Students						

SHORT ANSWER TYPE QUESTION (3 MARKS) SECTION C

Q1. The following table gives the life time of 400 neon lamps.

Life time (in	1500- 2000	2000- 2500	2500- 3000	3000- 3500	3500- 4000	4000- 4500	4500- 5000
hours)							
No. of lamps	14	56	60	86	74	62	48

Find the median life time of a lamp.

Q2. The mean of the following distribution is 48 and the sum of all frequencies is 50. Find the missing frequencies

Class	20-30	30-40	40-50	50-60	60-70
Frequency	8	6	Х	11	у

Q3. The median of the distribution given below is 14.4. Find the values of 'x' and 'y', if the sum of frequency is 20.

Class interval	0-6	6-12	12-18	18-24	24-30
Frequency	4	Х	5	у	1

Q4.Find mean and mode of the given data. Also find median using Empirical Formula.

Class	20-30	30-40	40-50	50-60	60-70
Frequency	25	40	42	33	10

Q5.The median of the following data is 525. Find the missing frequency 'x'



Class	0-	100-	200-	300-	400-	500-	600-	700-	800-	900-
	100	200	300	400	500	600	700	800	900	1000
Frequency	2	5	Х	12	17	20	15	9	7	4

Q6.Data regarding the height of students of class X is given Find the average height of students of the class

Height (in cm)	150-156	156-162	162-168	168-174	174-180
Number of	4	7	15	8	6
students					

Q7.Find the median for the following frequency distribution

Class	0-6	6-12	12-18	18-24	24-30
Frequency	1	4	9	3	3

Q8.Find the mode of the following distribution

Class	0-10	10-20	20-30	30-40	40-50
Frequency	8	12	10	11	9

Q9. The median of the data is 46. Find the value of p and q

Marks	10-20	20-30	30-40	40-50	50-60	60-70	70-80
Frequency	12	30	р	65	q	25	18

Q10. The mean of the following data is18.75.Find p

Class marks	10	15	Р	25	30
Frequency	5	10	7	8	2
F' 1.4	6.41 6.11	1.4			

Q11. Find the mean of the following data.

Class	Less than 20	Less than 40	Less than 60	Less than 80	Less than 100
Frequency	15	37	74	99	120

Q12. Monthly pocket money of students of a class is given in the following frequency distribution:

POCKET	100-125	125-150	150-175	175-200	200-225
MONEY					
NO OF	14	8	12	5	11
STUDENTS					

Find mean pocket money using step deviation method.

Q13. Find the mean of the following distribution by Assumed Mean Method:



CI	10-20	20-30	30-40	40=50	50-60	60-70	70-80	80-90	90-100
Frequency	8	7	12	23	11	13	8	6	12

Q14. Heights of students of class X are given in the following frequency distribution:

HEIGHTS	150-155	155-160	160-165	165-170	170-175
(CM) NO OF	15	8	20	12	5
STUDENTS					

Find the modal height.

Q15. For helping poor girls of their class, students saved pocket money as shown in the following table:

MONEY	5-7	7-9	9-11	11-13	13-15
SAVED IN					
RUPEES					
NO OF	6	3	9	5	7
STUDENTS					

Find median for this data.

LONG ANSWER TYPE QUESTIONS (4 MARKS)

SECTION D

1) If mode of the following distribution is 55, then find the value of x.

Class	0-15	15-30	30-45	45-60	60-75	75-90
Frequency	10	7	Х	15	10	12

2) If the median of the distribution is 28.5, find the values of x and y

Class	0-10	10-20	20-30	30-40	40-50	50-60	Total
Frequency	5	Х	20	15	у	5	60

3) The daily wages of 110 workers obtained in a survey are tabulated below. Compute the mean daily wages and modal daily wages of these workers.

Daily	100-120	120-140	140-160	160-180	180-200	200-220	220-240
wages							
(Rs)							
No. of	10	15	20	22	18	12	13
workers							

4) The mean of the following distribution is 53. Find the missing frequencies f1 and f2

,		0		U	1	
Classes	0-20	20-40	40-60	60-80	80-100	Total
Frequency	15	f1	21	f2	17	100

5) The lengths of 40 leaves of plant are measured correct to the nearest millimetre and the data is given



Length	118-126	127-135	136-144	145-153	154-162	163-171	172-180
in mm							
Number of leaves	3	5	9	12	5	4	2

Find the median length of leaves

6) Find the missing frequency x of the following data if its mode is 240 rupees

Expenditure	0-100	100-200	200-300	300-400	400-500
Number of	140	230	270	Х	150
families					

7) The following distribution gives the monthly consumption of electricity of 68 consumers of a locality .As Mr.Syam always saves electricity by switching off after usage, his family belongs to 65-85

	5	5	5	0	\mathcal{O}	5	0
Monthly	65-85	85-105	105-125	125-145	145-165	165-185	185-205
consumption							
Number of	4	5	13	20	14	8	4
consumers							

Find the mean and mode of the data. Also find the median using empirical formula 8) Find the values of x and y if the median of the following data is 31

Class	0-10	10-20	20-30	30-40	40-50	50-60	Total
Frequency	5	Х	6	Y	6	5	40

9) Mode of the distribution is 65 and sum of frequencies is 70.find x and y

Class	0-20	20-40	40-60	60-80	80-100	100-	120-	140-
						120	140	160
Frequency	8	11	Х	12	Y	9	9	5
10) Find mo	do of the f	allowing	listribution		•		•	•

10) Find mode of the following distribution

Class	25-35	35-45	45-55	55-65	65-75	75-85				
Frequency	7	31	33	17	11	1				
CASE STUE	CASE STUDY BASED QUESTIONS									

Case Study Question 1

Direct income in India was drastically impacted due to the COVID-19 lockdown. Most of the companies decided to bring down the salaries of the employees up to 50%.





The following table shows the salaries (in percent) received by 50 employees during lockdown.

U				
Salary received in	50-60	60-70	70-80	80-90
%				
Number of	18	12	16	4
employees				

Based on the above information, answer the following questions.

- i. Find the total number of persons whose salary is reduced by more than 20 %.
- ii. Calculate the median of the given data

Case Study Question 2

Electricity energy consumption is the form of energy consumption that uses electric energy. Global electricity consumption continues to increase faster than world population, leading to an increase in the average amount of electricity consumed per person (per capita electricity consumption).

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		a Kendra, Sansad Marg, New Delhi - 110 001 vrber ihr: vre wrl, vd ftreh-110001			Pay By Date	30/06/2015
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A survey is conducted for 56 families of a Colony A. The following table gives the weekly consumption of electricity of these families.

Weekly consumption (in units)	0-10	10-20	20-30	30-40	40-50	50-60
No. of families	16	11	19	6	4	0

i. Find the difference between upper limit of the modal class and lower limit of median class.

ii. Calculate mean of the data.

Case Study Question 3

An electric scooter manufacturing company wants to declare the mileage of their electric scooters. For this, they recorded the mileage (km/ charge) of 50 scooters of the same model. Details of which are given in the following table.



Mileage (km/charge)	100-120	120-140	140-160	160-180
Number of scooters	7	12	18	13

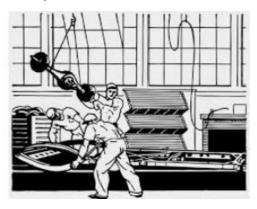


Based on the case given, answer the following

- i. Find the average mileage.
- ii. Find the average of maximum number of scooters.

Case Study Question 4

As the demand of the products grew, a manufacturing company decided to hire more employees. For which they want to know the mean time required to complete the work for a worker.



The following table shows the frequency distribution of the time required for each worker to complete the work

Time(in hours)	15-19	20-24	25-29	30-34	35-39
Number of workers	10	15	12	8	5

Based on the above information answer the following

- i. Find mean time required to complete the work for a worker (in hrs)
- ii. If a worker works for 8 hours in a day, then the approximate time required to complete the work for a worker is (in days)

Case Study Question 5

Transport department of a city wants to buy some electric buses for the city for which they wants to analyse the distance travelled by existing public transport buses in a day





The following shows the distance travelled by 60 existing public transport buses in a day

Daily distance travelled(km)	200-209	210-219	220-229	230-239	240-249
No of buses	4	14	26	10	6

Based on the above information answer the following questions

- i. Find median of the distance travelled
- ii. If the mode of the distance travelled is 223.78 km, find the mean of the distance travelled by the bus

Case Study Question 6

A group of 71 people visited to a museum on a certain day. The following table shows their ages



Age in	Less than					
years	10	20	30	40	50	60
No. of	3	10	22	40	54	71
persons						

Based on the above information answer the following

- i. Find the median age of the persons visited the museum
- ii. If the price of the ticket for the age group 30-40 is ₹30 .then the total amount spent by this age group is

Case Study Question 7





An agency has decided to install customized playground equipment's at various colony parks. For that they decided to study the age group of children playing in a park of the particular colony The classification of children according to their ages, playing in a park is shown in the following table

Age group of child	ren (in 6	5-8	8-10	10-12	12-14	14-16	
years)							Based
Number of child	dren 4	43	58	70	42	27	on the
			•				ahovo

above

information answer the following

- i. In which age group, will the maximum number of children belong?
- ii. Find the mode of the ages of children playing in the park



ANSWER KEY

Answer key (1 mark questions)
1. (n+1)/2
2. 3Median=Mode +2Mean
3.4
4.2
5.4
6.9
7.27
8.0
9. 25
10.46
11. Median of 2, 3, 5, 7, 11, 13, 17, 19, 23 = 11
12. Mode= $3x15 - 2x14 = 17$
13. Lower limit of 20-30 is 20.
14. Mean= a+ h x $(\Sigma fiui)/(\Sigma fi) = 27$
15. Frequency= $51-48=3$
16. Mode-Median=24
Mode=24+Median
3Median-2Mean=Mode
3Median-2Mean=24+Median
3Median-Median=24+2Mean
Median-Mean=24/2=12
17. $(7+8+x+11+14)/5 = x$; $x=10$
$\frac{1}{18} \frac{(7+6+x+11+1)}{(6+7+x+8+y+14)} = \frac{1}{6} = \frac{1}{6} ; x+y=19$
19. Mean = $(1+3+5+\dots+(2n-1))/n = n$
20. Class mark= $\frac{1}{2}(10+25) = 17.5$
20. Clubb murk= 72(10+20) =17.0

(
Answer key (2 m	arks)		
1) Mode-3.28			
2) lower limit of median class-			
99.50			
3) p=6			
4) Mean-25.2			
5) x=12			
6) Median-44 runs			
7) Mode- 42.77			
8) Mean=43			
9) Mean=8.15			
10) n=29			
11. Marks	number		
0-20	17		
20-40	5		
40-60	7		
60-80	8		
80-100	13		
12. Mean= 50.10			
Median=52			
13. Mode exceeds m	ean by 9		
14. Mean=25	-		
15. x=13 , y=61			
16. Median=23.33			
17. Mean=52			
18. Less than 300	12		
Less than 400	30		
Less than 500	65		
Less than 600	85		
Less than 700	100		
19. More than 0	100		
More than 10	95		
More than 20	80		
More than 30	60		
More than 40	37		
More than 50	20		
More than 60	20 9		
	2		
20. Modal Class $= 30$	0-40		

ANSWER KEY (3 MARKS)

1)
T)

Life time (in	No. of lamps (f)	Cumulative frequency
hours)		
1500-2000	14	14
2000-2500	56	70
2500-3000	60	130
3000-3500	86	216

MATHEMATICS / X / 2022 – 23



3500-4000	74	290
4000-4500	62	352
4500-5000	48	400

$$n=\sum f=400, \frac{n}{2}=200, \text{ median class } 3000-3500$$

l=3000, c=130, h=500, f=86

$$M = 1 + \frac{\frac{n}{2} - c}{f} * h = 3000 + \frac{200 - 130}{86} * 500 = 3406.98$$

2)

CI	Fi	xi	$\text{Ui} = \frac{xi-a}{h}$	fiui
20-30	8	25	-2	-16
30-40	6	35	-1	-6
40-50	Х	45=a	0	0
50-60	11	55	1	11
60-70	у	65	2	2y
Total	$\sum_{\substack{i=25+x\\i=y}}^{fi}$			$\sum_{i=2y}^{i=2y} fiui$
Maan	∑fiui _{*h}		A.1.c.o.	

Mean= $a + \frac{\sum f u}{\sum f i} *h$

Also

 $\sum fi=25 + x + y = 50$

$$48=45+\frac{2y-11}{50}*10$$
, y=13

x+y=25, x=12

3)

CI	Frequency	Midpoint (x)	Cu.freq
0-6	4	3	4
6-12	Х	9	4+x
12-18	5	15	9+x
18-24	Y	21	9+x+y
24-30	1	27	10+x+y
Total	20		
$\sum f=20$			

x+y=10, median is 14.4.So median class is 12-18

$$M = 1 + \frac{\frac{n}{2} - c}{f} * h \qquad 14.4 = 12 + \frac{\frac{20}{2} - (4 + x)}{5} * 6 , \quad x = 4 \text{ and } y = 6$$

CI	Frequency	Class mark (xi)	fixi
10-20	4	15	60
20-30	8	25	200
30-40	10	35	350
40-50	12	45	54



50-60	10	55	550
60-70	4	65	260
70-80	2	75	150
	$\sum f=50$		$\sum fixi=2110$
			-
$\Sigma fixi = 2110$ (2.2)			

Mean= $\frac{\sum f(x)}{\sum f(x)} = \frac{2110}{50} = 42.2$

12 is the maximum frequency.so 40-50 is the modal class.

Mode =
$$l + \frac{f - f1}{2f - f1 - f2} * h = l + \frac{12 - 10}{2(12) - 10 - 10} * 10 = 45$$

Empirical formula

3 Median= Mode + 2 Mean

Median= $\frac{Mode+2 mean}{3} = \frac{45+2*42.2}{3} = 99.4$

5) n=100, 76+x+y=100, x+y=24, given median is 525. Median class 500-600

I=500, h=100, f=20, cf=36+x,
$$M = 1 + \frac{\frac{n}{2} - c}{f} * h$$
 525= 500+ $\frac{50 - (36 + x)}{20} * 100$

Simplifying we get x=9 and y=15

- 6) $\sum fi = 40$ Mean = 165+($\frac{5}{40}$ x 6)=165.75
- 7) Median= $12 + \frac{5X6}{9} = 15.3$

8) Mode=
$$10 + \frac{12-8}{24-8-10} \times 10 = 10 + 6.6666 = 16.67$$

9)
$$150+p+q = 230$$

p+q=80(1)

On applying formulae for median p=34 q=46

10)
$$18.75 = \frac{460+7p}{32}$$

p=20

class	frequency	Xi	di =	fidi
			$\frac{xi-50}{20}$	
0-20	15	10	-2	-30
20-40	22	30	-1	-22
40-60	37	50	0	0
60-80	25	70	1	25
80-100	21	90	2	42



∑fi=120		∑fidi=15
$Mean = A + \frac{\sum fidi}{\sum fi} x h =$	$50 + \frac{15}{120}x$	20 =50+2.5 =52.5

12)

POCKET	NO OF	xi	di = $\frac{xi - 162.5}{xi - 162.5}$	fidi
MONEY	STUDENTS		25	
	fi			
100-125	14	112.5	-2	-28
125-150	8	137.5	-1	-8
150-175	12	A =	0	0
		162.5		
175-200	5	187.5	1	5
200-225	11	212.5	2	22
	$\sum fi=50$			∑fidi=-
				9
	∑fidi 1 1 co 5	9		- 150

Mean= A + $\frac{\Sigma \text{fidi}}{\Sigma \text{fi}}$ x h = 162.5 + $\frac{-9}{50}$ x 25 = 162.5 - 4.5 = 158

13)

CLASS	FREQUENCY	xi	$di = \frac{xi-55}{xi-55}$	fidi
INTERVAL			10	
10-20	8	15	-4	-32
20-30	7	25	-3	-21
30-40	12	35	-2	-24
40-50	23	45	-1	-23
50-60	11	55	0	0
60-70	13	65	1	13
70-80	8	75	2	16
80-90	6	85	3	18
90-100	12	95	4	48
	$\sum fi = 100$			∑fidi
				= -5

Mean= A +
$$\frac{\Sigma \text{fid}}{\Sigma \text{fi}}$$
 x h = 55+($\frac{-5}{100}$ x10) = 55-0.5 = 54.5

14)

HEIGHTS (CM)	NUMBER OF STUDENTS
150-155	15
155-160	8 f_0
160-165	20 f ₁
165-170	12 f ₂
170-175	5

Model class 160-165

Mode = l+
$$\left(\frac{f_1-f_0}{2f_1-f_0-f_2}\right)xh = 160 + \frac{20-8}{40-8-12}x5 = 160 + \frac{12}{20}x5 = 160 + 3 = 163$$



MONEY SAVED IN RUPEES	NO OF STUDENTS	Cf
5-7	6	6
7-9	3	9 cf
9-11	9 f	18
11-13	5	23
13-15	7	30
	N	

N=30
$$\frac{N}{2}$$
= 15, Median = l + $\frac{\frac{N}{2}-cf}{f}$ x h = 9 + $\frac{15-9}{9}$ x 2 = 9 + $\frac{6}{9}$ x2= 9 + 1.33=10.33

ANSWER KEY (4 MARKS)

1) mode = 55, modal class 45-60, l=45, h=15, fo=15, f1=x, f2=10

 $55 = 45 + \frac{15 - x}{30 - x - 10} * 15$ we get x=5

2) median= 28.5 n=60, median class 20-30, l=20, h=10, f=20, cf=5+x

 $28.5 = 20 + \frac{30 - (5 + x)}{20} * 10$ x=8, also x+y+45=60, y=7

3)

Daily wages	No.of	xi	xi-A	$ui = \frac{xi - 170}{20}$	fiui
	workersfi)			20	
100-120	10	110	-60	-3	-30
120-140	15	130	-40	-2	-30
140-160	20	150	-20	-1	-20
160-180	22	170	0	0	0
180-200	18	190	20	1	18
200-220	12	210	40	2	24
220-240	13	230	60	3	39
Σ fini	$\sum f=110$				$\sum fiui=1$

Mean= $a + \frac{\sum fiui}{\sum fi} *h$ Mean=170+ $\frac{1}{110} *20 = 170.18$, mean daily wages=170.18

Modal class 160-180, f=22, l=160, h=20, f1=20, f2=18

Mode = $160 + \frac{22-20}{44-20-18} * 20 = 166.67$, modal daily wages = 166.67

4)
$$53+f1+f2=100$$

 $f_1 + f_2 = 47....(A)$

mean=53

 $\frac{2730+30f1+70f2}{100} = 53....(B)$

Solving A and B f1=18, f2=29



Length (in mm)	Class Interval (inclusive)	Number of leaves	Cumulative Frequency
118 126	117.5 - 126.5	3	3
127 135	126.5 - 135.5	5	3 + 5=8
136 144	135.5 - 144.5	9	8 + 9=17(F)
145 - 153	144.5 - 153.5	12(f)	17 + 12=29
154 162	153.5 - 162.5	5	29 + 5=34
163 - 171	162.5 - 171.5	4	34 + 4=38
172	171.5 - 180.5	2	38 + 2=40

n = 40, n/2 = 20

median class is 144.5-153.5 , l= 144.5 ,cf= 17 , f= 12, h = 9

Using the formula, = 144.5 + 2.25 = 146.75

6) Mode = 240

 $240=200+(\frac{270-230}{2X270-230-x}) \times 100$ Solving x =210

7) Median =
$$125 + \frac{34-22}{20} \times 20 = 137$$
 Mode = $125 + \frac{20-13}{2x20-13-14} \times 20 = 135.7$

Mean=137.7 (2 mean=3median-mode)

the medi	an of the fol	lowing data is 3	1	median = 31
class	frequency	Cf		$1 + \frac{\frac{N}{2} - cf}{f} \mathbf{x} \mathbf{h} = 31$
0-10	5	5		
10-20	Х	5 + x		$30 + \frac{20 - (11 + x)}{x} \times 10 = 31$
20-30	6	11 +x		v
30-40	Y	11 +x +y		$\frac{20-(11+x)}{y}$ x10 = 31-30
40-50	6	17 +x +y		$\frac{20-11-x}{y}$ x10 =1
50-60	5	22 + x + y		-
total	40			10(9-x) = y
	0-22	= 40		90-10x =y Sub in x+y =18 x + 90-10x =18 90-9x =18 90-18 =9x 72 = 9x $X = \frac{72}{9}$
				X = 8



Y = 90 - 10 x = 90 -(10x8) = 90 - 80
= 10

Class	frequency
0-20	8
20-40	11
40-60	X f _o
60-80	12 f ₁
80-100	Y f ₂
100-120	9
120-140	9
140-160	5

	1
Sum of all frequencies $=70$	
8+11+x+12+y+9+9+5=70	
54 + x + y = 70	
x + y = 70-54	
$\mathbf{x} + \mathbf{y} = 16$	
Mode = $l + (\frac{f_1 - f_0}{2f_1 - f_0 - f_2} xh)$	$\mathbf{Y} = \mathbf{3x} \cdot 24$
$65 = 60 + \frac{12-x}{24-x-y} \times 20$	Sub in x+y =16
$65-60 = \frac{12-x}{24-x-y} \times 20$	x + 3x - 24 = 16 4x = 16 + 24
5 $=\frac{12-x}{24-x-y}x$ 20	4x = 40
$\frac{5}{12-x} = \frac{12-x}{12-x}$	$X = \frac{40}{4} = 10$
$\frac{5}{20} = \frac{12-x}{24-x-y}$	4
	Y =(3x10)-24
$\frac{1}{4} = \frac{12-x}{24-x-y}$	= 30-24
1(24-x-y) = 4(12-x)	=6
24 - x - y = 48 - 4x	
24-48 = -4x + x + y	
24-48 =y-3x	
-24 = y - 3x	
10)	

1	\mathbf{U}	
T	U)	

Class	frequency	
25-35	7	
35-45	31 f _o	
45-55	33 f ₁	
55-65	17 f ₂	
65-75	11	
75-85	1	
Mode = $l + (\frac{f_1 - f_0}{2f_1 - f_0 - f_2} xh)$		

Mode =
$$l + (\frac{f^2 + f^2}{2f 1 - f 0 - f 2} xh)$$



$$= 45 + \frac{33-31}{66-31-17} \times 10$$
$$= 45 + \frac{2}{18} \times 10$$
$$= 45 + \frac{10}{9}$$
$$= 45 + 1.11$$
$$= 46.11$$

PROBABILITY

Probability is the study of the chances of events happening. By means of probability, the chance of the events is measured by a number lying from 0 to 1.

Experiment: An operation which produces some well-defined outcomes, is called an experiment. Eg. Tossing a coin, throwing a dice etc.

If an experiment is repeated under identical conditions and they do not produce the same outcomes every time, then it is said to be a **Random experiment**.

An event of an experiment is the collection of some outcomes of the experiment, generally denoted by E. Eg. Getting an odd number in a single throw of die is an event. This case there are three outcomes 1,3 and 5

Elementary event: An event having only one outcome of the random experiment is called an elementary event. Eg. Tossing a coin and getting H or T is an elementary event

Probability of an event : If E is an event associated with a random experiment , then probability of event E, denoted by P(E) represents the chance of occurrence of event E.

Eg. If E denotes the event of getting an odd number in a single throw of die, then P(E) represents the chance of occurrence of event E, i.e, the chance of getting 1,3 or 5

Compound event: The collection of two or more elementary events associated with an experiment is called a compound event. Eg. In the random experiment of tossing a die, if we define the event "getting a multiple of 3". Then the event has two outcomes 3 and 6 and hence is a compound event.

Impossible event: An event which does not occur at all when an experiment is performed is called an impossible event. Eg. "Event of getting 7 on a die" when a die is tossed, is an impossible event.

Sure event: The event which always occurs when the experiment is carried out is called a sure event. Eg. If we toss a die, the total outcomes are 1,2,3,4,5,6. Let the event be "the number on the die is less than 7" then E is 1,2,3,4,5,6 and hence always occurs and is a sure event.

Equally likely outcomes: Two or more outcomes are said to be equally likely outcomes if each outcome has the same chance of appearing as any other. Eg. If we



toss a coin, the two outcomes i.e, H or T are equally likely to appear, so they are equally likely outcomes.

Formula for finding probability: The probability of an event E is denoted by P(E) and is

defined as

$$P(E) = \frac{Number of outcomes favourable to event E}{Total number of all possible outcomes of the experiment}$$

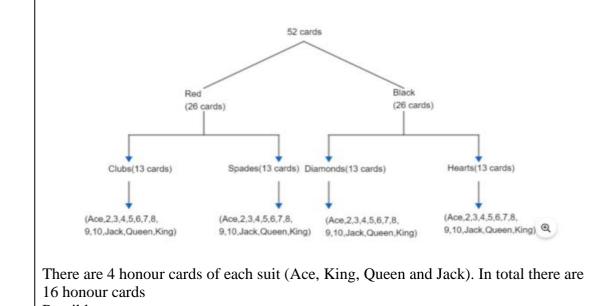
The numerator in the definition of P(E) is always less than or equal to denominator of P(E)

- $0 \le P(E) \le 1$
- For an impossible event P(E) = 0
- For sure event P(E) = 1
- Probability of an event cannot be negative
- The sum of probabilities of all the elementary events of an experiment = 1

Complement of an event / Negation of an event: If E is an event associated with a random experiment, then if we delete the outcomes in event E from total outcomes, then the event of collection of remaining outcomes is called complement event of 'event E' and is denoted by \overline{E}

- E and \overline{E} are complementary events
- $P(E) + P(\bar{E}) = 1$

A pack of (or deck) of playing cards consists of four suits called Diamonds, Hearts, clubs and Spades. Each suit consists of 13 cards totaling 52 in all -26 of red colour and 26 of black colour. Diamonds and Hearts are red cards whereas Clubs and Spades are black cards. Each suit contains an Ace, King, Queen and Jack ,2 3 , 4, 5, 6, 7 ,8, 9and,10. The Kings, Queens and Jacks are called face cards (there are 3 face cards in each suit). Thus, there are 12 face cards in all in a pack. Nine cards of each suit are numbered from 2 to 10.



Possible outcomes



	Tossing a coin Head , Tail
	Tossing two coins(HH) (HT) (TT) (TH)
	Tossing 3 coins(HHH) (HHT) (HTH) HTT) (TTH) (TTT) (THT) (THT) Throwing a die1, 2, 3, 4, 5, 6
	Throwing two dices(1,1) $(1,2)(1,3)(1,4)(1,5)(1,6)$
	(2,1) (2,2) (2,3) (2,4) (2,5) (2,6)
	(3,1) (3,2) (3,3) (3,4) (3,5) (3,6)
	(4,1) $(4,2)$ $(4,3)$ $(4,4)$ $(4,5)$ $(4,6)$
	$\begin{array}{c} (5,1) & (5,2) & (5,3) & (5,4) & (5,5) & (5,6) \\ (6,1) & (6,2) & (6,3) & (6,4) & (6,5) & (6,6) \end{array}$
	(0,1) $(0,2)$ $(0,3)$ $(0,4)$ $(0,3)$ $(0,0)$
	Leap year 53 days (Sunday, Monday) (Monday, Tuesday)
	(Tuesday, Wednesday) (Wednesday, Thursday) (Thursday, Friday)
	(Friday, Saturday) (Saturday, Sunday)
	Non leap yearSunday, Monday, Tuesday, Wednesday, Thursday, Friday, Saturday
	PART A (1 MARK QUESTIONS)
1	The probability that a number selected from the numbers { 1,2,3,4,20 } is a multiple
	of 5 is
	(1, 5,, 1,, 2, 4,, 2)
	(A) $\frac{5}{20}$ (B) $\frac{1}{5}$ (C) $\frac{4}{5}$ (D) $\frac{2}{5}$
2	A letter of English alphabet is chosen at random. The probability that the chosen letter
	is a consonant is
	$(1)^{21}$ (2) 5 (3) 2 (3) 1
	(A) $\frac{21}{26}$ (B) $\frac{5}{26}$ (C) $\frac{2}{25}$ (D) None of these
3	Which of the following cannot be the probability of an event?
	(A) 1.5 (B) $\frac{3}{5}$ (C) 25% (D) 0.3
4	If $P(E) = 0.05$, then the probability of P (not E) is
	(A) 0.85 (B) 0.75 (C) 0.25 (D) 0.95
5	In a single throw of a die, the probability of getting a multiple of 3 is
	$(A)\frac{1}{2}$ $(B)\frac{1}{3}$ $(C)\frac{1}{6}$ $(D)\frac{2}{3}$
6	A bag contains three green marbles, four blue marbles & two orange marbles. One
	marble is picked at random, then the probability that it is not an orange marble is
	$(A)\frac{1}{4}$ $(B)\frac{1}{3}$ $(C)\frac{4}{9}$ $(D)\frac{7}{9}$
7	The probability of getting a bad egg in a lot of 400 eggs is 0.035. The number of bad
	eggs in the lot is
	(A)7 (B)14 (C)21 (D)28
8	Two coins are tossed simultaneously, then the probability of getting exactly one head
	is



	(A) $\frac{1}{3}$ (B) $\frac{2}{6}$ (C) $\frac{1}{2}$ (D) $\frac{1}{8}$
9	A card is drawn at random from a well shuffled pack of 52 cards. The probability that the drawn card is not an ace is
	$(A)\frac{1}{13}$ $(B)\frac{12}{13}$ $(C)\frac{9}{13}$ $(D)\frac{4}{13}$
10	The probability that a non – leap year has 53 Sundays is
	$(A)\frac{2}{7}$ $(B)\frac{5}{7}$ $(C)\frac{6}{7}$ $(D)\frac{1}{7}$
11	The Probability of guessing the right answer to a certain question in a test is $\frac{x}{12}$. If the
	probability of not guessing the correct answer to this question is $\frac{2}{3}$, then find value of x
12	Two coins are tossed simultaneously. Find the probability of getting at most one head
13	A die is thrown twice. Find the probability of getting a sum less than 8
14	A card is drawn from a pack of 52 cards. Find the probability that the card drawn is not a face card
15	A number is selected from first 50 natural numbers. What is the probability that it is a multiple of 3 or 5?
16	A card is drawn from a pack of 52 cards. Find the probability of getting a king of red colour
17	A box contains cards numbered 6 to 50. A card is drawn at random from the box. Find the probability that the card drawn has a number which is a perfect square
18	A bag contains 40 balls out of which some are red, some are blue and remaining are black. If the probability of drawing a red ball is $\frac{11}{20}$ and that of blue ball is $\frac{1}{5}$, then what is the no. of black balls?
19	A bag contains cards which are numbered from 2 to 90. A card is drawn at random from the bag. Find the probability that it bears a two digit number
20	A bag contains cards numbered from 1 to 49. After mixing the cards thoroughly a card is drawn from the bag at random, Find the probability that the number on the drawn card is an odd number
21	A card is drawn from a well shuffled deck of cards. What is the probability that the card drawn is neither a king nor a queen?
22	The probability of selecting a rotten apple randomly from a heap of 900 apples is 0.18. What is the number of rotten apples in the heap.
23	A month is selected at random in a year. Find the probability that it is March or October.
	PART B (2 MARK QUESTIONS)



24	A coin & a die are tossed simultaneously. Find the probability that a tail & a prime number turns up
25	A letter is chosen at random from the letters of the word "ASSASSINATION", then
	the probability that the letter chosen is a vowel is in the form of $\frac{6}{2x+1}$, if so find the
	value of x $2x+1$
26	In a family of 3 children calculate the probability of having at least one boy.
	A letter of English alphabet is chosen at random. Determine the probability that the
27	chosen letter is a vowel
28	A coin is tossed two times. Find the probability of getting both heads or both tails
29	A box contains cards bearing numbers 6 to 70. If one card is drawn at random from
	the box ,find the probability that it bears
	(i) a one digit number
20	(ii) a number divisible by 5.A box contains 20 cards numbered from 1 to 20. A card drawn at random from the
30	box. Find the probability that the card drawn at random is divisible by 2 or 3
31	From a bag containing 5 red, 8 black and 7 blue balls, a ball selected at random .Find
01	the probability that
	(i) it is not a red ball
	(ii) it is a blue ball
32	Two different dice are tossed together. Find the probability
	(i)of getting a doublet
	(ii) of getting a sum 10, on the two dice.
33	Two dices are rolled once. Find the probability of getting such numbers on the two
34	dice, whose product is 12 All cards of ace , jack and queen are removed from a deck of playing cards. One card
54	is drawn at random from the remaining cards. Find the probability that the card drawn
	is
	(i) a face card
	(ii) a black king
27	
35	A number is selected at random from the numbers 3,5,5,7,7,7,9,9,9,9,9,. Find
36	the probability that the selected number is their average. A number x is selected at random from the numbers 1, 4, 9, 16 and another number
30	y is selected at random from numbers 1, 2, 3 4. Find the probability that the value of
	xy is more than 16
37	A group consists of 12 persons, out of which 4 are extremely patient, other 6 are
	extremely honest and rest are extremely kind. A person from the group is selected at
	random. Assuming that each person is equally likely to be selected, find the
	probability of selecting a person who is
	(i)extremely patient.
20	(ii) extremely kind or honest.
38	A card is drawn from a well – shuffled pack of 52 cards. Find the probability that the card drawn is neither a red card nor a queen
39	A card is drawn from a well – shuffled pack of 52 cards. Find the probability that the
57	card drawn is either a red card or a queen
40	A card is drawn from a well – shuffled pack of 52 cards. Find the probability of
	getting
	(i) a red king



	(ii) a queen or jack
41	A square of side 5 cm is drawn in the interior of another square of side 10 cm and
	shade as shown in the figure. A point is selected at random from the interior of square.
	What is the probability that the point will be chosen from the shaded part?
42	A bag contains 2 green, 3 red and 4 black balls. A ball is taken out of the bag at
	random. Find the probability that the selected ball is
	(i) not green
	(ii) not black
43	12 defective pens are accidentally mixed with 132 good ones. It is not possible to just
	look at a pen and tell whether or not it is defective. One pen is taken out at random
	from the lot .Determine the probability that the pen taken out is a good one
44	Two players, Sangeeta and Reshma, play a tennis match. It is known that the
	probability of Sangeeta's winning the match is 0.62. What is the probability of
	Reshma's winning the match?
	PART C - (3 MARK QUESTIONS)
45	A child has a die whose six faces show the letters as given below:
	A B C D E A
	The die is thrown once. What is the probability of getting
	(i) A
	(i) D?
	(III) Vowels:
46	Out of 400 bulbs in a box, 15 bulbs are defective. One bulb is taken out at random
	from the box. Find the probability that the drawn bulb is not defective.
47	A bag contains 15 white and some black balls. If the probability of drawing a black
	ball from the bag is thrice that of drawing a white ball, find the number of black balls
	in the bag.
10	
48	A bag contains 12 balls out of which x are white. (i) If one ball is drawn at random,
	what is the probability that it will be a white ball? (ii) If 6 more white balls are put in
10	the bag, the probability of drawing a white ball will be double that in case (i). Find x.
49	A pair of dice is thrown once. Find the probability of getting
	(i) doublet of prime numbers
50	(ii) a doublet of odd numbers.
50	All the three face cards of spades are removed from a well- shuffled pack of 52 cards.
	A card is drawn at random from the remaining pack. Find the probability of getting
	(i) a black face cards
	(ii) a queen
51	(iii) a black card A hey contains cards bearing numbers 6 to 70. If one card is drawn at rendom from
51	A box contains cards bearing numbers 6 to 70. If one card is drawn at random from the box find the probability that it bears
	the box, find the probability that it bears
	(a) not a one digit number(b) a number not divisible by 5
	(c) number is a perfect square



52	There are 100 cards in a bag on which numbers from 1 to 100 are written. A card is taken out from the bag at random. Find the probability that the number on the selected
	card I. is divisible by 9 and is a perfect square
	II. (ii) is a prime number greater than 80
53	A bag contains 24 balls of which x are red 2x are white and 3x are blue. A ball is
	selected at random. What is the probability that
	(i) it is red
	(ii) it is blue
51	(iii) neither red nor blue
54	A bag contains white, black and red balls only. A ball is drawn at random from the
	bag. The probability of getting a white ball is $\frac{3}{10}$ and that of black is $\frac{2}{5}$. Find the
	probability of getting a red ball. If the bag contains 20 black balls, then find the total number of balls in the bag.
55	A child's game has 6 triangles of which 3 are blue and rest are red and 10 squares of
	which 6 are blue and rest are red. One piece Is lost at random. Find the probability that
	that it is a
	(i) Triangle
	(ii) Square (iii) Square of blue colour
56	(iii) Square of blue colour A lot consists of 48 mobile phones of which 42 are good, 3 have only minor defects
50	and 3 have major defects. Varnika will buy a phone if it is good but the trader will
	only buy a mobile if it has no major defect. One phone is selected at random from the
	lot. What is the probability that it is:
	(i) acceptable to. Varnika?
	(ii) acceptable to the trader?
57	Five cards – the ten, jack, queen, king and ace of diamonds, are well-shuffled with
	their face downwards. One card is then picked up at random.
	(i) What is the probability that the card is the queen?
	(ii) If the queen is drawn and put aside, what is the probability that the second card
50	picked up is (a) an ace? (b) a queen?
58	A bag contains 5 black, 7 red and 3 white balls. A ball is drawn from the bag at random. Find the probability that the ball drawn is:
	(i) red.
	(ii) black or white.
	(iii) not black.
59	The probability of selecting a blue marble at random from a jar that contains only
	blue, black and green marbles is 1/5. The probability of selecting a black marble at
	random from the same jar is 1/4. If the jar contains 11 green marbles, find the total
	number of marbles in the jar.
	SECTION D (4 MARK QUESTIONS)
60	All the black Ace cards are removed from a pack of 52 playing cards. The remaining cards are
	well shuffled and then a card is drawn at random. Find the probability of getting
	i) a Ace card ii) a red card iii) a black card iv) a Jack
61	. Cards marked with the number 2 to 101 are placed in a box and mixed thoroughly. One card
	· · ·
	is drawn from the box. Find the probability that the number on the card is:



	(i) An even number (ii) A number less than 14 (iii) A number is perfect square (iv) A prime number less than 20
62	Out of the families having three children, a family is chosen random. Find the probability that the family has (i) Exactly one girl (ii) At least one girl (iii) At most one girl
63	The Ace, number 10 and jack of clubs are removed from a deck of 52 playing cards and remaining cards are shuffled. A card is drawn from the remaining cards. Find the probability of getting a card of (a) heart (b) Ace (c) clubs (d) either 10 or jack
64	Two dice are thrown simultaneously. What is the probability that: (a) 5 will not come up either of them? (b) 5 will come up on at least one time? (c) 5 will come at both dice? (d) Sum of 5 comes on both the dice together
65	Cards bearing numbers 3, 5 35 are kept in a bag. A card is drawn at random from the bag. Find the probability of getting a card bearing (a) a prime number less than 15 (b) a number divisible by 3 and 5
66	A bag contains 8 red balls & some blue balls. If the probability of drawing a blue ball is 3 times of a red ball, find the number of blue balls in the bag.
67	Three coins are tossed simultaneously. Find the probability of getting (i) Exactly 2 heads (ii) at least 1 head (iii) at most 2 tails (iv) exactly 3 heads
	Case study questions
68	
	Akshith & Dikshith are good friends. During vacation Dikshith went to Akshith's house to play Ludo.They played Ludo with 2 dice.(i)To win a game Dikshith needs a total of 7. What is the probability of winning game by Dikshith ?(ii) Find the probability that 5 will come up atleast in one die?
69	CASE STUDY 2



	 Two friends Neha and Sohan have some savings in their piggy bank. They decided to count the total coins they both had. After counting they find that they have fifty ₹ 1 coins, forty eight ₹ 2 coins, thirty six ₹ 5 coins, twenty eight ₹10 coins and eight ₹ 20 coins. Now, they said to Isha, their another friends, to choose a coin randomly (i) Find the probability of getting a denomination of ₹10 (ii) Find the probability of getting a denomination of ₹ 2 or ₹ 5
70	CASE STUDY 3 Fric bought balls for decorating Christmas tree. The bag contains 24 balls ,of which x number are red balls (i) If one ball is drawn at random, find the probability of getting a red ball
	(ii) If 6 more red balls are put in the bag ,the probability of drawing a red ball is double that in first case , find the number of red balls
71	CASE STUDY 4 Gunjan is fond of playing cards. She tries to find out probability in different situations. One such situation is given below Five cards – ten, jack, queen, king, and an ace of diamonds are shuffled face downwards. One card is picked at random. (i) What is the probability that the card is a queen? (ii) If a king is drawn first and put aside, what is the probability that the second card picked up is the (a) ace? (b) king?
72	CASE STUDY 5 BRIDGE GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD GARD



(ii) Find the probability that a card drawn is with a number less than 8
 73 CASE STUDY 6
 Find the probability of getting no heads

Find the probability of getting one tail;

ANSWER KEY

II.

Q NO	ANSWER	Q NO	ANSWER	Q NO	ANSWER
1	$\frac{1}{5}$	20	$\frac{25}{49}$	39	$\frac{7}{13}$
2	21	21	11	40	$\frac{13}{\frac{1}{26}},$ (ii) $\frac{2}{13}$
3	26 1.5	22	13 162	41	$\frac{1}{4}$
4	0.95	23	$\frac{1}{6}$	42	$\frac{7}{9}, \frac{5}{9}$
5	$\frac{1}{3}$	24	$\frac{1}{4}$	43	$\frac{11}{12}$
6	$ \frac{1}{3} \\ \frac{7}{9} $	25		44	0.38
7	14	26	$\frac{7}{8}$	45	$\frac{1}{3}, \frac{1}{6}, \frac{1}{2}$
8	$\frac{1}{2}$	27	5 26	46	$\frac{77}{80}$
9	12 13	28	$\frac{1}{2}$	47	45
10	$\frac{1}{7}$	29	$\frac{4}{65}$, (ii) $\frac{1}{5}$	48	$\frac{1}{4}$,3
11	4	30	$\frac{13}{20}$	49	$\frac{1}{12}, \frac{1}{12}$
12	$\frac{3}{4}$	31	$\frac{3}{4}$, (ii) $\frac{7}{20}$	50	$\frac{3}{49}, \frac{3}{49}, \frac{23}{49}$
13	$\frac{7}{12}$	32	$\frac{1}{6}$, (ii) $\frac{1}{12}$	51	$\frac{61}{65}, \frac{52}{65}, \frac{6}{65}$



14	$\frac{10}{13}$	33	$\frac{1}{9}$	52	$\frac{3}{100}, \frac{3}{100}$
15	$\frac{23}{50}$	34	$\frac{1}{10}$ (ii) $\frac{1}{20}$	53	$\frac{1}{6}, \frac{1}{2}, \frac{2}{3}$
16	$\frac{1}{26}$	35	$\frac{3}{10}$	54	$\frac{3}{10}$, 50
17	$\frac{1}{9}$	36	$\frac{3}{8}$	55	$\frac{3}{8}, \frac{5}{8}, \frac{3}{8}$
18	10	37	$\frac{1}{3}$, (ii) $\frac{2}{3}$	56	$\frac{7}{8}, \frac{15}{16}$
19	81 89	38	$\frac{6}{13}$	57	$\frac{1}{5}, \frac{1}{4}, 0$
58	$\frac{7}{15}, \frac{8}{15}, \frac{2}{3}$	64	$\frac{25}{36}, \frac{11}{36}, \frac{1}{36}, \frac{1}{9}$	70	$\frac{1}{6}$, 4
59	20	65	$\frac{5}{17}, \frac{2}{17}$	71	$\frac{3}{47}, \frac{3}{46}, \frac{3}{46}$
60	$\frac{1}{25}$, $\frac{13}{25}$, $\frac{12}{25}$, $\frac{2}{25}$	66	24	72	$\frac{2}{13}, \frac{6}{13}$
61	$\frac{1}{2}, \frac{3}{25}, \frac{9}{100}, \frac{2}{25}$	67	$\frac{3}{8}, \frac{7}{8}, \frac{7}{8}, \frac{1}{8}$	73	$\frac{1}{8}, \frac{3}{8}$
62	$\frac{3}{8}, \frac{7}{8}, \frac{1}{2}$	68	$\frac{1}{6}, \frac{11}{36}$		
63	$\frac{13}{49}$, $\frac{3}{49}$, $\frac{10}{49}$, $\frac{6}{49}$	69	$\frac{14}{85}, \frac{42}{85}$		



CBSE SAMPLE QUESTION PAPER 2022-23



SECTION A

Class- X

Session- 2022-23

Subject- Mathematics (Standard)

Sample Question Paper

Time Allowed: 3 Hrs.

Maximum Marks : 80

General Instructions:

- 1. This Question Paper has 5 Sections A-E.
- 2. Section A has 20 MCQs carrying 1 mark each
- 3. Section **B** has 5 questions carrying 02 marks each.
- 4. Section C has 6 questions carrying 03 marks each.
- 5. Section **D** has 4 questions carrying 05 marks each.
- 6. Section **E** has 3 case based integrated units of assessment (04 marks each) with sub-parts of the values of 1, 1 and 2 marks each respectively.
- All Questions are compulsory. However, an internal choice in 2 Qs of 5 marks, 2 Qsof 3 marks and 2 Questions of 2 marks has been provided. An internal choice has been provided in the 2marks questions of Section E
- 8. Draw neat figures wherever required. Take $\pi = 22/7$ wherever required if not stated.

Section A consists of 20 questions of 1 mark each.

S.NO				MA RK S
1	-	 s such that $a = p^3q^4$ and and LCM(a,b) = p ^r c (c) 35	nd $b = p^2 q^3$, where p and q are q^s , then $(m+n)(r+s)=$ (d) 72	1
2			its roots as factors of p is $x + p=0$ (d) $x^2 - px + p + 1=0$	1

MATHEMATICS / X / 2022 – 23



3	If α and β are the	e zeros of a polynomi	al f(x) = $px^2 - 2x +$	- 3p and $\alpha + \beta = \alpha \beta$,	then p is 1
	(a)-2/3	(b) 2/3	(c) 1/3	(d) -1/3	
4	If the system of (a) -1	equations $3x+y=1$ and (b) 0	d $(2k-1)x + (k-1)y =$ (c) 1	=2k+1 is inconsisten (d) 2	it, then $k = 1$
5	then the coordin	a parallelogram PQF ates of its fourth verte	ex S are		d R(-3,-2), 1
	(a) (-2,-1)	(b) (-2,-3)	(c) (2,-1)	(d) (1,2)	
6	$\Delta ABC \sim \Delta PQR. I$ $PQ^{2} = 4 : 9, \text{ ther}$	f AM and PN are alti AM: PN =	tudes of ∆ABC and	d ΔPQR respectively	and AB ² : 1
	(a) 3:2	(b) 16:81	(c) 4:9	(d) 2:3	
7		$60^{\circ} = \sin 60^{\circ} \cot 60^{\circ}, t$ $\cos 30^{\circ}$ (b) ta		sin30° (d) cot30°
8	If $\sin\theta + \cos\theta =$ (a) 1	$\sqrt{2}$, then $\tan\theta + \cot\theta$ (b) 2) = (c) 3	(d) 4	1
9	In the given figure which of the following B C	re DE II BC , AE= a owing is true?	units, EC = b units	DE = x units $BC = x$	y units,
	(a) x	$= \frac{a+b}{ay} $ (b) y	$= \frac{ax}{a+b}$ (c)	$x = \frac{ay}{a+b} \qquad (d)$	l) /y <u>=</u> a/b
10	1	zium with AD BC a her at O such that AC cm b) 7cm		0	BD 1

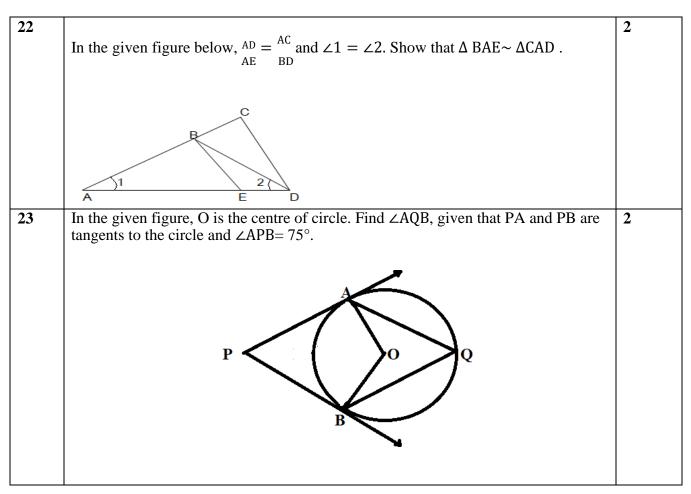


11	If two tangents inclined at an angle length of each tangent is equal to (a) $^{3\sqrt{3}}$ cm (b) 3cm (c) 6cm (d)		a circle of radiu	s 3cm, then the	1
12	The area of a circle that can be insa) 36 IIcm2b) 18IIcm2	ed in a square of c) 12∏cm2		cm2	1
13	The sum of the length, breadth an diagonal is $2\sqrt{3}$ cm. The total surf a) 48 cm2 b) 72 cm2			e length of its	1
14	The difference of mode and med- mean of the data is a) 8 b) 12 c) 24 d)	f a data is 24, the	en the difference	of median and	1
15	The number of revolutions made distance of 11 km is a) 2800 b) 4000 c) 5500	d) 7000	f radius 0.25m i	n rolling a	1
16	For the following distribution,	10.17			1
	Class 0-5 5-	10-15	15-20	20-25	_
	Frequency1015The sum of the lower limits of th		20 class is	9	-
17	a) 15b) 25c) 30Two dice are rolled simultaneous once?a) 1/6b) 7/36c) 11/2	d) 35 what is the probab d) 13/30		come up at least	1
18	If $5 \tan\beta = 4$, then $5 \sin\beta - 2\cos\beta = 5\sin\beta + 2\cos\beta$ a) $1/3$ b) $2/5$ c) $3/5$ c				1
19	DIRECTION: In the question nisfollowed by a statement of Rea Choose the correct optionStatement A (Assertion): If prod	(R).			1

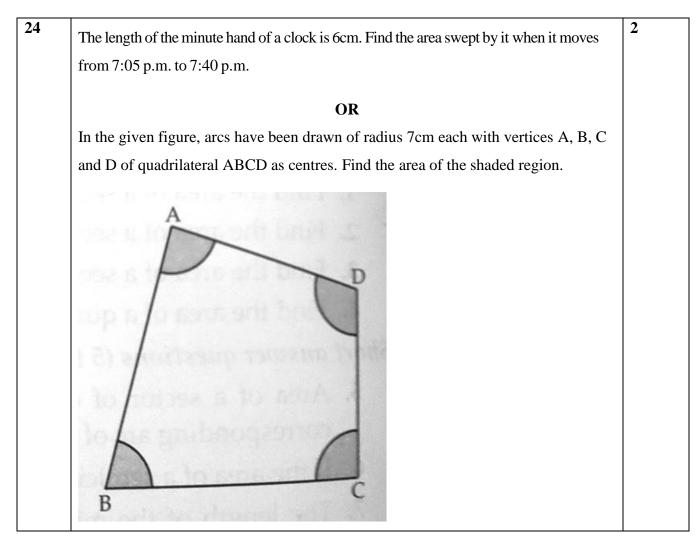


	thentheir LCM is 340	
	Statement R(Reason): HCF is always a factor of LCM	
	(a) Both assertion (A) and reason (R) are true and reason (R) is the correct explanation of assertion (A)	
	(b) Both assertion (A) and reason (R) are true and reason (R) is not the correct explanation of assertion (A)	
	(c) Assertion (A) is true but reason (R) is false.	
	Assertion (A) is false but reason (R) is true	
20	Statement A (Assertion): If the co-ordinates of the mid-points of the sides AB and ACof \triangle ABC are D(3,5) and E(-3,-3) respectively, then BC = 20 units	1
	<i>Statement R(Reason)</i> : The line joining the mid points of two sides of a triangle isparallel to the third side and equal to half of it.	
	(a) Both assertion (A) and reason (R) are true and reason (R) is the correct explanation of assertion (A)	
	(b) Both assertion (A) and reason (R) are true and reason (R) is not the correct explanation of assertion (A)	
	(c) Assertion (A) is true but reason(R) is false.	
	Assertion (A) is false but reason(R) is true.	
	SECTION B	
	Section B consists of 5 questions of 2 marks each.	
S.No.		Marks
21	If $49x+51y=499$, $51x+49y=501$, then find the value of x and y	2







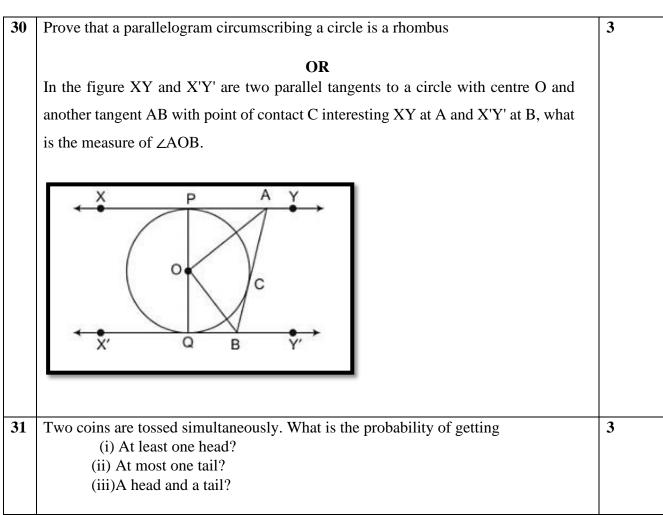


25	If $sin(A+B) = 1$ and $cos(A-B) = \sqrt{3/2}$, $0^{\circ} < A+B \le 90^{\circ}$ and $A > B$, then find the measures of angles A and B.	2
	OR Find an acute angle θ when $\cos\theta - \sin\theta = 1 - \sqrt{3}$ $\cos\theta + \sin\theta 1 + \sqrt{3}$	



	SECTION C	
	Section C consists of 6 questions of 3 marks each.	
S. No		Marks
26	Given that $\sqrt{3}$ is irrational, prove that $5 + 2\sqrt{3}$ is irrational.	3
27	If the zeroes of the polynomial $x^2 + px + q$ are double in value to the zeroes of the polynomial $2x^2 - 5x - 3$, then find the values of p and q.	3
28	A train covered a certain distance at a uniform speed. If the train would have been 6 km/h faster, it would have taken 4 hours less than the scheduled time. And, if the train were slower by 6 km/hr ; it would have taken 6 hours more than the scheduled time. Find the length of the journey.	3
	Anuj had some chocolates, and he divided them into two lots A and B. He sold the first lot at the rate of $\gtrless 2$ for 3 chocolates and the second lot at the rate of $\gtrless 1$ per chocolate, and got a total of $\gtrless 400$. If he had sold the first lot at the rate of $\gtrless 1$ per chocolate, and the second lot at the rate of $\gtrless 4$ for 5 chocolates, his total collection would have been $\gtrless 460$. Find the total number of chocolates he had.	
29	Prove the following that- $\frac{\tan^{3}\theta}{1+\tan^{2}\theta} + \frac{\cot^{3}\theta}{1+\cot^{2}\theta} = \sec\theta \csc\theta - 2\sin\theta \cos\theta$	3







	SECTION D	
	Section D consists of 4 questions of 5 marks each.	
S. No		Marks
32	To fill a swimming pool two pipes are used. If the pipe of larger diameter	5
	used for 4 hours and the pipe of smaller diameter for 9 hours, only half of	
	the pool can be filled. Find, how long it would take for each pipe to fill	
	the pool separately, if the pipe of smaller diameter takes 10 hours more	
	than the pipe of larger diameter to fill the pool?	
	OR	
	In a flight of 600km, an aircraft was slowed down due to bad weather. Its	
	average speed for the trip was reduced by 200 km/hr from its usual speed	
	and the time of the flight increased by 30 min. Find the scheduled	
	duration of the flight.	
33	Prove that if a line is drawn parallel to one side of a triangle intersecting the other two sides in distinct points, then the other two sides are divided in the same ratio.	5
	Using the above theorem prove that a line through the point of intersection of the diagonals and parallel to the base of the trapezium divides the non-parallel sides in the same ratio.	

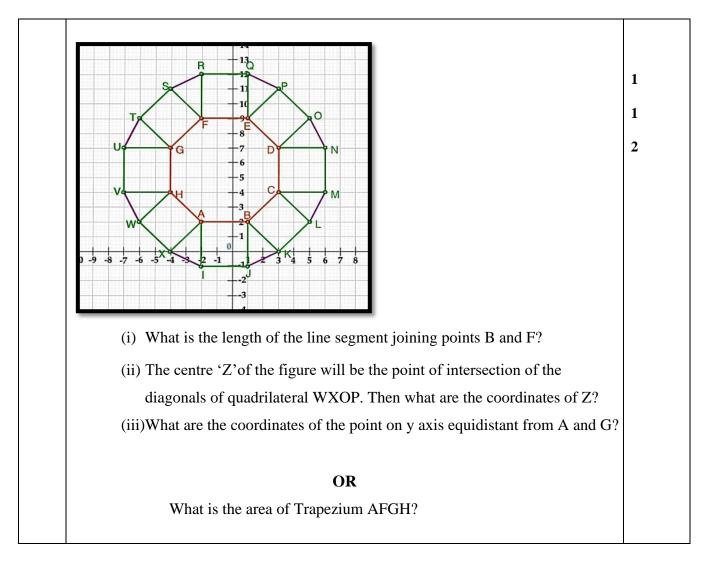


					-				
	Due to heavy flo	oods in a state	e, thousands v	were rendered homeless. 50	5				
	schools collectiv	ely decided to	o provide pla	ce and the canvas for 1500					
34	tents and share the	he whole exp	enditure equa	lly. The lower part of each					
	tent is cylindrica	l with base ra	dius 2.8 m ai	nd height 3.5 m and the upper					
	part is conical w	ith the same b	oase radius, b	ut of height 2.1 m. If the					
	canvas used to make the tents costs $\gtrless 120$ per m ² , find the amount shared by each school to set up the tents.								
			OR						
	There are two id	entical solid o		of side 7cm. From the top					
				eter equal to the side of the					
		-		-					
	-		-	verted and placed on the top					
	of the second cu	be's surface to	o form a dom	ie. Find					
	(i) The ratio	of the total s	urface area of	f the two new solids formed					
	(ii) Volume	of each new s	solid formed.						
	The median of the	following dat	a is 525 Find	the values of x and y, if the total	5				
35	frequency is 100	tonowing dat	a 18 <i>323</i> . Fillu	the values of x and y, if the total	5				
		Class	Frequency						
		interval							
		0-100	2						
		100-200	5						
		200-300	Х						
		300-400	12						
		400-500	17						
		500-600	20						
		600-700	У						
		700-800	9						
		800-900	7						
		900-1000	4						

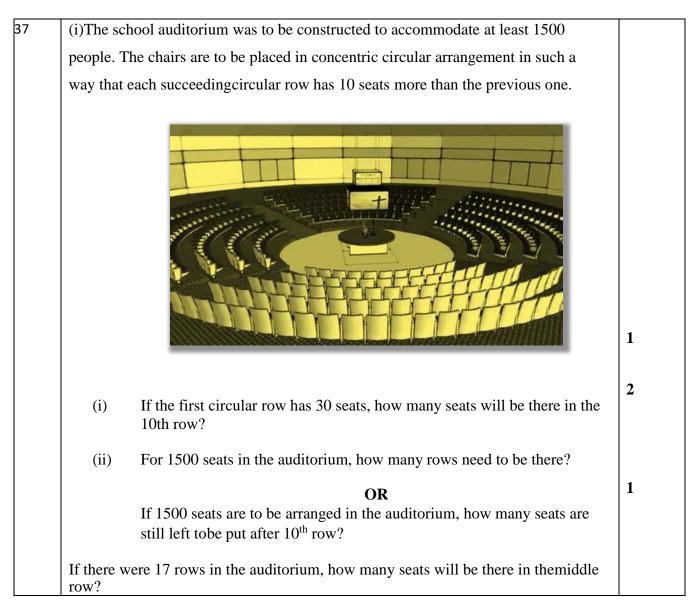


	SECTION E	
	Case study-based questions are compulsory.	
36	A tiling or tessellation of a flat surface is the covering of a plane using one or more	
	geometric shapes, called tiles, with no overlaps and no gaps. Historically,	
	tessellations were used in ancient Rome and in Islamic art. You may find tessellation	
	patterns on floors, walls, paintings etc. Shown below is a tiled floor in the	
	archaeological Museum of Seville, made using squares, triangles and hexagons.	
	A craftsman thought of making a floor pattern after being inspired by the above design. To ensure accuracy in his work, he made the pattern on the Cartesian plane. He used regular octagons, squares and triangles for his floor tessellation pattern Use the above figure to answer the questions that follow:	



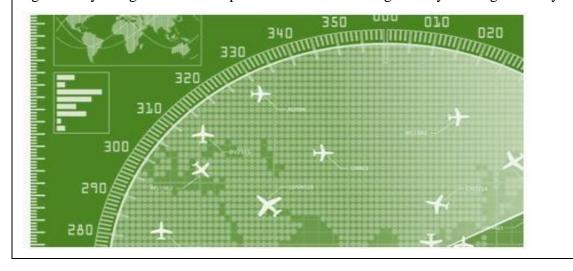








38 We all have seen the airplanes flying in the sky but might have not thought of how they actually reach the correct destination. Air Traffic Control (ATC) is a service provided by ground-based air traffic controllers who direct aircraft on the ground and through a given section of controlled airspace, and can provide advisory services to aircraft in non-controlled airspace. Actually, all this air traffic is managed and regulated by using various concepts based on coordinate geometry and trigonometry.



Γ



At a given instance, ATC finds that the angle of elevation of an airplane from a point	
on the ground is 60° . After a flight of 30 seconds, it is observed that the angle of	
elevation changes to 30°. The height of the plane remains constantly as $3000\sqrt{3}$ m. Use	1
the above information to answer the questions that follow-	2
(i) Draw a neat labelled figure to show the above situation diagrammatically.	
(ii) What is the distance travelled by the plane in 30 seconds?	
OR	
Keeping the height constant, during the above flight, it was observed that	1
after $15(\sqrt{3} - 1)$ seconds, the angle of elevation changed to 45° . How much	
is the distance travelled in that duration.	
(iii)What is the speed of the plane in km/hr.	



SAMPLE QUESTION PAPER -1 ANSWERS SUBJECT:MATHEMATICS-STANDARD CLASS X

SECTION - A

1	(c) 35
2	(b) x^2 -(p+1)x +p=0
3	(b) 2/3
4	(d) 2
5	(c) (2, -1)
6	(d) 2:3
7	(b) tan 30°
8	(b) 2
9	(c) $x = \frac{ay}{a+b}$

- **10** (c) 8cm
- **11** (d) $3\sqrt{3}$ cm



12	(d) 9π cm ²	
	(c) 96 cm ² (b) 12	
15	(d) 7000	
16	(b) 25	
17	(c) 11/36	
18	(a) 1/3	
19	(b) Both assertion (A) and reason (R) are true and reason (R) is not the correct assertion (A)	explanation of
	20. (a) Both assertion (A) and reason (R) are true and reason (R) is the correct of assertion (A)	explanation

SECTION – B

21 x = 11/2

y = 9/2

22 $In \Delta ABC,$

 $\angle 1 = \angle 2$



1⁄2

 $\therefore AB = BD \dots (i)$

Given,

AD/AE = AC/BD

Using equation (i), we get

AD/AE = AC/AB(ii)

In \triangle BAE and \triangle CAD, by equation (ii),

AC/AB = AD/AE

 $\angle A = \angle A \text{ (common)}$

: $\Delta BAE \sim \Delta CAD$ [By SAS similarity criterion]

∠PAO = ∠ PBO = 90₀ (angle b/w radius and tangent)
∠AOB = 105₀ (By angle sum property of a triangle)
∠AQB = ½ x105₀ = 52.5₀ (Angle at the remaining part of the circle is half the angle subtended by the arc at the centre)

24 We know that, in 60 minutes, the tip of minute hand moves 360.

In 1 minute, it will move $=360^{\circ}/60 = 6_{\circ}$

:. From 7 : 05 pm to 7: 40 pm i.e. 35 min, it will move through = $35 \times 6_0 = 210_0$

: Area of swept by the minute hand in 35 min = Area of sector with sectorial angle θ

of 210**O** and radius of 6 cm
=
$$\frac{7}{12} x \frac{22}{7} x 6 x 6$$



1⁄2

OR

$=66 cm^{2}$

OR

Let the measure of $\angle A$, $\angle B$, $\angle C$ and $\angle D$ be θ_1 , θ_2 , θ_3 and θ_4 respectively

Required area = Area of sector with centre A + Area of sector with centre B

+ Area of sector with centre C + Area of sector with centre D
=
$$\frac{\theta_1}{360} \times \pi \times 7^2 + \frac{\theta_2}{360} \times \pi \times 7^2 + \frac{\theta_3}{360} \times \pi \times 7^2 + \frac{\theta_4}{360} \times \pi \times 7^2$$

$$= \frac{(\theta_1 + \theta_2 + \theta_3 + \theta_4)}{360} \times \pi \times 7^2$$
$$= \frac{(360)}{360} \times \frac{22}{7} \times 7 \times 7 \text{ (By angle sum property of a triangle)}$$
$$= 154 \text{ cm}^2$$

25
$$sin(A+B) = 1 = sin 90$$
, so $A+B = 90$(i)

 $\cos(A-B) = \sqrt{3/2} = \cos 30$, so A-B = 30.....(ii)

From (i) & (ii) $\angle A = 60^{\circ}$

And
$$\angle B = 30^{\circ}$$

 $\frac{\cos\theta - \sin\theta}{\cos\theta + \sin\theta} = \frac{1 - \sqrt{3}}{1 + \sqrt{3}}$

Dividing the numerator and denominator of LHS by $\cos\theta$, we get

$$\frac{1-\tan\theta}{1+\tan\theta} = \frac{1-\sqrt{3}}{1+\sqrt{3}}$$

Which on simplification (or comparison) gives $tan\theta = \sqrt{3}$

Or $\theta = 60^{\circ}$

SECTION - C

26 Let us assume $5 + 2\sqrt{3}$ is rational, then it must be in the form of p/q where p and 1 q are co-prime i.e $5 + 2\sqrt{3} = p/q$ integers and $q \neq 0$

So $\sqrt{3} = \frac{p-5q}{2q}$(i)

Since p, q, 5 and 2 are integers and $q \neq 0$, HS of equation (i) is rational. But

LHS of (i) is $\sqrt{3}$ which is irrational. This is not possible.

This contradiction has arisen due to our wrong assumption that $5 + 2\sqrt{3}$ is rational.

So, $5 + 2\sqrt{3}$ is irrational.

27 Let α and β be the zeros of the polynomial $2x^2$ -5x -3

Then $\alpha + \beta = 5/2$

And $\alpha\beta = -3/2$.

Let 2α and 2β be the zeros $x^2 + px + q$

Then $2\alpha + 2\beta = -p$ $2(\alpha + \beta) = -p$ $2 \ge 5/2 = -p$

So p = -5And $2\alpha \ge 2\beta = q$

 $4 \alpha \beta = q$





So q = 4 x - 3/2

28)

Let the actual speed of the train be x km/hr and let the actual time taken be y hour

Distance covered is xy km

If the speed is increased by 6 km/hr, then time of journey is reduced by 4 hours i.e., when speed is (x+6)km/hr, time of journey is (y-4) hours.

: Distance covered =(x+6)(y-4)

 \Rightarrow xy=(x+6)(y-4)

 $\Rightarrow -4x + 6y - 24 = 0$

 $\Rightarrow -2x+3y-12=0$(i)

Similarly xy=(x-6)(y+6)

 \Rightarrow 6x-6y-36=0

⇒x-y-6=0(ii)

Solving (i) and (ii) we get x=30 and y=24

Putting the values of x and y in equation (i), we obtain

MATHEMATICS / X / 2022 – 23



Distance = (30×24) km =720km.

Hence, the length of the journey is 720km.

OR

Let the number of chocolates in lot A be x

And let the number of chocolates in lot B be y

 \therefore total number of chocolates =x+y

Price of 1 chocolate = ₹ 2/3, so for x chocolates $= \frac{2}{3}x$

and price of y chocolates at the rate of $\mathbf{\overline{\xi}}$ 1 per chocolate =y.

∴ by the given condition $\frac{2}{3}x + y = 400$ $\frac{1}{2}$ $\Rightarrow 2x + 3y = 1200$ (i) Similarly $x + \frac{4}{5}y = 460$ $\frac{1}{2}$ $\Rightarrow 5x + 4y = 2300$ (ii)

Solving (i) and (ii) we get

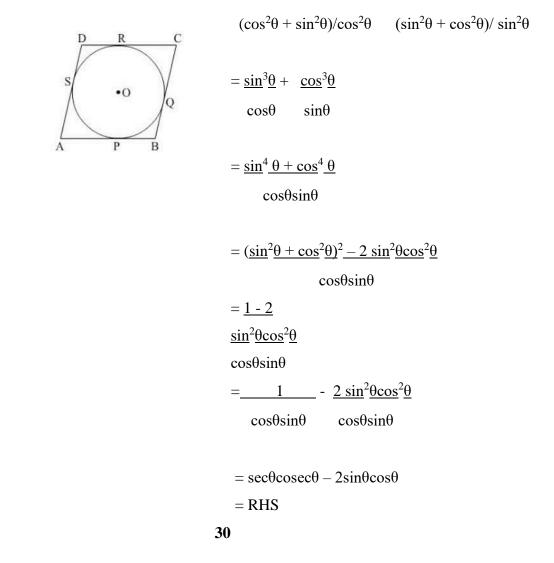
x=300 and y=200

∴x+y=300+200=500



So, Anuj had 500 chocolates.

29 LHS: $\underline{\sin^3\theta}/\cos^3\theta + \underline{\cos^3\theta}/\sin^3\theta$ $1+\sin^2\theta/\cos^2\theta + 1+\cos^2\theta/\sin^2\theta$



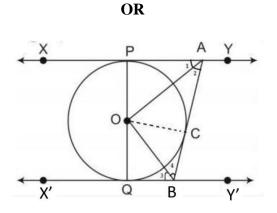


Let ABCD be the rhombus circumscribing the circle with centre O, such that AB, BC, CD and DA touch the circle at points P, Q, R and S respectively. We know that the tangents drawn to a circle from an exterior point are equal in length.

 $\therefore AP = AS.....(1)$ BP = BQ.....(2) CR = CQ(3) DR = DS.....(4). Adding (1), (2), (3) and (4) we get AP+BP+CR+DR = AS+BQ+CQ+DS (AP+BP) + (CR+DR) = (AS+DS) + (BQ+CQ) $\therefore AB+CD=AD+BC-----(5)$ Since AB=DC and AD=BC (opposite sides of parallelogram ABCD) putting in (5) we get, 2AB=2AD or AB = AD.

:AB=BC=DC=AD

Since a parallelogram with equal adjacent sides is a rhombus, so ABCD is a rhombus





Join OC

In \triangle OPA and \triangle OCA

OP = OC (radii of same circle)

PA = CA (length of two tangents from an external point)

AO = AO (Common)

Therefore, \triangle OPA $\cong \triangle$ OCA (By SSS congruency criterion)

Hence, $\angle 1 = \angle 2$ (CPCT)

Similarly $\angle 3 = \angle 4$

 $\angle PAB + \angle QBA = 180^{\circ}$ (co interior angles are supplementary as XYIX'Y')

 $2\angle 2 + 2\angle 4 = 180^{\circ}$

 $\frac{1}{2}$

 $\angle 2 + \angle 4 = 90^{\circ} - \dots - (1)$

 $\angle 2 + \angle 4 + \angle AOB = 180^{\circ}$ (Angle sum property)

Using (1), we get, $\angle AOB = 90^{\circ}$



31 (i) P (At least one head) $\frac{3}{4} =$ (ii) P(At most one tail) $= \frac{3}{4}$ (iii) P(A head and a tail) $= \frac{2}{4} = \frac{1}{2}$

SECTION D

32 Let the time taken by larger pipe alone to fill the tank= x hours .Therefore, the time taken by the smaller pipe = x+10 hours

Water filled by larger pipe running for 4 hours $=\frac{4}{x}$ litres

Water filled by smaller pipe running for 9 hours $=\frac{9}{x+10}$ litres

We know that

 $\frac{4}{x} + \frac{9}{x+10} = \frac{1}{2}$

Which on simplification gives:

$$x^{2}-16x-80=0$$

 $x^{2}-20x + 4x-80=0$
 $x(x-20) + 4(x-20)=0$
 $(x + 4)(x-20)=0$ x=-
4, 20 x cannot be
negative. Thus, x=20
 $x+10=30$



Larger pipe would alone fill the tank in 20 hours and smaller pipe would fill the tank alone in 30 hours.

OR

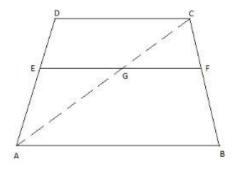
Let the usual speed of plane be x km/hr and the reduced speed of the plane be (x-200) km/hr Distance =600 km [Given] According to the question, $\frac{600}{x-200} - \frac{600}{x} = \frac{1}{2}$ (time taken at reduced speed) - (Schedule time) = 30 minutes = 0.5 hours.

the scheduled duration of the flight is =1hour

33

For the Theorem : Given, To prove, Construction and figure Proof





Let ABCD be a trapezium DC AB and EF is a line parallel to AB and hence to DC.

To prove : $\frac{DE}{EA} = \frac{CF}{FB}$

Construction : Join AC, meeting EF in G.

Proof :

In \triangle ABC, we have

 $GF\|AB$

CG/GA=CF/FB [By BPT](1)

In \triangle ADC, we have

EG || DC (EF || AB & AB || DC)

DE/EA = CG/GA [By BPT](2)

From (1) & (2), we get,



$$\frac{DE}{EA} = \frac{CF}{FB}$$

34. Radius of the base of cylinder (r) = 2.8 m = Radius of the base of the cone(r)

Height of the cylinder (h)=3.5 m

Height of the cone (H)=2.1 m.

Slant height of conical part (l)= $\sqrt{r^2+H^2}$

 $=\sqrt{(2.8)^2+(2.1)^2}$

 $=\sqrt{7.84}+4.41$

 $=\sqrt{12.25}=3.5$

Area of canvas used to make tent = CSA of cylinder + CSA of cone

$$= 2 \times \pi \times 2.8 \times 3.5 + \pi \times 2.8 \times 3.5$$

= 61.6 + 30.8

$$= 92.4 m^2$$

Cost of 1500 tents at ₹120 per sq.m



 $= 1500 \times 120 \times 92.4$

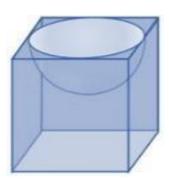
= 16,632,000

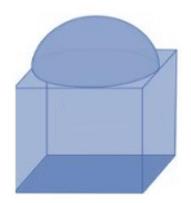
Share of each school to set up the tents = 16632000/50 = ₹332,640

OR

First Solid

Second Solid





(i) SA for first new solid (S₁): $6 \times 7 \times 7 + 2 \pi \times 3.5^2 - \pi \times 3.5^2$ $= 294 + 77 - 38.5 = 332.5 \text{ cm}^2$ SA for second new solid (S₂): $6 \times 7 \times 7 + 2 \pi \times 3.5^2 - \pi \times 3.5^2$ = 294 + 77 - 38.5 $= 332.5 \text{ cm}^2$ So S₁: S₂ = 1:1



(ii) Volume for first new solid $(V_1)=$

$$= 343 - \frac{539}{6} = \frac{1519}{6} \,\mathrm{cm}^3$$

Volume for second new solid (V₂)= $7 \times 7 \times 7 + \frac{539}{6} = \frac{2597}{6} \text{ cm}^3$

= 343 + 539/6 = 25976/6 cm³



35 Median = 525, so Median Class = 500 - 600

Class	Frequency	Cumulative Frequency
interval		
0-100	2	2
100-200	5	7
200-300	Х	7+x
300-400	12	19+x
400-500	17	36+x
500-600	20	56+x
600-700	У	56+x+y
700-800	9	65+x +y
800-900	7	72+x+y
900-1000	4	76+x+y

76+x+y=100⇒x+y=24(i)
Median = 1 +
$$\frac{\overline{2}-cf}{f}$$
 x h

Since, l=500, h=100, f=20, cf=36+x and n=100

Therefore, putting the value in the Median formula, we get;

$$525 = 500 \quad \frac{50 - (36 + x)}{20} +$$

so x = 9

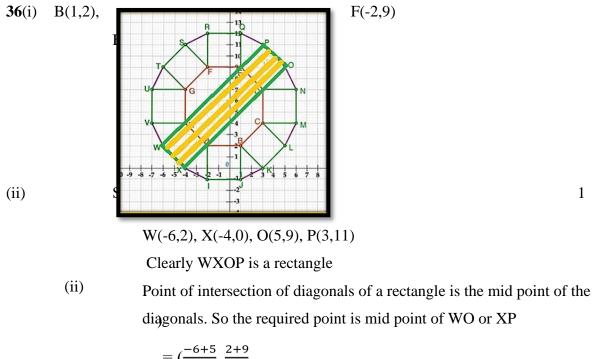


1

$$y = 24 - x$$
 (from eq.i) $y = 24 - 9 = 15$

Therefore, the value of x = 9

and y = 15.



$$= \left(\frac{-6+5}{2}, \frac{2+9}{2}\right)$$
$$= \left(\frac{-7}{2}\right) = \left(-\frac{1}{2}, -\frac{11}{2}\right)$$



(iii) A(-2,2), G(-4,7)

Let the point on y-axis be Z(0,y)

 $AZ^2 = GZ^2$

$$(0+2)^2 + (y-2)^2 = (0+4)^2 + (y-7)^2$$

 $(2)^2 + y^2 + 4 - 4y = (4)^2 + y^2 + 49 - 14y$

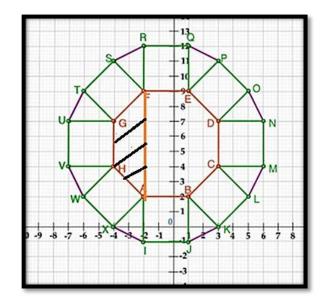
8-4y = 65-14y

10y= 57 So, y= 5.7

i.e. the required point is (0, 5.7)

OR





A(-2,2), F(-2,9), G(-4,7), H(-4,4)

Clearly GH = 7-4=3units

AF = 9-2=7 units

So, height of the trapezium AFGH = 2 units

So, area of AFGH =
$$\frac{1}{2}$$
(AF + GH) x height
 $\frac{1}{2}$ (7+3) x 2

= 10 sq. units

37. (i) Since each row is increasing by 10 seats, so it is an AP with first term a = 30,

and common difference d=10.

So number of seats in 10^{th} row = a_{10} = a+ 9d

 $= 30 + 9 \times 10 = 120$



(ii)
$$S_n = \frac{n}{2}(2a + (n-1)d)$$

 $1500 = \frac{n}{2}$
 $(2 \times 30 + (n-1)10)$
 $3000 = 50n + 10n^2$ $n^2 + 5n - 300 = 0$
 $n^2 + 20n - 15n - 300 = 0$ (n+20) (n-15)

Rejecting the negative value, n= 15

OR

=0

No. of seats already put up to the 10^{th} row = S_{10}

$$S_{10} = \frac{10}{2} \{2 \times 30 + (10 - 1)10)\}$$

= 5(60 + 90) = 750

So, the number of seats still required to be put are 1500 -750 = 750

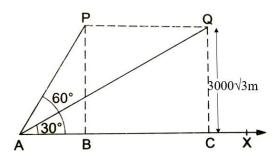
(iii) If no. of rows =17

then the middle row is the 9th row

 $a_8 = a + 8d$ = 30 + 80 = 110 seats

38 (i)





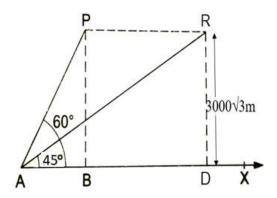


P and Q are the two positions of the plane flying at a height of $3000\sqrt{3}$ m. A is the point of observation.

(ii) In \triangle PAB, tan60° =PB/AB Or $\sqrt{3} = 3000\sqrt{3}$ / AB So AB=3000m tan30°= QC/AC $1/\sqrt{3} = 3000\sqrt{3}$ / AC AC = 9000m distance covered = 9000-3000 = 6000 m.

OR





In \triangle PAB, tan60° =PB/AB

Or $\sqrt{3} = 3000\sqrt{3}$ / AB

So AB=3000m

 $tan45^{\circ} = RD/AD$

 $1 = 3000\sqrt{3} / AD$

 $AD = 3000\sqrt{3} m$

distance covered = $3000\sqrt{3}$ - 3000

 $= 3000(\sqrt{3} - 1)m.$

(iii) speed = 6000/30

= 200 m/s

= 200 x 3600/1000

= 720 km/hr

Alternatively: speed = $3000(\sqrt{3} - 1)15(\sqrt{3} - 1)$

= 200 m/s = 200 x 3600/1000 = 720km/hr



Class - X Session 2022-23 Subject - Mathematics (Basic) Sample Question Paper

Time Allowed: 3 Hours

Maximum Marks: 80

General Instructions:

- 1. This Question Paper has 5 Sections A, B, C, D, and E.
- 2. Section A has 20 Multiple Choice Questions (MCQs) carrying 1 mark each.
- 3. Section B has 5 Short Answer-I (SA-I) type questions carrying 2 marks each.
- 4. Section C has 6 Short Answer-II (SA-II) type questions carrying 3 marks each.
- 5. Section D has 4 Long Answer (LA) type questions carrying 5 marks each.
- 6. Section E has 3 Case Based integrated units of assessment (4 marks each) with sub-parts of the values of 1, 1 and 2 marks each respectively.
- 7. All Questions are compulsory. However, an internal choice in 2 Qs of 2 marks, 2 Qs of 3 marks and 2 Questions of 5 marks has been provided. An internal choice has been provided in the 2 marks questions of Section E.
- 8. Draw neat figures wherever required. Take $\pi = 22/7$ wherever required if not stated.

	Section A	
	Section A consists of 20 questions of 1 mark each.	
SN		Ma
		rks
1	If two positive integers p and q can be expressed as p = ab2 and q = a3b; a, b being prime numbers, then LCM (p, q) is	1
	(a) ab (b) a2b2 (c) a3b2 (d) a3b3	



2	What is the greatest possible speed at which a man can walk 52 km and 91 km in an exact numb of hours?	er 1
	(a) 17 km/hours (b) 7 km/hours	
	(c) 13 km/hours (d) 26 km/hours	
3	If one zero of the quadratic polynomial x2 + 3x + k is 2, then the value of k is	1
	(a) 10 (b) -10 (c) 5 (d) —5	
4	Graphically, the pair of equations given by $6x - 3y + 10 = 0$	1
	2x - y + 9 = 0	
	represents two lines which are	
	(a) intersecting at exactly one point.(b) parallel.	
	(c) coincident. (d) intersecting at exactly two points.	
5	If the quadratic equation $x^2 + 4x + k = 0$ has real and equal roots, then	1
	(a) $k < 4$ (b) $k > 4$ (c) $k = 4$ (d) $k \ge 4$	
6	The perimeter of a triangle with vertices (0, 4), (0, 0) and (3, 0) is	1
	(a) 5 units (b) 12 units (c) 11 units (d) (7 + √5) units	
7	AB BC	1
	If in triangles ABC and DEF, DE = FD , then they will be similar, when	
	(a) $\angle B = \angle E$ (b) $\angle A = \angle D$ (c) $\angle B = \angle D$ (d) $\angle A = \angle F$	
8	In which ratio the y-axis divides the line segment joining the points $(5, -6)$ and $(-1, -4)$?.	1
	(a) 1 : 5 (b) 5 : 1 (c) 1 : 1 (d) 1 : 2	
L		



9	In the figure, if PA and PB are tangents to the circle with centre O such that $\angle APB = 50^\circ$, then	1
	∠OAB is equal to(a) 25° (b) 30° (c) 40° (d) 50°	
10		1
	If sin A = , then the value of sec A is :	
	2	
	(a) 2 (b) 1 (c) √3 (d) 1	
	V3 V3	
11	V3 cos2A + v3 sin2A is equal to	1
	(a) 1 (b) 1 (c) √3 (d) 0	
	v3	
12	The value of cos1°. cos2°. cos3°. cos4° cos90° is	1
	(a) 1 (b) 0 (c) – 1 (d) 2	
13	If the perimeter of a circle is equal to that of a square, then the ratio of their areas is	1
	(a) 22 : 7 (b) 14 : 11 (c) 7 : 22 (d) 11: 14	
14	If the radii of two circles are in the ratio of 4 : 3, then their areas are in the ratio of :	1
	(a) 4 : 3 (b) 8 : 3 (c) 16 : 9 (d) 9 : 16	
15	The total surface area of a solid hemisphere of radius 7 cm is :	1
	(a) 447π cm2 (b) 239π cm2 (c) 174π cm2 (d) 147π cm2	

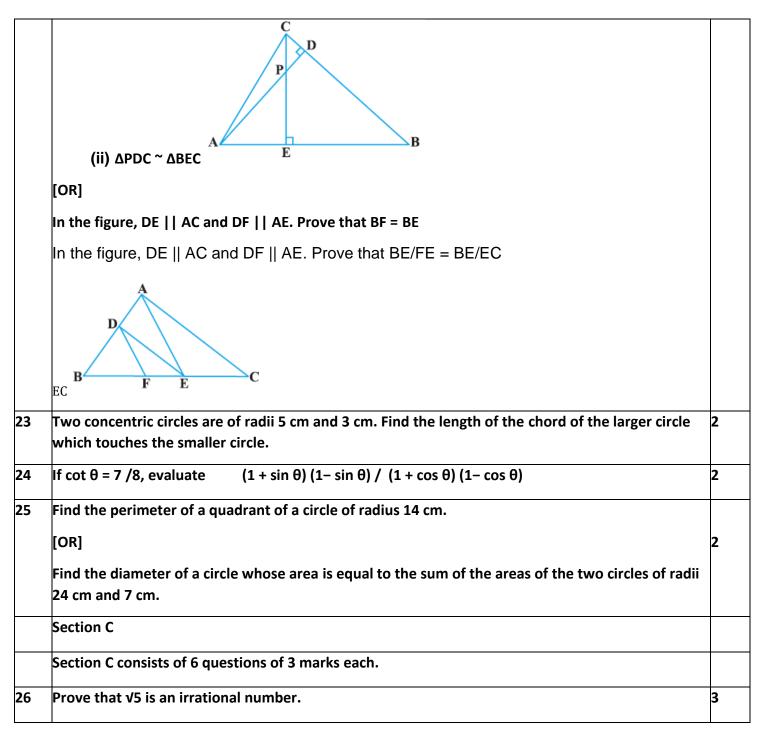


16	For the following on the upper limit of the time of time of the time of time of time of the time of ti								1	
	Class	0 - 5	5 - 10	10 - 15	15 - 20	20 - 25				
	Frequency	10	15	12	20	9				
,	(a) 10 (b) 15 (c) 2	:0 (d) 25							1	
	the following	Varia	ble (x)	1	2	3	2	4 5	¥	
	distribution is 2.6, then the value of y is	Freq	uency	4	5	у	· 1	1 2		
	(a) 3 (b) 8 (c) 1	.3 (d) 24								
}	A card is selected a red face card is	at random f	rom a wel	l shuffled d	leck of 52 o	cards. The	probability	y of its being a	1	
	(a)3/ 26 (b) 3/13 (c)2/ 13 (d) 1/2									
	Direction for quest followed by a state		-				ment of A	ssertion (A) is		



Assertion: If HCF of 510 and 92 is 2, then the LCM of 510 & 92 is 32460 Reason: as HCF(a,b) x LCM(a,b) = a x b	
Deth Acception (A) and Decean (D) are two and Decean (D) is the convect contention of Acception	
Both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of Assertion (A).	
Both Assertion (A) and Reason (R) are true but Reason (R) is not the correct explanation of Assertion (A).	
Assertion (A) is true but Reason (R) is false.	
Assertion (A) is false but Reason (R) is true.	
Assertion (A): The ratio in which the line segment joining (2, -3) and (5, 6) internally divided by x axis is 1:2.	1
Reason (R): as formula for the internal division is (^{mx2 + nx1} /m+n, ^{my2 + ny1} /m+n)	
Both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of Assertion (A).	
Both Assertion (A) and Reason (R) are true but Reason (R) is not the correct explanation of Assertion (A).	
Assertion (A) is true but Reason (R) is false.	
Assertion (A) is false but Reason (R) is true.	
Section B	
Section B consists of 5 questions of 2 marks each.	
For what values of k will the following pair of linear equations have infinitely many solutions? kx + 3y - (k - 3) = 0	2
12x + ky - k = 0	
In the figure, altitudes AD and CE of Δ ABC intersect each other at the point P. Show that: (i) Δ ABD ~ Δ CBE	2
	Both Assertion (A) and Reason (R) are true but Reason (R) is not the correct explanation of Assertion (A). Assertion (A) is true but Reason (R) is false. Assertion (A) is false but Reason (R) is true. Assertion (A): The ratio in which the line segment joining (2, -3) and (5, 6) internally divided by x axis is 1:2. Reason (R): as formula for the internal division is $(mx^2 + nx^1/m+n, my^2 + ny^1/m+n)$ Both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of Assertion (A). Both Assertion (A) and Reason (R) are true but Reason (R) is not the correct explanation of Assertion (A). Assertion (A) is true but Reason (R) is false. Assertion (A) is true but Reason (R) is false. Assertion (A) is false but Reason (R) is true. Section B Section B Section B Section B consists of 5 questions of 2 marks each. For what values of k will the following pair of linear equations have infinitely many solutions? kx + 3y - (k - 3) = 0 12x + ky - k = 0 In the figure, altitudes AD and CE of Δ ABC intersect each other at the point P. Show that:







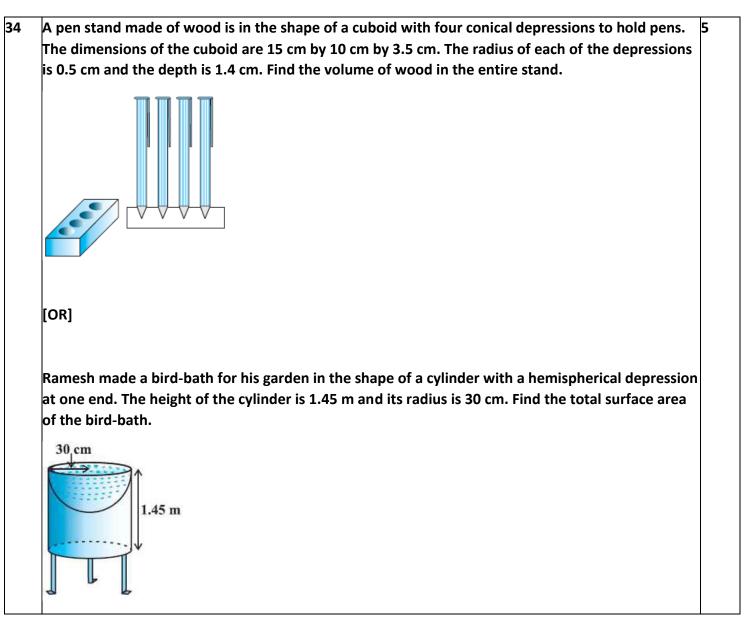
27	Find the zeroes of the quadratic polynomial $6x^2 - 3 - 7x$ and verify the relationship between the zeroes and the coefficients.	3		
28	A shopkeeper gives books on rent for reading. She takes a fixed charge for the first two days, and an additional charge for each day thereafter. Latika paid Rs 22 for a book kept for six days, while Anand paid Rs 16 for the book kept for four days. Find the fixed charges and the charge for each extra day.			
	[OR]			
	Places A and B are 100 km apart on a highway. One car starts from A and another from B at the same time. If the cars travel in the same direction at different speeds, they meet in 5			

	hours. If they travel towards each other, they meet in 1 hour. What are the speeds of the two cars?	
29	In the figure, PQ is a chord of length 8 cm of a circle of radius 5 cm. The tangents at P and Q intersect at a point	3
	T. Find the length TP.	
30	Prove that tan $\theta/1 - \cot \theta + \cot \theta/1 - \tan \theta = 1 + \sec \theta \csc \theta$ [OR] If sin θ + cos θ = $\sqrt{3}$, then prove that tan θ + cot θ = 1	3



31	Two dice are thrown at the same time. What is the probability that the sum of the two numbers	3
	appearing on the top of the dice is	
	(i) 8?	
	(ii) 13?	
	(iii) less than or equal to 12?	
	Section D	
	Section D consists of 4 questions of 5 marks each.	
32	An express train takes 1 hour less than a passenger train to travel 132 km between Mysore and Bangalore (without taking into consideration the time they stop at intermediate stations). If the average speed of the express train is 11km/h more than that of the passenger train, find the average speed of the two trains.	5
	[OR]	
	A motor boat whose speed is 18 km/h in still water takes 1 hour more to go 24 km upstream than to return downstream to the same spot. Find the speed of the stream.	
33	Prove that If a line is drawn parallel to one side of a triangle to intersect the other two sides in distinct points, the other two sides are divided in the same ratio. In the figure, find EC if AD/ DB = AE/ EC using the above	5
	theorem. $2 \text{ cm} \xrightarrow{A} 3 \text{ cm}$ $\overline{D} \xrightarrow{E}$ 6 cm $B \xrightarrow{C}$	







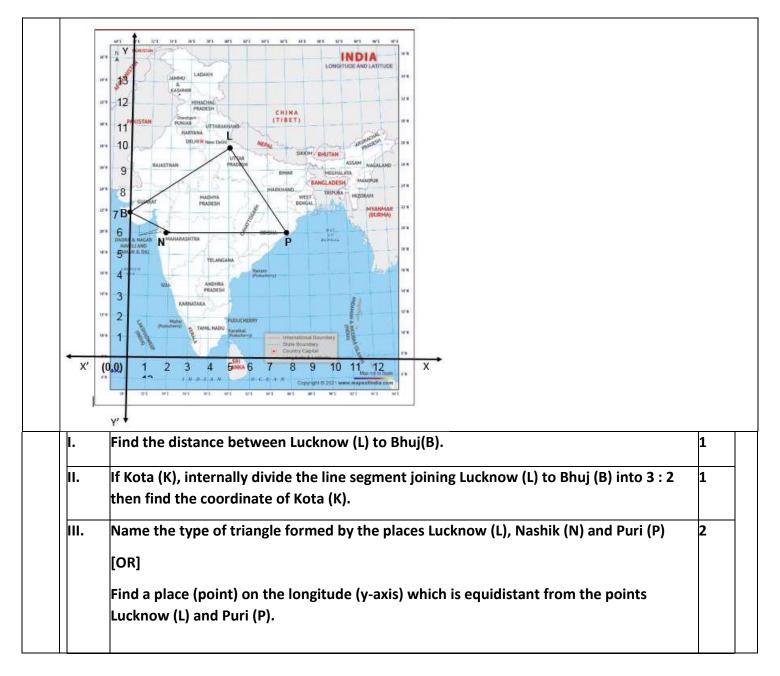
Age (in years)	(in years) Number of policy holders	
Below 20	2	
20-25 25-30	4	
	18	
30-35	21	
35-40 40-45 45-50 50-55 55-60	5-40 33	
	11	
	3	
	6 2	
Section E		
Case study based	questions are compulsory.	
Case Study – 1		
corresponding qu	arter of 2021–22, as per a repo ear and 2600 cars in 8th year. A	f passenger cars from India increased by 26% in rt. A car manufacturing company planned to pro ssuming that the production increases uniform



			7
l.	Find the production in the 1 st year.	1]
۱. ۱.	Find the production in the 1 st year. Find the production in the 12 th year.	1	
			-

37	Case Study – 2
	In a GPS, The lines that run east-west are known as lines of latitude, and the lines running north-south are known as lines of longitude. The latitude and the longitude of a place are its coordinates and the distance formula is used to find the distance between two places. The distance between two parallel lines is approximately 150 km. A family from Uttar
	Pradesh planned a round trip from Lucknow (L) to Puri (P) via Bhuj (B) and Nashik (N) as shown in the given figure below.







38 Case Study – 3

Lakshaman Jhula is located 5 kilometers north-east of the city of Rishikesh in the Indian state of Uttarakhand. The bridge connects the villages of Tapovan to Jonk. Tapovan is in Tehri Garhwal district, on the west bank of the river, while Jonk is in Pauri Garhwal district, on the east bank.

Lakshman Jhula is a pedestrian bridge also used by motorbikes. It is a landmark of Rishikesh.

A group of Class X students visited Rishikesh in Uttarakhand on a trip. They observed from a point (P) on a river bridge that the angles of depression of opposite banks of the river are 60° and 30° respectively. The height of the bridge is about 18 meters from the river.



Based on the above information answer the following questions.

Ι.	Find the distance PA.	1
11.	Find the distance PB	1



III.	Find the width AB of the river.	2
	[OR]	
	Find the height BQ if the angle of the elevation from P to Q be 30°.	



Class- X Mathematics Basic (241) Marking Scheme SQP-2022-23

Time Allowed: 3 Hours

Maximum Marks: 80

Section A	
(c) a ³ b ²	1
(c) 13 km/hours	1
(b) -10	1
(b) Parallel.	1
(c) k = 4	1
(b) 12	1
(c) $\angle B = \angle D$	1
(b) 5 : 1	1
(a) 25°	1
(a) ²	1
$\sqrt{3}$	
(c) √3	1
(b) 0	1
	(c) a^3b^2 (c) 13 km/hours (b) -10 (b) Parallel. (c) k = 4 (b) 12 (c) $\angle B = \angle D$ (b) 5 : 1 (a) 25° (a) 25° (c) $\sqrt{3}$



13	(b) 14 : 11	1
14	(c) 16 : 9	1
15	(d) 147π cm ²	1
16	(c) 20	1
17	(b) 8	1
18	(a)	1
	^{3/} 26	
19	(d) Assertion (A) is false but Reason (R) is true.	1

20	(a) Both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of Assertion (A).	1
	Section B	
21	For a pair of linear equations to have infinitely many solutions :	
	$a_1 = b_1 = c_1 \implies k = 3 = k - 3 a_2 b_2 c_2$ 12 k k	1⁄2
	$k = {}^{3} \Rightarrow k^{2} = 36 \Rightarrow k = \pm 6$	1/2
	12 k	
	Also, ${}^3 = {}^{k-3} \Rightarrow k^2 - 6k = 0 \Rightarrow k = 0, 6$	1⁄2
	k k	1⁄2
	Therefore, the value of k , that satisfies both the conditions, is $k = 6$.	

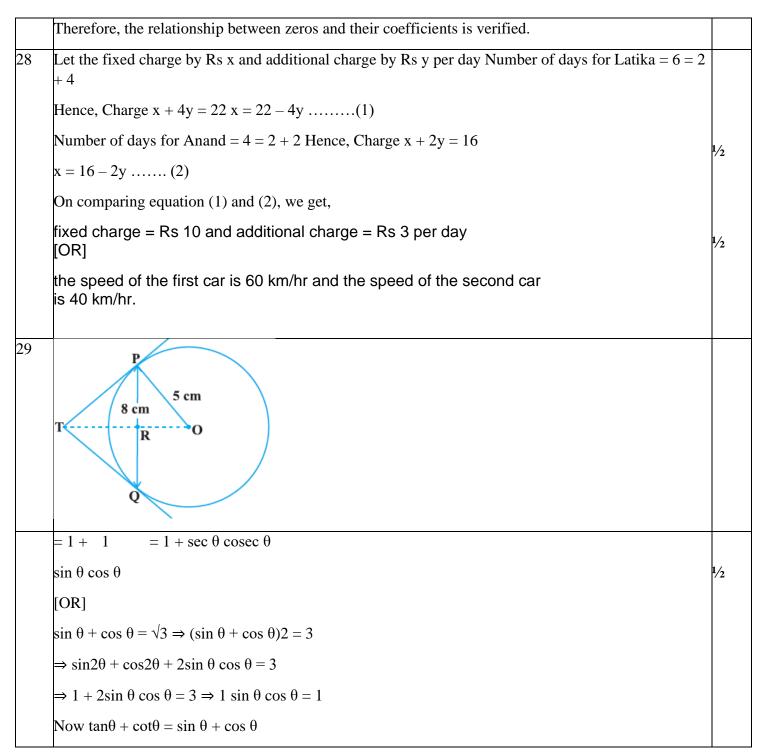


	-	
23	Let O be the centre of the concentric circle of radii 5 cm	
	and 3 cm respectively. Let AB be a chord of the larger circle touching the smaller circle at P	
	Then $AP = PB$ and $OP \perp AB$	
	Applying Pythagoras theorem in $\triangle OPA$, we have $OA^2 = OP^2 + AP^2 \Rightarrow 25 = 9 + AP^2$	1⁄2
	$\Rightarrow AP^2 = 16 \Rightarrow AP = 4 \text{ cm}$	
	$\therefore AB = 2AP = 8 cm$	1⁄2
		1⁄2
	5 cm 3 cm B	1/2
25	Perimeter of quadrant = $2r + 1 \times 2\pi r$	
	4	1/2
	$\Rightarrow \text{Perimeter} = 2 \times 14 + 1 \times 22 \times 14$	
	2 7	¹ /2 1
	$\Rightarrow \text{Perimeter} = 28 + 22 = 28 + 22 = 50 \text{ cm}$	
	[OR]	
	Area of the circle = Area of first circle + Area of second circle	1/2
	$\Rightarrow \pi R2 = \pi (r1)2 + \pi (r1)2$	1/2
	$\Rightarrow \pi R2 = \pi (24)2 + \pi (7)2 \Rightarrow \pi R2 = 576\pi + 49\pi$	
	$\Rightarrow \pi R2 = 625\pi \Rightarrow R2 = 625 \Rightarrow R = 25$ Thus, diameter of the circle $= 2R = 50$ cm.	1
	Section C	
L		



26		
	Let us assume to the contrary, that $\sqrt{5}$ is rational. Then we can find a and b ($\neq 0$) such that $\sqrt{5} = a$ (assuming that a and b are co-primes).	1
	b So, $a = \sqrt{5} b \Rightarrow a^2 = 5b^2$	_
	Here 5 is a prime number that divides a2 then 5 divides a also	
	(Using the theorem, if a is a prime number and if a divides p2, then a divides p, where a is a positive integer)	l/2
	Thus 5 is a factor of a	
	Since 5 is a factor of a, we can write $a = 5c$ (where c is a constant). Substituting $a = 5c$ We get $(5c)2 = 5b2 \Rightarrow 5c2 = b2$	1/2
	This means 5 divides b2 so 5 divides b also (Using the theorem, if a is a prime number and if a divides p2, then a divides p, where a is a positive integer).	
	Hence a and b have at least 5 as a common factor.	1/2
	But this contradicts the fact that a and b are coprime. This is the contradiction to our assumption that p and q are co-primes.	
	So, $\sqrt{5}$ is not a rational number. Therefore, the $\sqrt{5}$ is irrational.	
		1/2
27	$6x2 - 7x - 3 = 0 \Rightarrow 6x2 - 9x + 2x - 3 = 0$	
	$\Rightarrow 3x(2x-3) + 1(2x-3) = 0 \Rightarrow (2x-3)(3x+1) = 0$	1/2
	$\Rightarrow 2x - 3 = 0 \& 3x + 1 = 0$	
	x = 3/2 & x = -1/3 Hence, the zeros of the quadratic polynomials are $3/2$ and $-1/3$.	1/2
	For verification	
	Sum of zeros = $-$ coefficient of x \Rightarrow 3/2 + (-1/3) = $-$ (-7) / 6 \Rightarrow 7/6 = 7/6	
	coefficient of x2	1
	Product of roots = constant $\Rightarrow 3/2 \times (-1/3) = (-3)/6 \Rightarrow -1/2 = -1/2$	
	coefficient of x2	1







	$\cos \theta isn \theta$	
	$=\sin 2\theta + \cos 2\theta \sin \theta \cos \theta$	
	= 1 $=$ 1 $=$ 1	
	$\sin\theta\cos\theta$ 1	
31	(i) $P(8) = 5$	1
	36	
	(ii) $P(13) = 0 = 0$	
	36	
	(iii) P(less than or equal to 12) = 1	
	Section D	
32	Let the average speed of passenger train = $x \text{ km/h}$. and the average speed of express train = $(x + 11) \text{ km/h}$	
	As per given data, time taken by the express train to cover 132 km is 1 hour less than the passenger train to cover the same distance. Therefore,	
	132 - 132 = 1	
	x x+11	
	$\Rightarrow 132 (x+11-x) = 1 \Rightarrow 132 x 11 = 1$	
	x(x+11) $x(x+11)$	
	$\Rightarrow 132 \times 11 = \mathbf{x}(\mathbf{x} + 11) \Rightarrow \mathbf{x}2 + 11\mathbf{x} - 1452 = 0$	
	$\Rightarrow x2 + 44x - 33x - 1452 = 0$	
	$\Rightarrow x (x + 44) - 33(x + 44) = 0 \Rightarrow (x + 44)(x - 33) = 0$	
	\Rightarrow x = -44, 33	
	As the speed cannot be negative, the speed of the passenger train will be 33 km/h and the speed of the express train will be $33 + 11 = 44$ km/h.	



	[OR]		
	Let the speed of the stream be x km/hr		
	So, the speed of the boat in upstream = $(18 - x)$ km/hr & the speed of the boat in downstream = $(18 + x)$ km/hr		
	ATQ, distance - distance $= 1$		
	upstream speed downstream speed		
	\Rightarrow 24 - 24 = 1		
	$18 - x \ 18 + x$		
	As speed to stream can never be negative, the speed of the stream is 6 km/hr.	1/2	
34	Volume of one conical depression = $1 \times \pi r^2 h$	1/2	
	3		
	$= 1 \times 22 \times 0.52 \times 1.4 \text{ cm}^3 = 0.366 \text{ cm}^3$		
	3 7		
	Volume of 4 conical depression = 4 x 0.366 cm3		
	= 1.464 cm3		
	Volume of cuboidal box = $L \times B \times H$		
	= 15 x 10 x 3.5 cm 3 = 525 cm 3		
	Remaining volume of box = Volume of cuboidal box – Volume of 4 conical depressions		
	= 525 cm3 - 1.464 cm3 = 523.5 cm3		
	[OR]		
	Let h be height of the cylinder, and r the common radius of the cylinder and hemisphere.		
	Then, the total surface area = CSA of cylinder + CSA of hemisphere		
	$=2\pi rh+2\pi r^2=2\pi r (h+r)$		
	$= 2 \times 22 \times 30 (145 + 30) \text{ cm}2$		



	7 = 2 x 22 x 30 x 17:	5 cm2			
	7				
	= 33000 cm2 = 3.3	m2			
35	Class Interval	Number of policy holders (f)	Cumulative Frequency (cf)		
	Below 20	2	2		
	20-25	4	6		
	25-30	18	24		
	30-35	21	45		
	35-40	33	78		
	40-45	11	89	1	
	45-50	3	92		1
	50-55	6	98] '	1
	55-60	2	100]	
n = 100 \Rightarrow n/2 = 50, Therefore, median class = 35 – 40, Class size, h = 5, Lower limit of median class, 1 = 35, frequency f = 33, cumulative frequency cf = 45 \Rightarrow Median = 1 + $\left[\frac{2}{f}\right] \times h$ \Rightarrow Median = 35 + $\left[\frac{50 - 45}{33}\right] \times 5$ = 35 + $\frac{25}{33}$ = 35 + 0.76 = 35.76 Therefore, median age is 35.76 years				14 14 1 1	¹ /2
		Section	n E		
36	1Since the production increases uniformly by a fixed number every year, the number of Cars manufactured in 1st, 2nd, 3rd,, years will form an AP.So, $a + 3d = 1800 \& a + 7d = 2600$ 1/2So $d = 200 \& a = 1200$ 1/2				
$\begin{array}{c c c c c c c c c c c c c c c c c c c $			1/2 1/2		



		\Rightarrow t ₁₂ = 3400	1/2	
	3	$S_n = {n \choose 2} a + (n-1)d] \Rightarrow S_{10} = {10 \choose 2} x \ 1200 + (10-1) \ 200]$	1⁄2	1
		$\Rightarrow S_{10} \stackrel{2}{=} \stackrel{13}{[2 x 1200 + 9 x 200]}^{2}$	1/	1
		\Rightarrow S ₁₀ = 5 x [2400 + 1800]	$\frac{1/2}{1/2}$	1
		$\Rightarrow S_{10} = 5 \times 4200 = 21000$	1/2	1
	[OR]			I
	Let in n years the production will reach to 31200 $n = \frac{n}{2} \left[2 + 2 \right] \left$			I
	$S_n = {n \brack 2} [2a + (n-1)d] = 31200 \Rightarrow {n \brack 2} x \ 1200 + (n-1)200] = 31200$			1
		$\Rightarrow n [2^{2} x 1200 + (n-1)200] = 31200 \Rightarrow n [12^{2} + (n-1)] = 312$	1⁄2	1
		$\Rightarrow n^2 + 11n - 312 = 0$		1
		$\Rightarrow n^{2} + 24n - 13n - 312 = 0$ $\Rightarrow (n + 24)(n - 13) = 0$	1⁄2	I
		\Rightarrow (n +24)(n -13) = 0 \Rightarrow n = 13 or - 24. As n can't be negative. So n = 13	1/2	1
	Case S	$\int \frac{1}{2\pi r^2} = $	/2	
37				
	1			
	-	$LB = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \Rightarrow LB = \sqrt{(0 - 5)^2 + (7 - 10)^2}$	1⁄2	1
		$LB = \sqrt{(5)^2 + (3)^2} \Rightarrow LB = \sqrt{25} + 9 \overline{LB} = \sqrt{34}$		1
		Hence the distance is $150\sqrt{34 \text{ km}}$	1⁄2	1
	2	Coordinate of Kota (K) is $\binom{3x5+2x0}{3+2}, \frac{3x7+2x10}{3+2}$	1/2	I
		3+2 3+2		I
		$-(^{15+0} 21+20) - (2^{41})$	1⁄2	I
		5 5 5		I
	3	L(5, 10), N(2,6), P(8,6)	1/2	
		$LN = \sqrt{(2-5)^2 + (6-10)^2} = \sqrt{(3)^2 + (4)^2} = \sqrt{9 + 16} = \sqrt{25} = 5$	1/2	I
		NP = $\sqrt{(8-2)^2 + (6-6)^2} = \sqrt{(4)^2 + (0)^2} = 4$	1⁄2	l
		PL = $\sqrt{(8-5)^2 + (6-10)^2} = \sqrt{(3)^2 + (4)^2} \Rightarrow LB = \sqrt{9+16} = \sqrt{25} = 5$		1
		as $LN = PL \neq NP$, so ΔLNP is an isosceles triangle.	1⁄2	1



[OR]	
Let A (0, b) be a point on the y – axis then $AL = AP$	
$\frac{1}{2} \sqrt{(5-0)^2 + (10-b)^2} = \sqrt{(8-0)^2 + (6-b)^2}$	1⁄2
$\Rightarrow (5)^{2} + (10 - b)^{2} = (8)^{2} + (6 - b)^{2}$ $\Rightarrow (5)^{2} + (10 - b)^{2} = (8)^{2} + (6 - b)^{2}$	1⁄2
$\Rightarrow 25 + 100 - 20b + b2 = 64 + 36 - 12b + b2 \Rightarrow 8b = 25 \Rightarrow b = 25/8$	1⁄2
So, the coordinate on y axis is (0, 25/8)	1⁄2
Study – 3	
	Let A (0, b) be a point on the y – axis then AL = AP $\frac{1}{\Rightarrow \sqrt{(5-0)2 + (10-b)2} = \sqrt{(8-0)2 + (6-b)2}}{\Rightarrow (5)2 + (10-b)2 = (8)2 + (6-b)2}$ $\Rightarrow 25 + 100 - 20b + b2 = 64 + 36 - 12b + b2 \Rightarrow 8b = 25 \Rightarrow b = 25/8$ So, the coordinate on y axis is (0, 25/8) Study – 3 Study – 3



1	$\sin 60^\circ = {}^{PC}$	1/2
	PA	
	$\Rightarrow \frac{\sqrt{3}}{2} = \frac{18}{PA} \Rightarrow PA = 12\sqrt{3} m$	1⁄2
2	$\sin 30^\circ = \frac{PC}{PB}$	1⁄2
	$\Rightarrow \frac{1}{2} \stackrel{18}{} \frac{18}{\text{PB}} \Rightarrow 36 \text{ m}$	1⁄2
3	$\tan 60^\circ = {}^{PC} \Rightarrow \sqrt{3} = {}^{18} \Rightarrow AC = 6 \sqrt{3} m$	1
	$\tan 30^\circ = \stackrel{PC}{\longrightarrow} \stackrel{1}{\underset{CB}{\longrightarrow}} \stackrel{AC}{\underset{CB}{\longrightarrow}} \stackrel{1}{\underset{CB}{\longrightarrow}} CB = 18 \sqrt{3} m$	1/2
	Width AB = AC + CB = $6\sqrt{3} + 18\sqrt{3} = 24\sqrt{3}$ m	1⁄2
	[OR]	
	$RB = PC = 18 \text{ m} \& PR = CB = 18 \sqrt{3 \text{ m}}$	1⁄2
	$\tan 30^\circ = \overset{QR}{\underset{PR}{\overset{PR}{\Rightarrow}}} \xrightarrow{1}_{\sqrt{3}} = \overset{QR}{\underset{18\sqrt{3}}{\overset{QR}{\Rightarrow}}} QR = 18 \text{ m}$	1
	PR $\sqrt{3}$ $18\sqrt{3}$ QB = QR + RB = 18 + 18 = 36m. Hence height BQ is 36m	1⁄2